

ECE 420 Homework#3

1. Consider the balanced three-phase system shown in Figure 1.  $V_{AN} = 132.79\angle 0^\circ$  kV,  $V_{BN} = 132.79\angle -120^\circ$  kV,  $V_{CN} = 132.79\angle +120^\circ$  kV. Transmission line impedance of **each phase** is  $Z_{line} = j3.0 \Omega$ . The load is Y connected and the load impedance of **each phase** is  $Z_{load} = 80 + j60 \Omega$ .

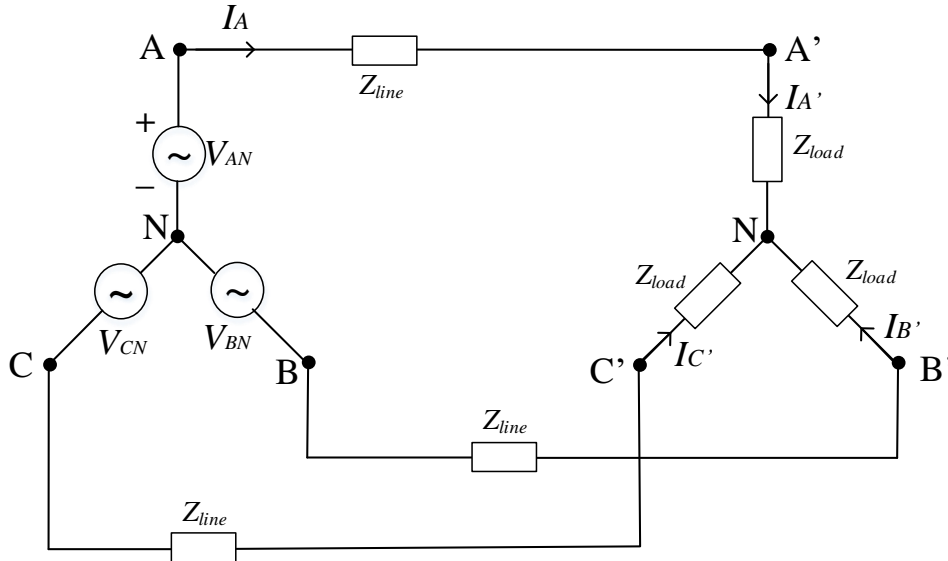


Figure 1

- (a) (1 points) Determine voltage  $V_{AB}$  and currents  $I_A$ ,  $I_A'$ ,  $I_B'$ ,  $I_C'$ .
- (b) (1 points) Determine voltages  $V_{A'N}$ ,  $V_{B'N}$ ,  $V_{C'N}$ , and  $V_{A'B'}$ .
- (c) (1 points) Determine the complex power consumed by phase A load ( $S_{loadA}$ ), phase B load ( $S_{loadB}$ ), and phase C load ( $S_{loadC}$ ). Determine the total complex power consumed by the three phases of load ( $S_{3\phi}$ ).
2. For the system as shown in Figure 1,  $V_{AN} = 132.79\angle 50^\circ$  kV,  $V_{BN} = 132.79\angle -70^\circ$  kV,  $V_{CN} = 132.79\angle -190^\circ$  kV. Transmission line impedance of **each phase** is  $Z_{line} = j3.0 \Omega$ . The load is Y connected and the load impedance of **each phase** is  $Z_{load} = 80 + j60 \Omega$ .
- (a) (2 points) Determine  $V_{AB}$ ,  $V_{A'N}$ ,  $V_{A'B'}$ ,  $I_A'$ ,  $S_{loadA}$ ,  $S_{loadB}$ ,  $S_{loadC}$ , and  $S_{3\phi}$
- (b) (1 points) Compare the results of  $V_{AB}$ ,  $V_{A'N}$ ,  $V_{A'B'}$ ,  $I_A'$ ,  $S_{loadA}$ ,  $S_{loadB}$ ,  $S_{loadC}$ , and  $S_{3\phi}$  to the values obtained in problem 1, what values have changed? What values stay the same?

3. Consider the balanced three-phase system shown in Figure 1.  $V_{AN,pu} = 1.0\angle 0^\circ$  pu,  $V_{BN,pu} = 1.0\angle -120^\circ$  pu,  $V_{CN,pu} = 1.0\angle +120^\circ$  pu. Transmission line impedance of **each phase** is  $Z_{line,pu} = (j3.0 \Omega)/Z_{base}$ . The load is Y connected and the load impedance of **each phase** is  $Z_{load,pu} = (80+j60 \Omega)/Z_{base}$

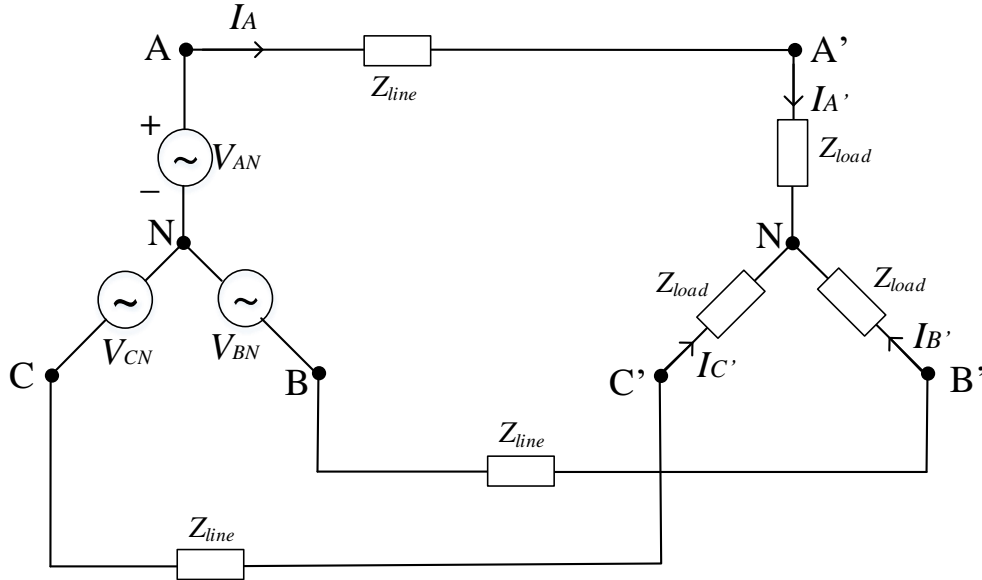


Figure 2

- (a) (1 points) Use  $V_{ll,b} = 230$  kV,  $V_{LN,b} = 230/\sqrt{3}$  kV = 132.79 kV,  $S_{3\phi,b} = 100$  MVA,  $S_{\phi,b} = 33.33$  MVA,  $I_{base} = \frac{S_{\phi,b}}{V_{LN,b}} = \frac{S_{3\phi,b}}{\sqrt{3}V_{ll,b}}$ ,  $Z_{base} = \frac{(V_{LN,b})}{(\frac{S_{\phi,b}}{V_{LN,b}})} = \frac{(V_{ll,b}/\sqrt{3})}{(\frac{S_{3\phi,b}}{\sqrt{3}V_{ll,b}})} = \frac{V_{ll,b}^2}{S_{3\phi,b}}$  to

determine  $I_{base}$ ,  $Z_{base}$ ,  $Z_{line,pu}$ , and  $Z_{load,pu}$ . (Note that  $I_{base}$  should have unit A,  $Z_{base}$  should have unit  $\Omega$ .  $Z_{line}$  and  $Z_{load}$  should have no unit because the  $\Omega$  on the numerator and denominator are canceled out.)

- (b) (2 points) Determine  $V_{A'N,pu}$ ,  $I_{A',pu}$ , and  $S_{loadA,pu}$

- (c) (1 points) Multiply line-to-neutral voltage  $V_{A'N,pu}$  by  $V_{LN,b}$ , multiply  $I_{A',pu}$  by  $I_{base}$ , and multiply  $S_{loadA,pu}$  by  $S_{\phi,b}$ , to obtain their actual values. Compare the results with problem 1.