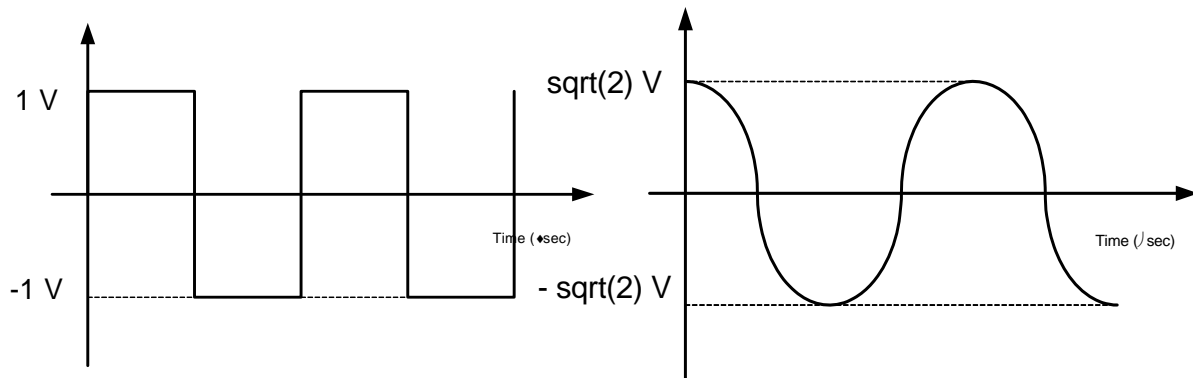


(4 points) On the axes given below, draw two different waveforms that each have an rms value of 1.0 Volts. Label the waveforms sufficiently that it is possible to calculate that rms value of 1.0 Volts from the labels that you provide.



2. (10 points) For the small power system shown below, the voltages and currents are as labeled. The three loads are identical.

a. (3 points) Find the voltage across the loads.

$$j := \sqrt{-1} \quad \text{VAr} := \text{V} \cdot \text{A}$$

$$V_s := 240 \cdot \text{V} \quad I_s := 4.2 \cdot e^{-j \cdot 25 \cdot \text{deg}} \cdot \text{A} \quad X_s := 5.0 \cdot \Omega$$

Use a loop equation.

$$V_L := V_s - j \cdot X_s \cdot I_s = (231.125 - 19.032i) \text{ V} \quad |V_L| = 231.907 \text{ V} \quad \arg(V_L) = -4.708 \cdot \text{deg}$$

b. (5 points) Find the real and reactive power consumed in one of the loads.

$$S_L := \frac{1}{3} \cdot (V_L \cdot \bar{I}_s) = (304.519 + 112.6i) \text{ W} \quad P_L := \text{Re}(S_L) = 304.519 \text{ W}$$

$$Q_L := \text{Im}(S_L) = 112.6 \cdot \text{VAr}$$

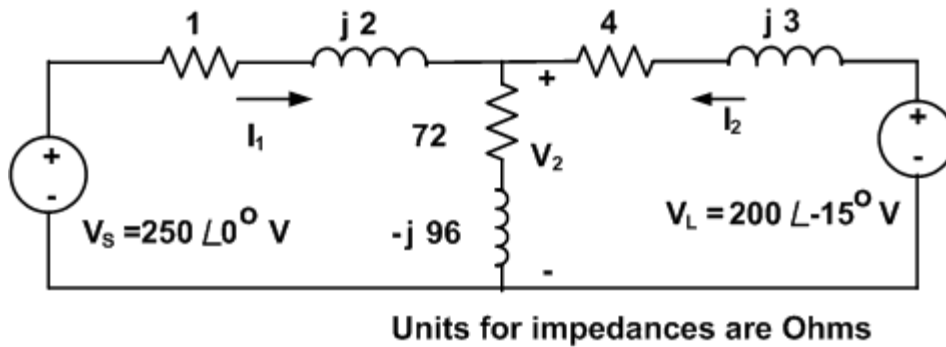
c. (2 points) If the frequency is 50 Hertz, what is the inductance of the line that connects the source to the loads?

The basic relation is  $X_s = \omega \cdot L_s$

$$\omega := 2 \cdot \pi \cdot 50 \cdot \frac{\text{rad}}{\text{sec}} = 314.159 \frac{1}{\text{s}} \quad X_s = 5 \Omega$$

$$L_s := \frac{X_s}{\omega} = 15.915 \cdot \text{mH}$$

3. (6 points) For the circuit shown below, write a set of linearly independent equations that can be solved for the voltage  $V_2$  and the current  $I_2$ . You need not solve the equations; just write them.



Here is one set of equations based on a node equation:

$$\frac{V_2 - 250}{1 + j \cdot 2} + \frac{V_2}{72 - j \cdot 96} + \frac{V_2 - 200 \cdot e^{-j \cdot 15 \cdot \text{deg}}}{4 + j \cdot 3} = 0$$

$$\frac{200 \cdot e^{-j \cdot 15 \cdot \text{deg}} - V_2}{4 + j \cdot 3} = I_2$$

Here is another set of equations based on loop equations:

$$-250 + (1 + j \cdot 2) \cdot I_1 + (72 - j \cdot 96) \cdot (I_1 + I_2) = 0$$

$$-200 \cdot e^{-j \cdot 15 \cdot \text{deg}} + (4 + j \cdot 3) \cdot I_2 + (72 - j \cdot 96) \cdot (I_1 + I_2) = 0$$

$$V_2 = (72 - j \cdot 96) \cdot (I_1 + I_2)$$