

ECE 404-TD / 504-TD

**ST: T&D APPLICATIONS OF
VOLTAGE SOURCE CONVERTERS**

SESSION no. 35

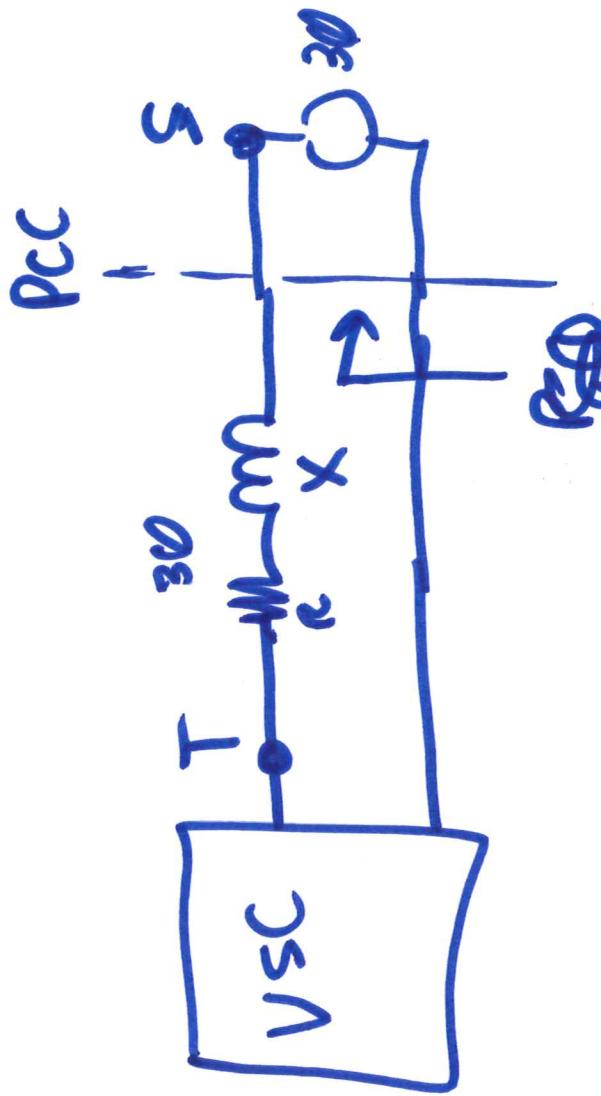
ECE 404/504: Homework #5

L34 L35 1.4
Due Session 37 (April 17)

RMC

1. Implement an averaged model of a three VSC with an AC source voltage of 2.4kV (L-L), $R = 0.096 \Omega$, $L = 3.82\text{mH}$ ($X/R = 15$) and a switching frequency of 3600Hz.
 - A. Determine V_{dc} if the maximum amplitude of the modulating function is 0.8 and the maximum reactive power the converter can supply is 4MVAR while transferring 0 MW (both measured at the source side of the R-L). Round up to nearest 10 V.
 - C. Generate open loop modulating functions ($m_a(t)$, $m_b(t)$, and $m_c(t)$) such that $P=4\text{MW}$ and $Q=0$. Verify that the converter supplies this using averaged models.
 - D. Generate open loop modulating functions such that $P=3.71\text{MW}$ and $Q=1.5\text{MVAR}$. Verify that the converter supplies this.
 - E. Generate open loop modulating functions such that $P=3.71\text{MW}$ and $Q=-1.5\text{MVAR}$. Verify that the converter supplies this.
 - F. Generate open loop modulating functions such that $P=-3.71\text{MW}$ and $Q=-1.5\text{MVAR}$. Verify that the converter supplies this.
 - G. ECE 504 students, implement using a switching model. Compare ac currents to those from the averaged models and the fundamental component of converter terminal voltages to averaged model results.
2. Now the VSC from problem 1 has a closed loop control scheme implemented in the synchronously rotating d-q reference frame. Assume that the source voltage is constant.
 - A. Determine the i_{dref} and i_{qref} such that $P=4\text{MW}$ and $Q=0$.
 - B. Determine the i_{dref} and i_{qref} such that $P=3.71\text{MW}$ and $Q=1.5\text{MVAR}$.
 - C. Determine the i_{dref} and i_{qref} such that $P=3.71\text{MW}$ and $Q=-1.5\text{MVAR}$
 - D. Determine the i_{dref} and i_{qref} such that $P=3.71\text{MW}$ and $Q=-1.5\text{MVAR}$
 - E. ECE 504 students implement cases A-D using closed loop control in your EMT program using averaged models.

Assume PLL $\rightarrow V_{sq} = 0$



$$P_{\text{out}} = -P_{\text{ST}}$$

$$Q_{\text{out}} = -Q_{\text{ST}}$$

$R \ll X \rightarrow$ approximate $R=0$ for calculations;

$$\begin{aligned}
 \bar{S}_{sr} &= \bar{V}_s \cdot \bar{I}_{sr}^* \\
 &\stackrel{\text{pu}}{=} \\
 &= \bar{V}_s \left(\frac{\bar{V}_s - \bar{V}_r}{jX} \right)^* \\
 &= \frac{|V_s|^2 - \bar{V}_s \bar{V}_r^*}{jX} \\
 &\quad \text{---} \delta \\
 &= \frac{|V_s|^2 / 0 - |V_s| |V_r| / \theta_{sr} - \theta_{vr}}{-jX}
 \end{aligned}$$

$$\bar{S}_{ST} = \frac{|V_S|^2 / 90^\circ - |V_S| |V_T| \sqrt{0-\delta + 90^\circ}}{X}$$

$$P_{ST} = \operatorname{Re}(\bar{S}_{ST}) = \frac{|V_S| |V_T|}{X} \sin(0-\delta)$$

$$\cos(\alpha + 90^\circ) = -\sin(\alpha)$$

$$P_{out} = -P_{ST} = \frac{|V_S| |V_T|}{X} \underbrace{\sin(\delta-\alpha)}_{-\sin(0-\delta) = \sin(\delta-\alpha)}$$

$$P_{TS} = -P_{ST} \quad \text{Since } R=0$$

}

$$\Theta_{ST} = \operatorname{Im}(\bar{S}_{ST})$$

$$= |V_S|^2 - |V_S| |V_T| \frac{\cos(\alpha-\delta)}{X}$$

$$\sin(\alpha + \delta) = \cos(\alpha) \cancel{\sin(\delta)} \cancel{\cos(\delta-\alpha)} = \cos(\delta)$$

$$Q_{\text{out}} = -Q_{ST} = -\frac{|V_S|^2}{X} + \frac{|V_S| |V_T| \cos(\alpha-\delta)}{X}$$

$$Q_{TS} = |V_+|^2 - |V_-| |V_S| \cos(\delta - \theta)$$

X

$Q_{TS} \neq -Q_{ST}$ in general

They differ by $|I|^2 X$

$$m(t) = \frac{N}{\omega} \cos(\omega t + \delta)$$

peak amplitude of m

$3Q$ P, Q with # Volts, ohm --

$$\bar{S}_{30} = 3 |V_{en}| |I_{\theta}| |(6 - \delta_x)|$$

$$S_{30} = 3 \left(\frac{|V_{AS}|^2 |q_0| - |V_{AS}| |V_{AT}| |(6 - \delta + 90^\circ)|}{X} \right)$$

$$|V_{el}| = \sqrt{3} |V_{en}| -$$

$$S_{30} = \frac{|V_{ASU}|^2 |q_0| - |V_{ASU}| |V_{ATU}| |(6 - \delta + 90^\circ)|}{X}$$

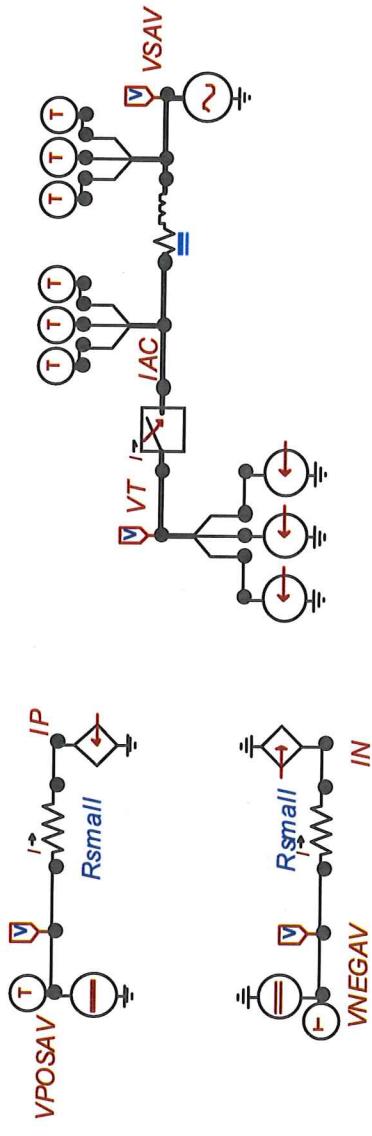
- Easiest way to get P, Q measured
in ATP

$\Rightarrow V_{SAG} \rightarrow$ have proxy find
 V_L, Θ_M

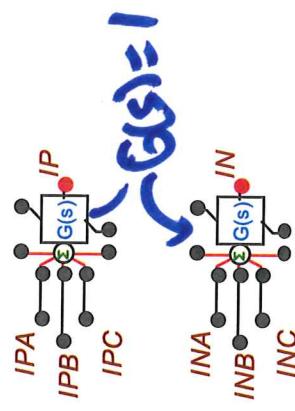
Same for $I_A \rightarrow I_L, \Theta_M$
calculate P, Q
off line

P and Q output from VSC and Applying Transformations

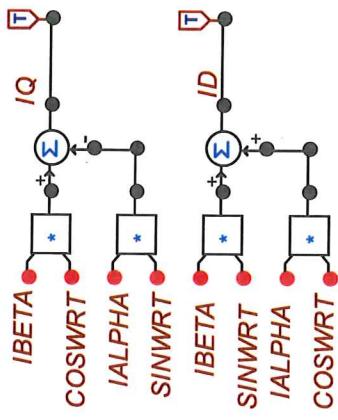
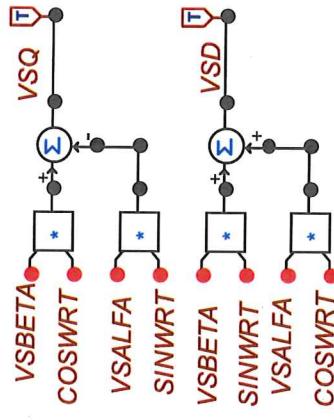
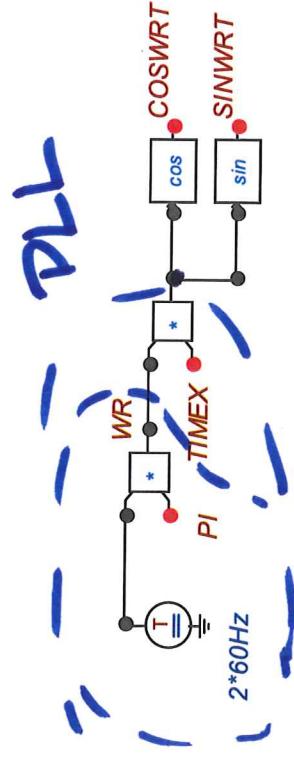
- Averaged Model Circuit



- Only a single current source on each rail in the DC bus -- take sum in TACS



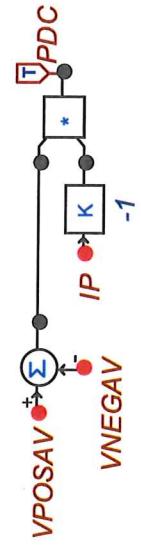
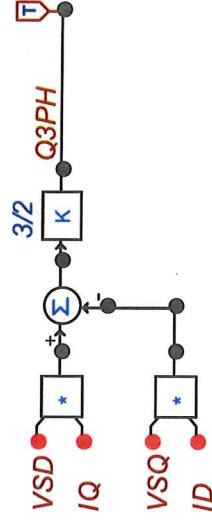
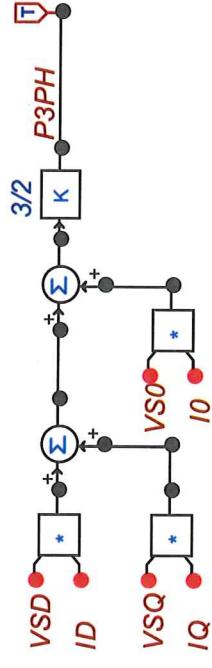
Synchronous DQ Transform



L35 19/11

L35 11/11

Calculate P and Q at PCC



~~↓ correct polarity or calculation~~

$$P = \frac{3}{2} (V_{SD} i_q + V_{SG} (q))$$

○ from PUL

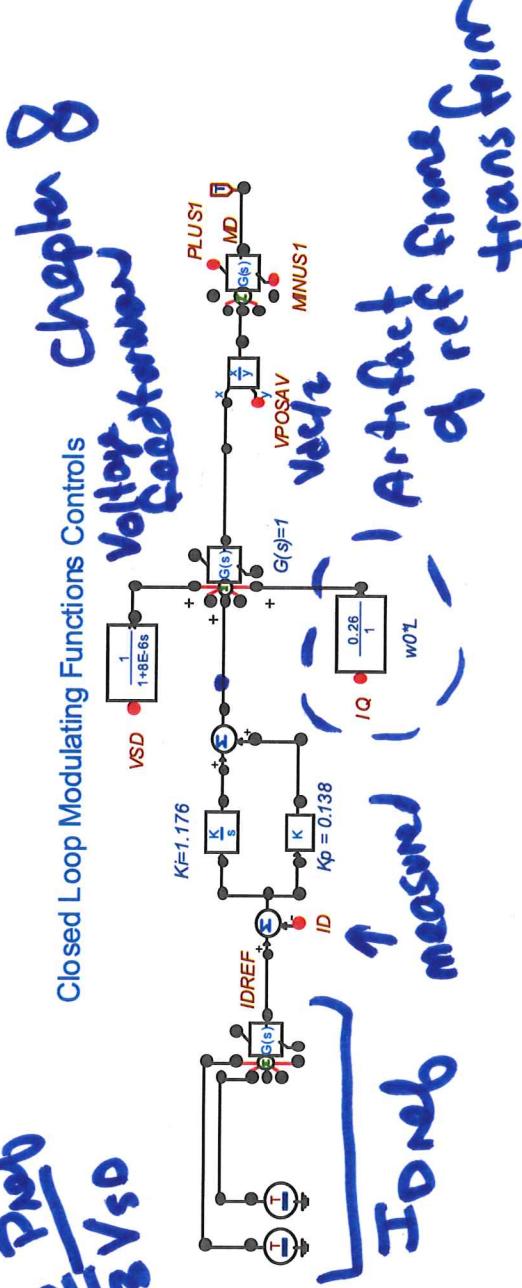
measured
volt at PCC

$$Q = -\frac{3}{2} (V_{SG} i_q - V_{SD} (q))$$

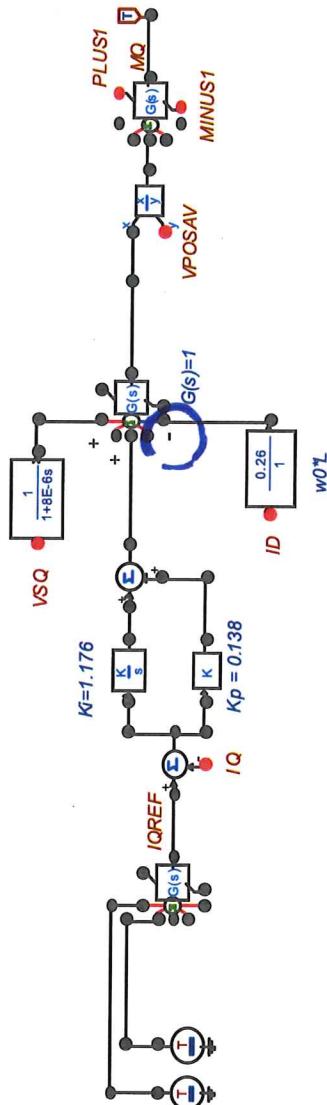
$$i_q = -\frac{Q_{ref}}{V_{SD}} \frac{2}{3}$$

13/14

$$I_{DQ} = \frac{2}{3} \frac{P_{\text{ref}}}{V_{S0}}$$

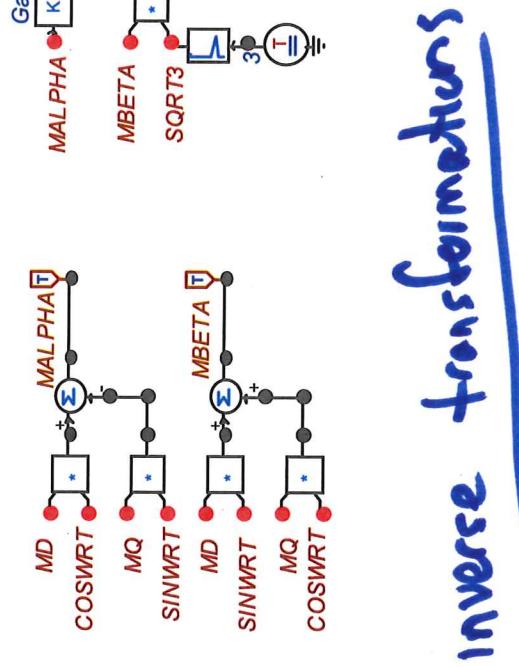
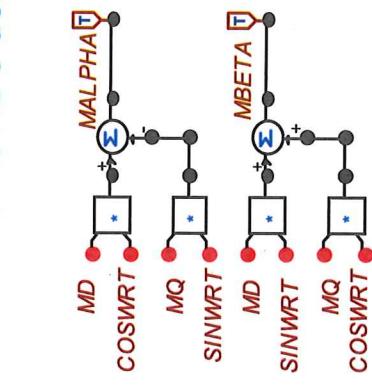


I_{DQ} measured \uparrow I_{DQ} ref measured \uparrow I_{DQ} ref from trans form



L35 10/1/14

Convert MD and MQ alpha-beta
and then to ABC domain



Inverse transformations

4.70

equation 4.47

