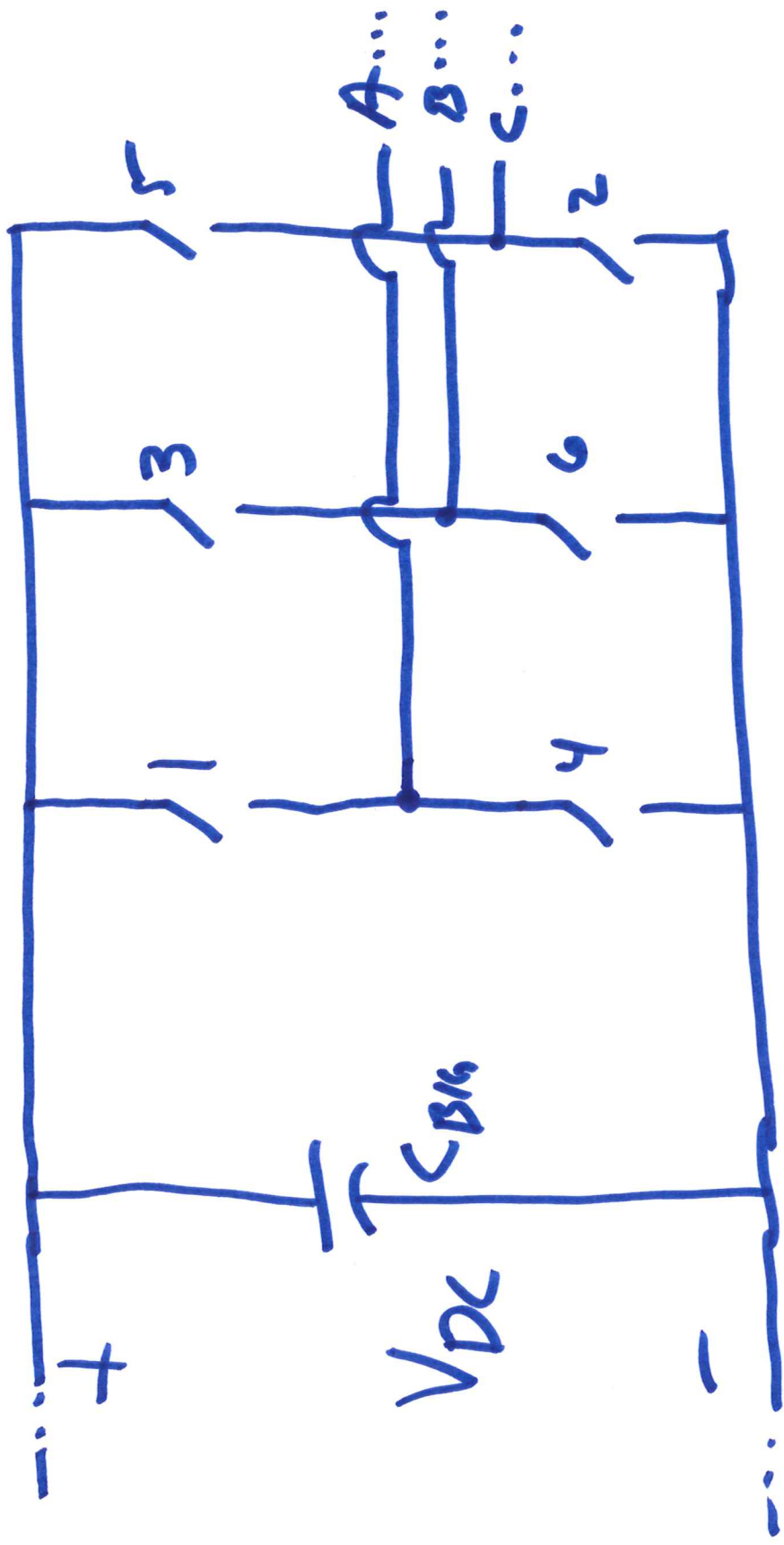
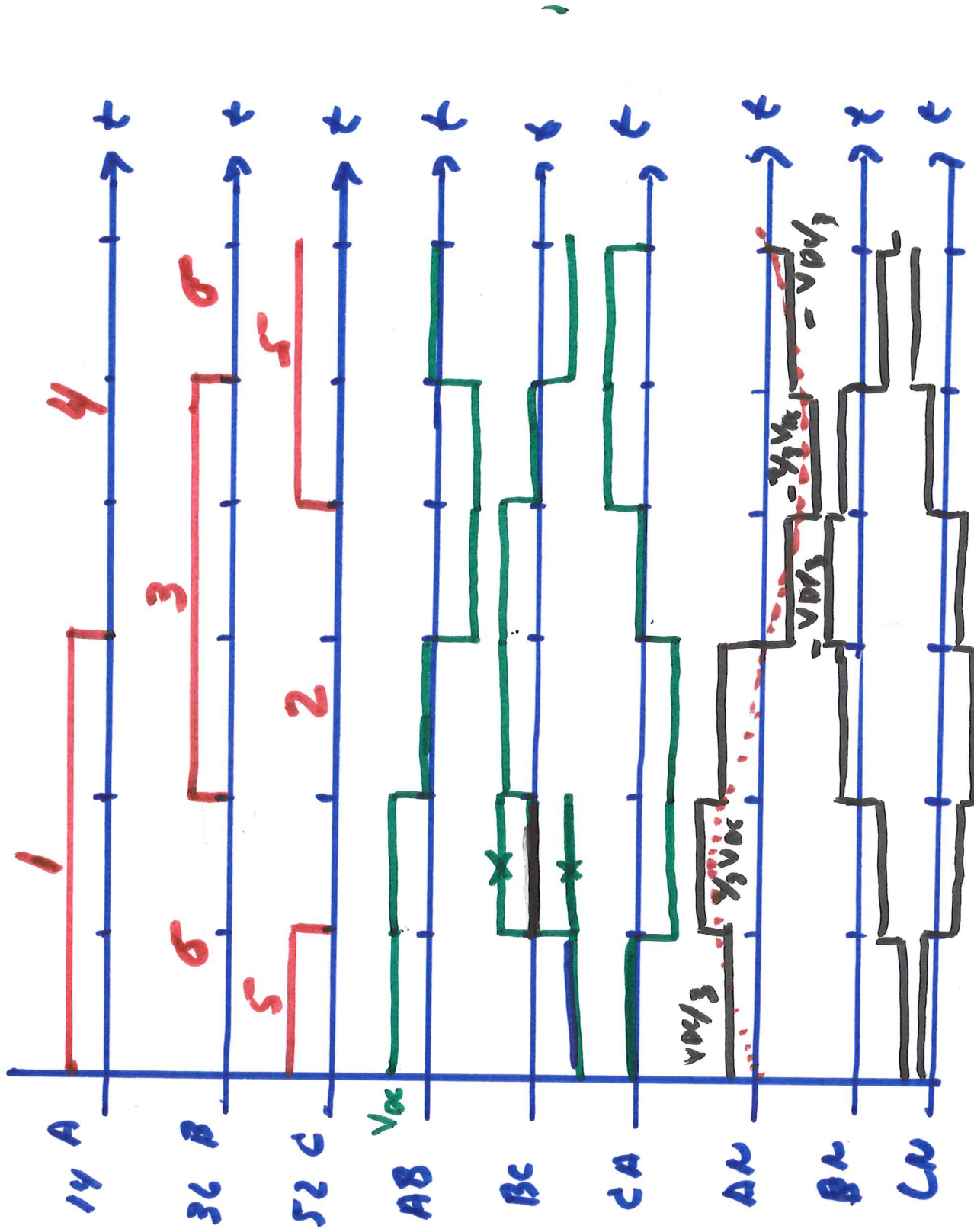


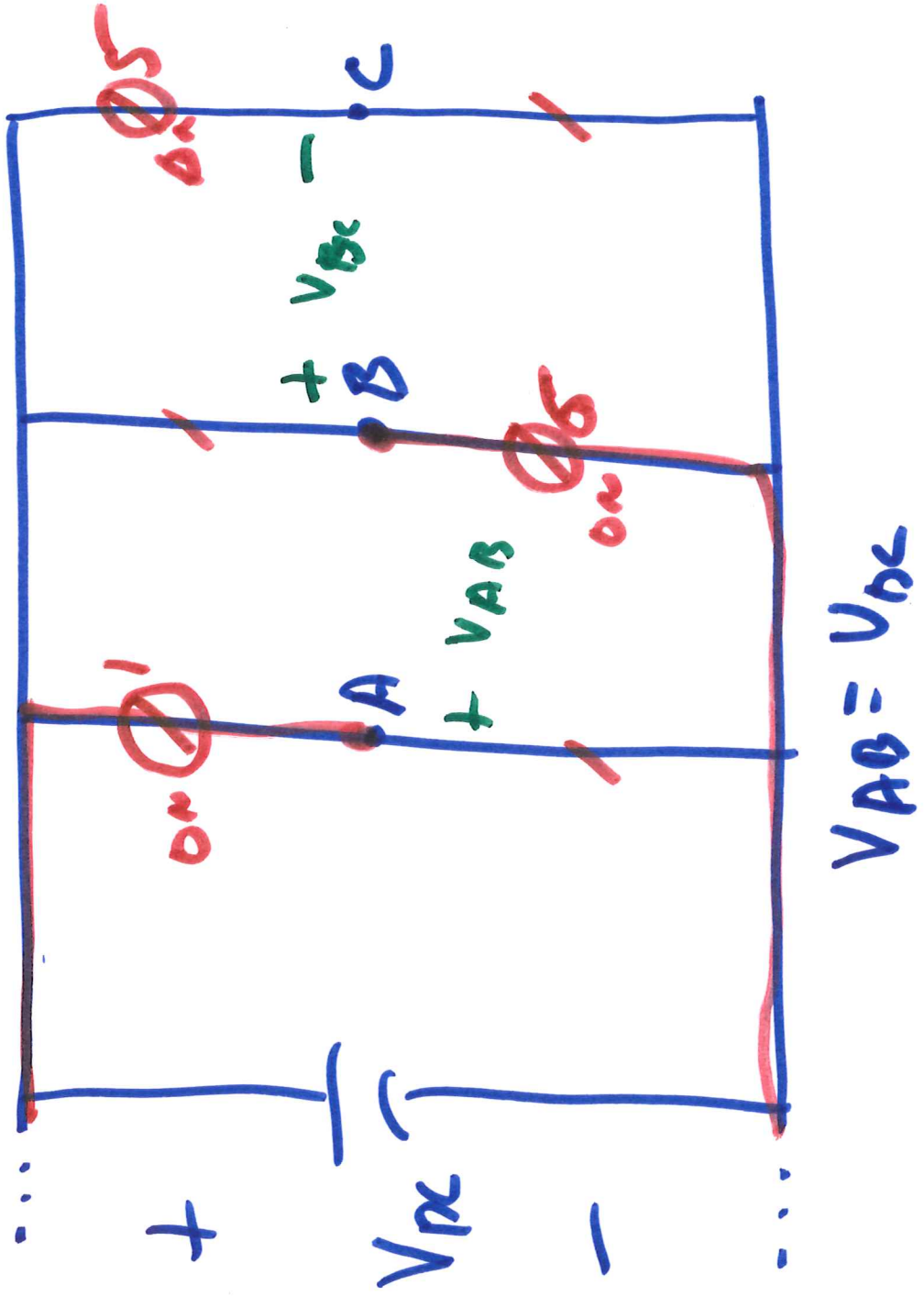
ECE 404-TD / 504-TD

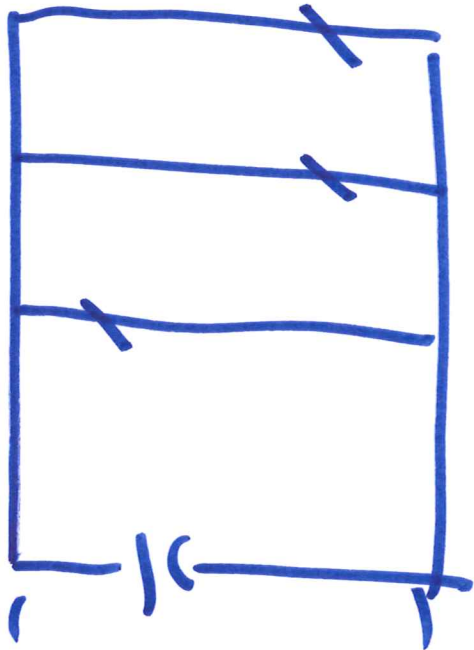
ST: T&D APPLICATIONS OF  
VOLTAGE SOURCE CONVERTERS

SESSION no. 11









612

$$V_{AB} = V_{AN} - V_{BN}$$

$$V_{BC} = V_{BN} - V_{CN}$$

$$0 = V_{AN} + V_{BN} + V_{CN}$$

$$\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} V_{AN} \\ V_{BN} \\ V_{CN} \end{bmatrix} = \begin{bmatrix} V_{AB} \\ V_{BC} \\ 0 \end{bmatrix}$$

$$\begin{pmatrix} V_{AN} \\ V_{BN} \\ V_{CN} \end{pmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ 1 & 1 & 1 \end{bmatrix}^{-1} \begin{pmatrix} V_{AB} \\ V_{AC} \\ 0 \end{pmatrix}$$

$$\begin{pmatrix} V_{AN} \\ V_{BN} \\ V_{CN} \end{pmatrix} = \frac{1}{3} \begin{bmatrix} 2 & 1 & 1 \\ -1 & 1 & 1 \\ -1 & -2 & 1 \end{bmatrix} \begin{pmatrix} V_{AB} \\ V_{BC} \\ 0 \end{pmatrix}$$



$$V_{AN_1} = \frac{2}{\pi} V_{DC} \sin(\omega t) \text{ V}$$

$$V_{BN_1} = \frac{2}{\pi} V_{DC} \sin\left(\omega t - \frac{2\pi}{3}\right) \text{ V}$$

$$V_{CN_1} = \frac{2}{\pi} V_{DC} \sin\left(\omega t + \frac{2\pi}{3}\right) \text{ V}$$



6N ± 1

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$$f = \sqrt{\frac{2}{\omega \mu \delta}}$$

**ECE 404 / 504**

**T & D Applications of Voltage  
Sourced Converters**

**Lesson 11**

**Three phase: Three power  
poles switching our DC input  
into AC output**

**Three power poles: six switches with one ON and one OFF in each power pole.**

**Three switches ON and three switches OFF at any time.**

**Switching is BREAK before MAKE.**

**In this way, we get a waveform set that has a certain three phase character to it.**

**What we have are the LINE-TO-LINE voltages at the output of the switching inverter.**

**Line-to-neutral voltages?**

**What does this ancient technology tell us?**

**By selecting our switching instants carefully, we can set/control the frequency, phase. We will eventually**

**figure out how to control the amplitude also.**

**What is the conservation of sorrows on these ancient waveforms?**

**☹ Harmonics!**

**We have set up waveforms with only ODD harmonics. At least we got rid of the even harmonics by using ODD symmetry.**

**For the three phase waveform,  
we have also rid ourselves of  
the triplen harmonics. 3, 6, 9,  
12, 15,...**

**What is so bad about having  
harmonics in the voltage (and  
current) waveforms that we  
send to our load?**

**Harmonics contribute mostly  
to losses. Useful power will**



**not appear in a synchronous machine from the harmonics. (Voltage and current at the same frequency is the only way to get real power.)**

**Harmonics contribute to vibrating torques and surface heating of the rotor.**

**Skin depth**

**Pulse width modulation**