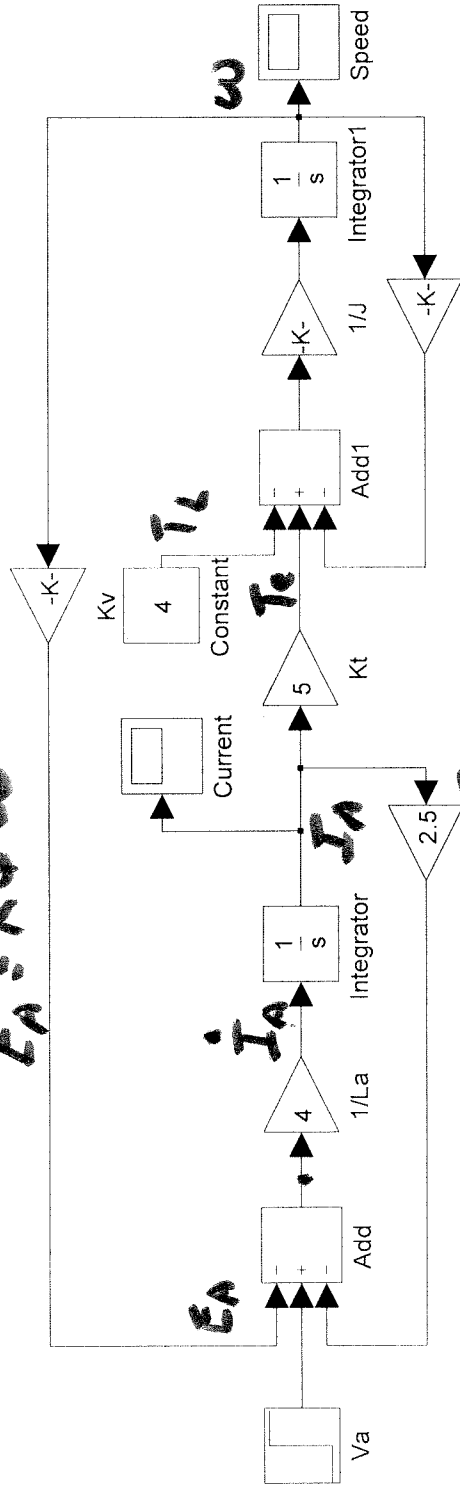


ECE 320 & ECE 329

ENERGY SYSTEMS I
BACKGROUND STUDY IN ENERGY SYSTEMS

SESSION no. 24

$$E_A = K \phi \omega$$



$$+V_A = E_A - I_A R_A = L \frac{dI_A}{dt}$$

$$T_e = K \phi I_A$$

$$T_e - T_L - b\omega = J \frac{d\omega}{dt}$$

$$\omega = 120 \frac{\text{rad}}{\text{sec}}$$

$$P = 15 \text{ hp}$$

$$P = 12 \text{ kW}$$

$$P = T\omega \Rightarrow T = 100 \text{ N}\cdot\text{m}$$

$$b\omega = 1 \text{ N}\cdot\text{m}$$

$$b = \frac{1}{120} \cdot \text{N}\cdot\text{m}\cdot\text{sec}$$

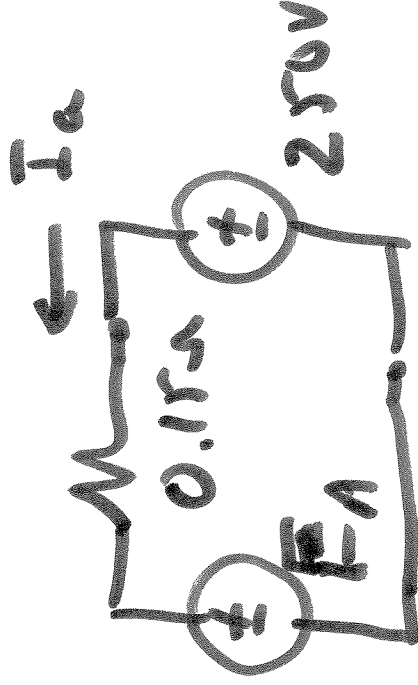
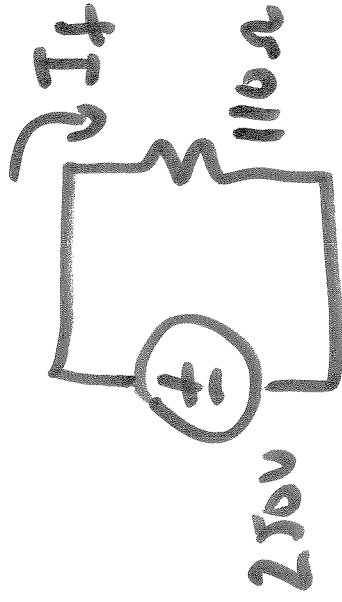
SEPARATELY SKETCHED

DC MOTOR

$$10 \text{ kW} \quad 250 \text{ V} \quad R_f = 110 \Omega \quad R_A = 0.15 \Omega$$

$$V_f = 250 \text{ V} \quad V_a = 250 \text{ V} \quad n = 1640 \text{ RPM}$$

a) FIND E_A



$$I_A = \frac{P}{V_A} = \frac{10 \text{ kW}}{250 \text{ V}} = 40 \text{ A}$$

$$E_A = V_A - I_A R_A$$

$$E_A = 250 \text{ V} - (40 \text{ A})(0.15 \Omega)$$

$$E_A = 244 \text{ V}$$

IF WE LOAD UP THE MOTOR,
WHAT HAPPENS TO SPEED?

$$\frac{E_A}{E_N} = K \phi \omega \quad \frac{250 \text{ V}}{244 \text{ V}} = \frac{\omega_{NL}}{\omega_{FL}}$$

b) Reduce V_A to 200V.

FIND SPEED, (SAMS)
CURRENT I_f AND FLUX
AND CURRENT I_A

$$E_A = V_A - I_A R_A$$

$$E_A = 200V - (40A)(0.15\Omega)$$

$$E_A = 194V$$

$$\frac{E_{A_{new}}}{K_a \phi_{new}} = \frac{K_a \phi_{old} \omega_{old}}{K_a \phi_{old} \omega_{old}}$$

$$\frac{E_{A_{new}}}{\omega_{new}} = \frac{K_a \phi_{old} \omega_{old}}{K_a \phi_{old} \omega_{old}}$$

$$\frac{2440}{1940} = \frac{1640 \text{ RPM}}{n_{\text{m2}}}$$

$$\underline{n_{\text{m2}} = 1304 \text{ RPM}}$$

c) FIND TORQUE AT BOTH CONNECTIONS

$$P_m = F_a I_a = T_e \omega \quad (1640 \text{ RPM}, \frac{2\pi \cdot 1640}{60} \text{ rad/sec})$$
$$(2440)(400) = T_e$$

$$\underline{T_e = 56.8 \text{ N.m}}$$

$$K_a \phi_d = \frac{2440}{(1640 \cdot \frac{2\pi}{60} \frac{\text{rad}}{\text{sec}})} = 1.42 \text{ V}\cdot\text{sec}$$

$$T_e = K_a \phi_d I_A$$

$$T_e = (1.42 \text{ V}\cdot\text{sec}) (40 \text{ A})$$

$$T_e = 56.8 \text{ N}\cdot\text{m}$$

$$T_e = K_a \phi_d I_A$$

d) Reduce I_A by $\frac{1}{2}$

\Rightarrow Torque $\times 3$

$$T_c \rightarrow \frac{1}{2} \dots$$

$$\text{or } \frac{1}{2} (56.8) \text{ N.m}$$

$$= \underline{\underline{28.4 \text{ N.m}}}$$

ECE 320

Energy Systems I

Lesson 24

DC Machine Examples

Torque is proportional to
CURRENT!

Speed is proportional to
VOLTAGE (generated voltage).