

Example with sample and hold

Plot the output versus time for an analog-to-digital (A/D) converter applied to the waveform for $x(t)$. Assume the following

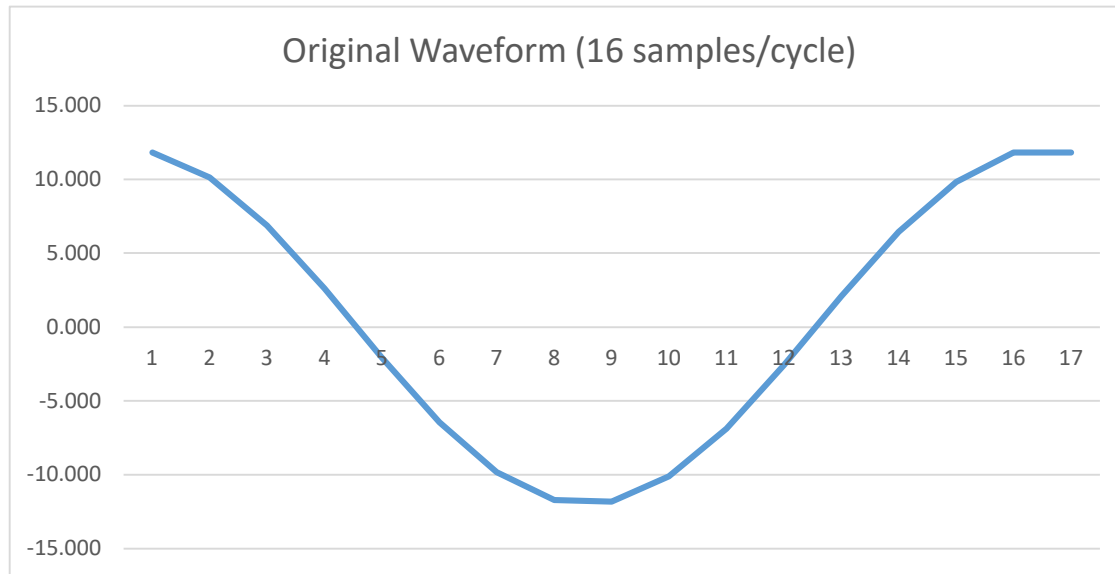
a) you are sampling at 8 samples per 10 Hz cycle

b) You have a 4 bit A/D where the most significant bit is a sign bit (MSB). Use the signed magnitude to represent the negative number (0 is positive and 1 is negative). In your plot, simply put the negative number below zero. Assume full scale for you're A/D converter is -15 to + 15.

Frequency (Hz)	Period	t_sample (8) sec	π	amplitude (A)	ϕ (deg)
10	0.1	0.0125	3.142	12	10
					in Radians
					0.175

Waveform: $x(t) = 12 \cdot \cos(2 \cdot \pi \cdot 10 \text{ Hz} \cdot t + \phi)$
 Xrms= $12/\text{SQRT}(2)$ 8.49

Original Waveform	Time	Value
	0	11.818
	1	10.121
	2	6.883
	3	2.597
	4	-2.084
	5	-6.448
	6	-9.830
	7	-11.716
	8	-11.818
	9	-10.121
	10	-6.883
	11	-2.597
	12	2.084
	13	6.448
	14	9.830
	15	11.818
	16	11.818



* Analog scale: Maximum positive and negative value has magnitude of 15

* We have $2n$ combinations of the magnitude bits, where $n=2$ (

* in this case two of which are 0, that step up as:

Num Magnitude Bits (n): 2

Current change per amplitude per bit

$$15A / (2^n - 1) = 5$$

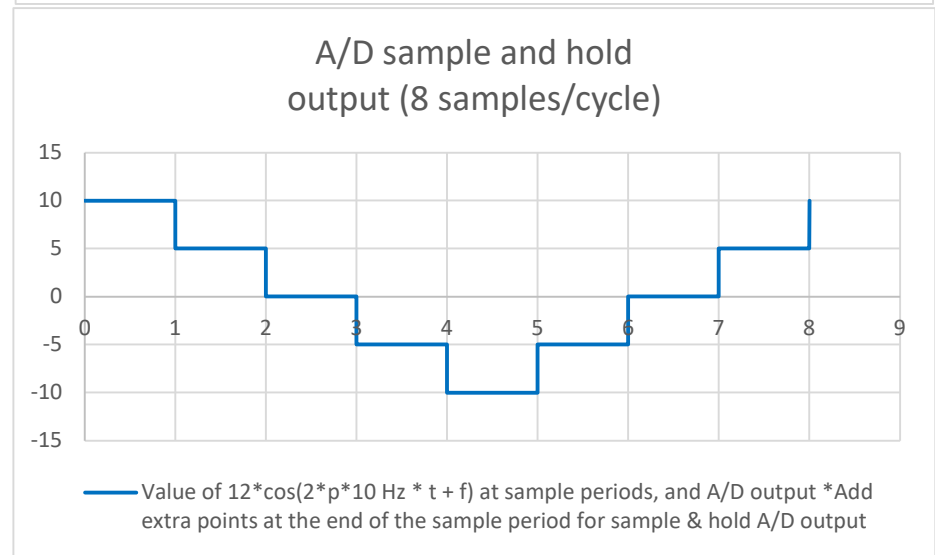
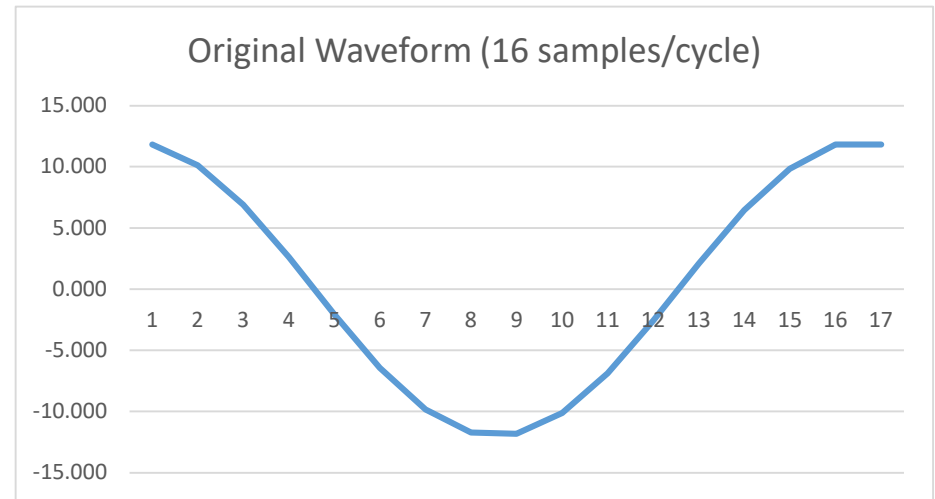
Mapping digital bit combinations to analog values (MSB is

0,0,0	0
0,0,1	5
0,1,0	10
0,1,1	15
1,0,0	-0
1,0,1	-5
1,1,0	-10
1,1,1	-15

Value of $12 \cdot \cos(2 \cdot \pi \cdot 10 \text{ Hz} \cdot t + \phi)$ at sample periods, and A/D output

*Add extra points at the end of the sample period for sample & hold

Sample number	Time	Value	A/D output
0	0.000	11.818	10
0.99999	0.012	11.818	10
1	0.013	6.883	5
1.99999	0.025	6.883	5
2	0.025	-2.084	0
2.99999	0.037	-2.084	0
3	0.038	-9.830	-5
3.99999	0.050	-9.830	-5
4	0.050	-11.818	-10
4.99999	0.062	-11.818	-10
5	0.063	-6.883	-5
5.99999	0.075	-6.883	-5
6	0.075	2.084	0
6.99999	0.087	2.084	0
7	0.088	9.830	5
7.99999	0.100	9.830	5
8	0.100	11.818	10



Now calculate RMS current

* Implement the following formula in pieces

* Remember that integral is a sum of areas

$$X_{RMS} = \sqrt{\frac{1}{T} \cdot \int_0^T (i(t)^2) dt}$$

Sample num	Current from A/D	Integrals by parts (t.sample * v^2)
0	10	1.25
1	5	0.3125
2	0	0
3	-5	0.3125
4	-10	1.25
5	-5	0.3125
6	0	0
7	5	0.3125
Sum		3.75

Sum/T 37.5 Where T is the period

Take SQRT **X_RMS_a/d 6.124**

Compare to original waveform

Xrms= 12/SQRT(2) 8.49 Significant difference due to quantization