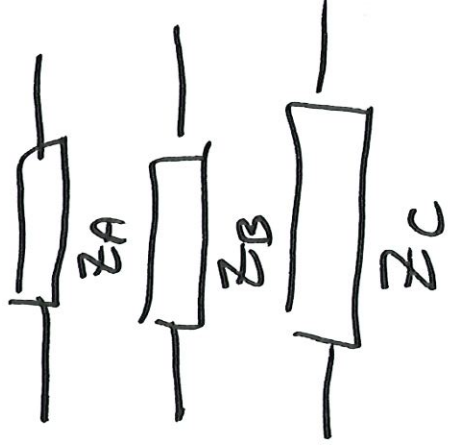
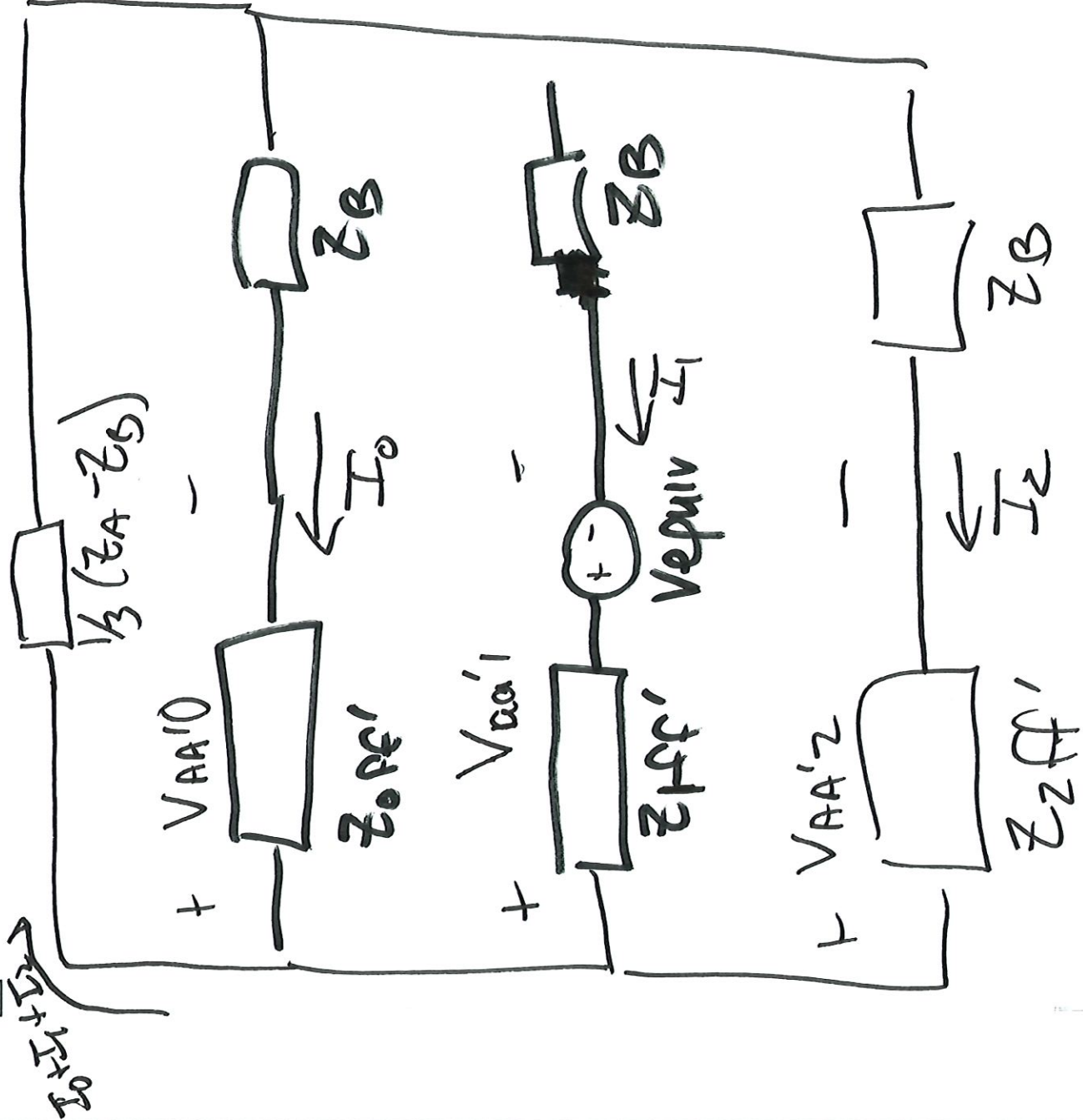


ECE 523
Symmetrical Components

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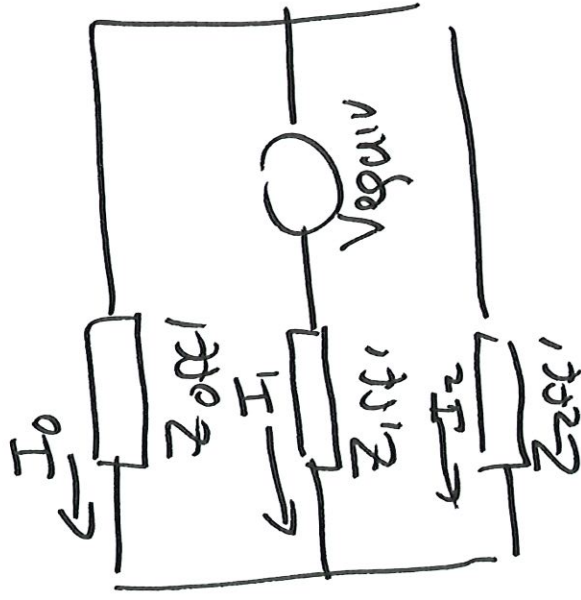
$Z_B = Z_C$
 $Z_A \neq Z_B = Z_C$

~~Example~~ phase A CB is open
(on fuse blown)

$$Z_A = \infty$$

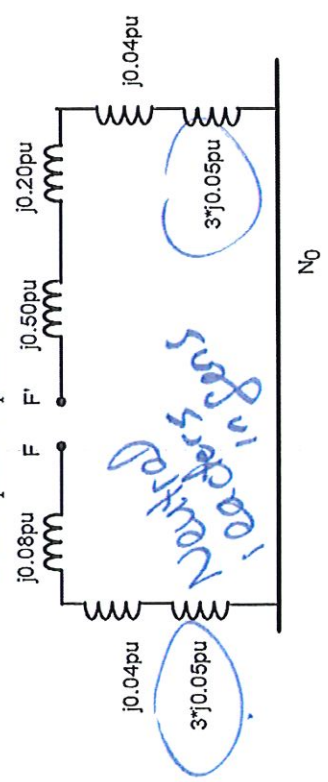
$$Z_B = Z_C = 0 \text{ (closed CB)}$$

$$\frac{1}{3}(Z_A - Z_B) = \infty$$



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- Zero sequence equivalent:



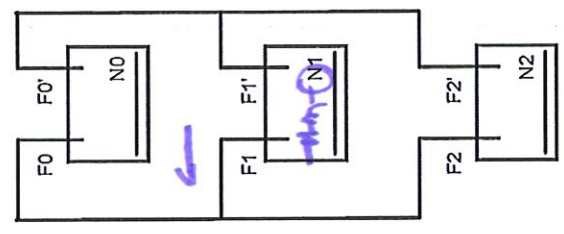
Find total impedance counterclockwise around loop from F to F'

$$Z_{0total} := j \cdot (2 \cdot X_{0Mach} + 2 \cdot X_{L0} + X_{L0} + 2 \cdot 3 \cdot X_{nMach})$$

$$Z_{0total} = 1.04j \cdot pu$$

$$Z_{OFF} := Z_{0total}$$

Now solve for the single phase open circuit currents and voltages:



$$I_1 := \frac{V_{equiv}}{Z_{1FF'} + \left(\frac{1}{Z_{2FF'}} + \frac{1}{Z_{OFF'}} \right)^{-1}}$$

$$I_2 := -I_1 \cdot \left(\frac{Z_{OFF'}}{Z_{2FF'} + Z_{OFF'}} \right)$$

$$I_0 := -I_1 \cdot \left(\frac{Z_{2FF'}}{Z_{2FF'} + Z_{OFF'}} \right)$$

$$I_1 = (0.43 - 0.26j) \cdot pu$$

$$|I_1| = 0.5 \cdot pu \quad \arg(I_1) = -31.79 \cdot deg$$

$$I_2 = (-0.25 + 0.16j) \cdot pu$$

$$|I_2| = 0.3 \cdot pu \quad \arg(I_2) = 148.21 \cdot deg$$

$$I_0 = (-0.17 + 0.11j) \cdot pu$$

$$|I_0| = 0.2 \cdot pu \quad \arg(I_0) = 148.21 \cdot deg$$

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$$I_{abc} := A_{012} \cdot \begin{pmatrix} I_0 \\ I_1 \\ I_2 \end{pmatrix} \Rightarrow \vec{I}_{abc} = \begin{pmatrix} 0 \\ 0.76 \cdot \text{pu} \\ 0.76 \end{pmatrix}$$

$\arg(I_{abc_1}) = -145.57 \cdot \text{deg}$
 $\arg(I_{abc_2}) = 82 \cdot \text{deg}$

0.8 pu fault

Using the right hand the sequence equivalent circuits:

$$V_{3\text{new}1} := E_2 + I_1 \cdot j \cdot (X_{1\text{Mach}} + X_T) \quad |V_{3\text{new}1}| = 0.96 \cdot \text{pu} \quad \arg(V_{3\text{new}1}) = -4.25 \cdot \text{deg}$$

$$V_{3\text{new}2} := 0 + I_2 \cdot j \cdot (X_{2\text{Mach}} + X_T) \quad |V_{3\text{new}2}| = 0.08 \cdot \text{pu} \quad \arg(V_{3\text{new}2}) = -121.79 \cdot \text{deg}$$

$$V_{3\text{new}0} := 0 + I_0 \cdot j \cdot (X_{0\text{Mach}} + X_T + 3 \cdot X_{n\text{Mach}}) \quad |V_{3\text{new}0}| = 0.05 \cdot \text{pu} \quad \arg(V_{3\text{new}0}) = -121.79 \cdot \text{deg}$$

$$V_{3\text{new}ABC} := A_{012} \cdot \begin{pmatrix} V_{3\text{new}0} \\ V_{3\text{new}1} \\ V_{3\text{new}2} \end{pmatrix} \Rightarrow \vec{V}_{3\text{new}ABC} = \begin{pmatrix} 0.903 \\ 0.971 \cdot \text{pu} \\ 1.014 \end{pmatrix} \Rightarrow \arg(V_{3\text{new}ABC}) = \begin{pmatrix} -12.06 \\ -119.95 \cdot \text{deg} \\ 118.58 \end{pmatrix}$$

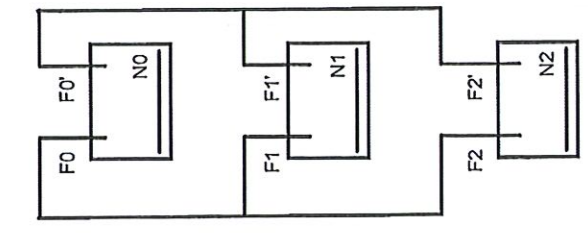
$$\Delta V_{ABC} := 1.0 \cdot \begin{pmatrix} 1 \\ a^2 \\ a \end{pmatrix} - V_{3\text{new}ABC}$$

$$|\Delta V_{ABC}| = \begin{pmatrix} 0.22 \\ 0.03 \\ 0.03 \end{pmatrix}$$

$$\arg(\Delta V_{ABC}) = \begin{pmatrix} 58.21 \\ -121.79 \cdot \text{deg} \\ -121.79 \end{pmatrix}$$

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Phase A open analysis:



Equivalent voltage source for phase A open analysis:

$$V_{sc} := V_S - V_R \quad V_{sc} = (0.06 - 0.34i) \cdot pu$$

Norton Equivalent Current:

$$I_{se} := \frac{V_{sc}}{Z_{1R} + Z_{1S}} \quad I_{se} = (-2.28 - 0.4i) \cdot pu$$

Equivalent Parallel Impedance:

$$Z_{eq} := \left(\frac{1}{Z_{1L2}} + \frac{1}{Z_{1S} + Z_{1R}} \right)^{-1} \quad Z_{eq} = 0.11i \cdot pu$$

Convert back to Thevenin Equivalent Voltage

$$V_f := Z_{eq} \cdot I_{se} \quad |V_f| = 0.25 \cdot pu \quad \arg(V_f) = -80 \cdot deg$$

two part theorem
two voltage

Positive sequence current in line 1:

$$I_{1L1_open} := \frac{V_f}{Z_{1equiv} + \left(\frac{1}{Z_{2equiv}} + \frac{1}{Z_{0equiv}} \right)^{-1}} \quad |I_{1L1_open}| = 0.34 \cdot pu$$

$$\arg(I_{1L1_open}) = -170 \cdot deg$$

Negative sequence current in line 1 (current divider on the line 1 current)

$$I_{2L1_open} := -I_{1L1_open} \cdot \frac{Z_{0equiv}}{Z_{2equiv} + Z_{0equiv}} \quad |I_{2L1_open}| = 0.27 \cdot pu$$

$$\arg(I_{2L1_open}) = 10 \cdot deg$$

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Using the sequence diagrams above calculate the positive-, negative-, and zero-sequence currents on Line 2 with $V_R = 1\text{ pu}$ @ 20 degrees.

$$V_S := 1\text{ pu} \cdot e^{j \cdot 0\text{deg}} \quad V_R := 1\text{ pu} \cdot e^{j \cdot 20\text{deg}}$$

Total prefault current:

$$I_{\text{sourceprefault}} := \frac{V_S - V_R}{Z_{1S} + Z_{1R} + \left(\frac{1}{Z_{1L1}} + \frac{1}{Z_{1L2}} \right)^{-1}}$$

$$|I_{\text{sourceprefault}}| = 1.08 \cdot \text{pu} \quad \arg(I_{\text{sourceprefault}}) = -170 \cdot \text{deg}$$

Current dividers to find the current in lines 1 and 2:

$$I_{L1_prefault} := I_{\text{sourceprefault}} \cdot \left(\frac{Z_{1L2}}{Z_{1L1} + Z_{1L2}} \right)$$

$$|I_{L1_prefault}| = 0.62 \cdot \text{pu} \quad \arg(I_{L1_prefault}) = -170 \cdot \text{deg}$$

$$I_{L2_prefault} := I_{\text{sourceprefault}} \cdot \left(\frac{Z_{1L1}}{Z_{1L1} + Z_{1L2}} \right)$$

$$|I_{L2_prefault}| = 0.46 \cdot \text{pu} \quad \arg(I_{L2_prefault}) = -170 \cdot \text{deg}$$

$$I_{\text{ABCL1_prefault}} := I_{L1_prefault} \cdot \begin{pmatrix} 1 \\ 2 \\ a \\ a \end{pmatrix}$$

$$|I_{\text{ABCL1_prefault}}| = \begin{pmatrix} 0.62 \\ 0.62 \cdot \text{pu} \\ 0.62 \end{pmatrix}$$

$$\arg(I_{\text{ABCL1_prefault}}) = \begin{pmatrix} -170 \\ 70 \\ -50 \end{pmatrix} \cdot \text{deg}$$

$$I_{\text{ABCL2_prefault}} := I_{L2_prefault} \cdot \begin{pmatrix} 1 \\ 2 \\ a \\ a \end{pmatrix}$$

$$|I_{\text{ABCL2_prefault}}| = \begin{pmatrix} 0.46 \\ 0.46 \cdot \text{pu} \\ 0.46 \end{pmatrix}$$

$$\arg(I_{\text{ABCL2_prefault}}) = \begin{pmatrix} -170 \\ 70 \\ -50 \end{pmatrix} \cdot \text{deg}$$

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Zero sequence current in line 1 (current divider on the line 1 current)

$$I_{0L1_open} := -I_{1L1_open} \cdot \frac{Z_{2equiv}}{Z_{2equiv} + Z_{0equiv}} \quad |I_{0L1_open}| = 0.07 \cdot pu \quad \arg(I_{0L1_open}) = 10 \cdot deg$$

$$I_{ABC_Line1} := A_{012} \cdot \begin{pmatrix} I_{0L1_open} \\ I_{1L1_open} \\ I_{2L1_open} \end{pmatrix}$$

$$\vec{I}_{ABC_Line1} = \begin{pmatrix} 0 \\ 0.545 \cdot pu \\ 0.545 \end{pmatrix}$$

$$\arg(I_{ABC_Line1}) = 88.74 \cdot deg$$

$$\arg(I_{ABC_Line2}) = -68.74 \cdot deg$$

Note that the magnitude on phase A is 0 and a little smaller on the unfaulted phases. There is also a phase shift compared to prefault

Now to find the line 2 current, we need to do another current divider on each of the sequence currents from line 1, since the sequence currents could either pass through the sources or line to return to line 1.

Positive sequence load current in line two ignoring open line

$$I_{LineA2} := \frac{V_S - V_R}{Z_{1S} + Z_{1L2} + Z_{1R}}$$

$$|I_{LineA2}| = 0.631$$

$$\arg(I_{LineA2}) = -170 \cdot deg$$

→ treating line 1 as open

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add current to I_{1L2}

$$I_{1L2} := -I_{1L1_open} \cdot \left(\frac{Z_{1S} + Z_{1R}}{Z_{1S} + Z_{1R} + Z_{1L2}} \right) + I_{LineA2}$$

$$\arg(I_{1L2}) = -170 \cdot \text{deg}$$

$$|I_{1L2}| = 0.54 \cdot \text{pu}$$

$$I_{2L2} := -I_{2L1_open} \cdot \left(\frac{Z_{1S} + Z_{1R}}{Z_{1S} + Z_{1R} + Z_{1L2}} \right)$$

$$\arg(I_{2L2}) = -170 \cdot \text{deg}$$

$$|I_{2L2}| = 0.07 \cdot \text{pu}$$

$$I_{0L2} := -I_{0L1_open} \cdot \left(\frac{Z_{0S} + Z_{0R}}{Z_{0S} + Z_{0R} + Z_{0L2}} \right)$$

$$\arg(I_{0L2}) = -170 \cdot \text{deg}$$

$$|I_{0L2}| = 0.02 \cdot \text{pu}$$

$$I_{ABC_Line2} := A_{012} \cdot \begin{pmatrix} I_{0L2} \\ I_{1L2} \\ I_{2L2} \end{pmatrix}$$

$$|I_{ABC_Line2}| = \begin{pmatrix} 0.63 \\ 0.494 \\ 0.494 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_Line2}) = \begin{pmatrix} -170 \\ 64.29 \\ -44.29 \end{pmatrix} \cdot \text{deg}$$

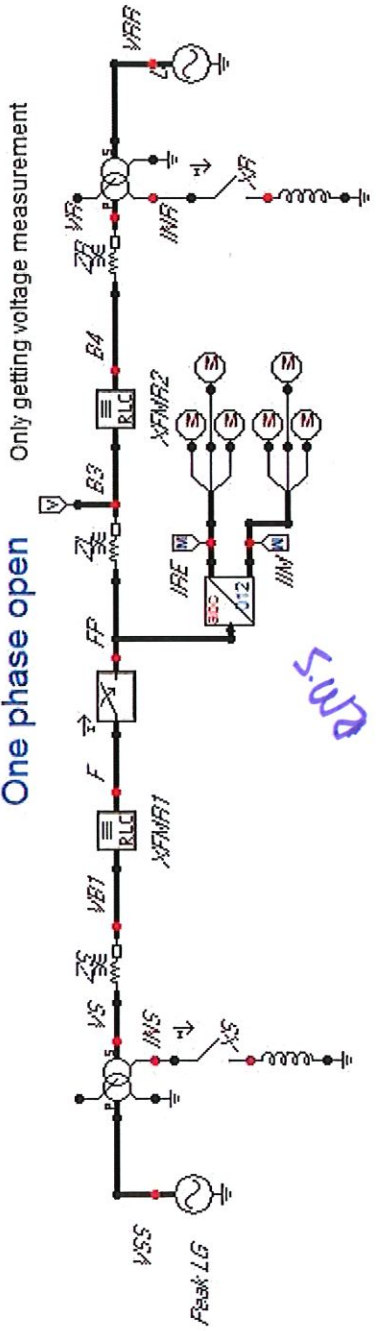
- See course web page for ATP, PSCAD/EMTDC, and EMT-P-RV examples



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ATP simulation results:

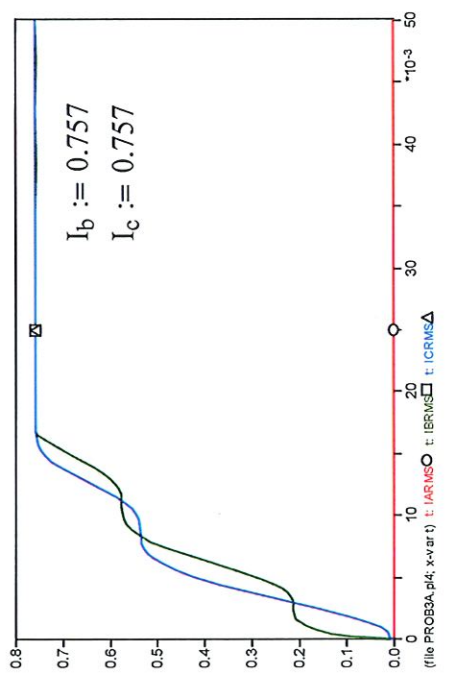
One phase open



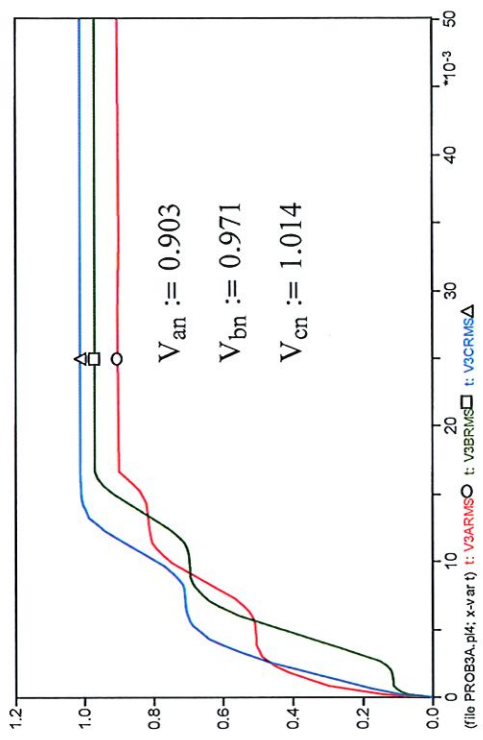
0.5 W

Only getting voltage measurement

Currents

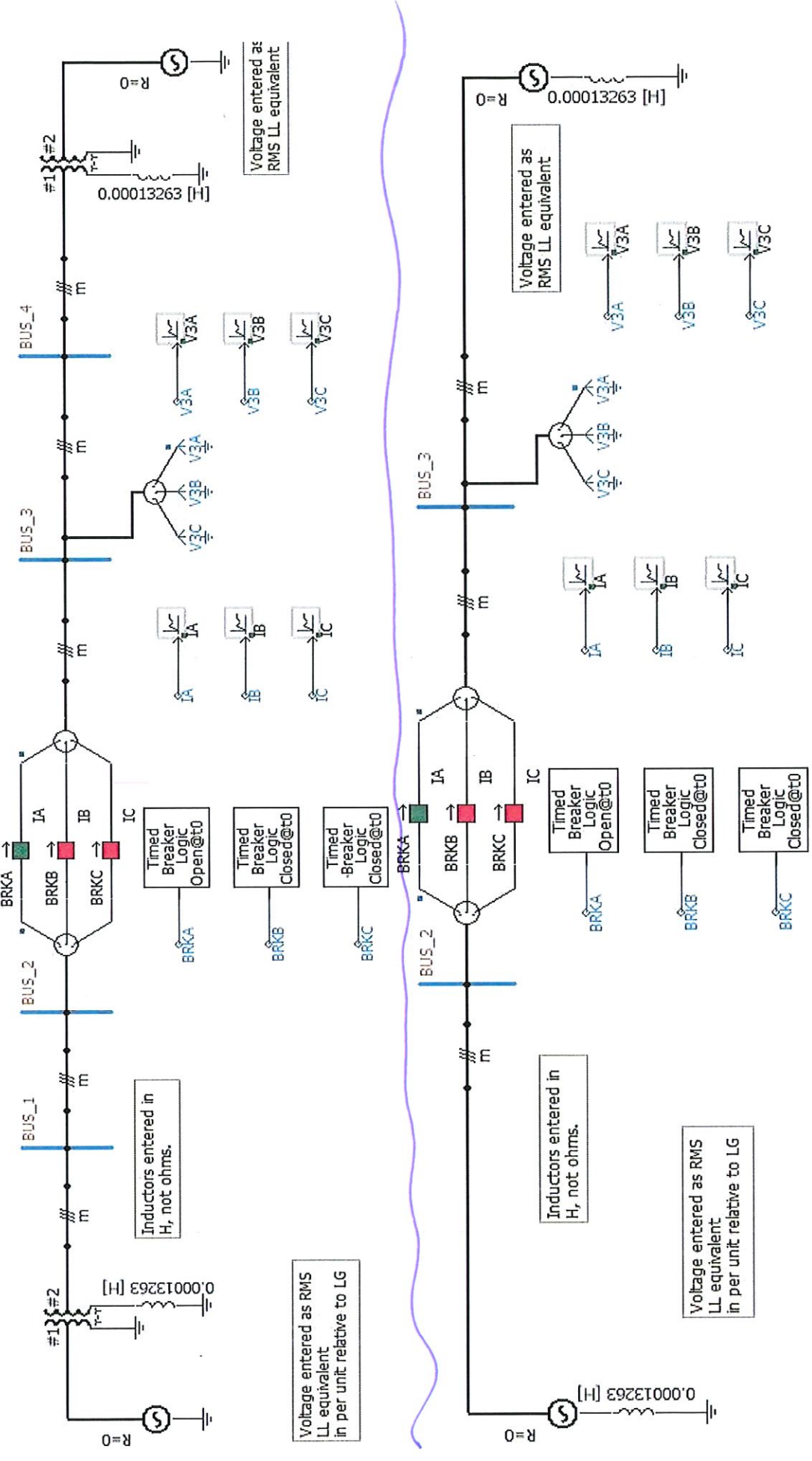


Voltages



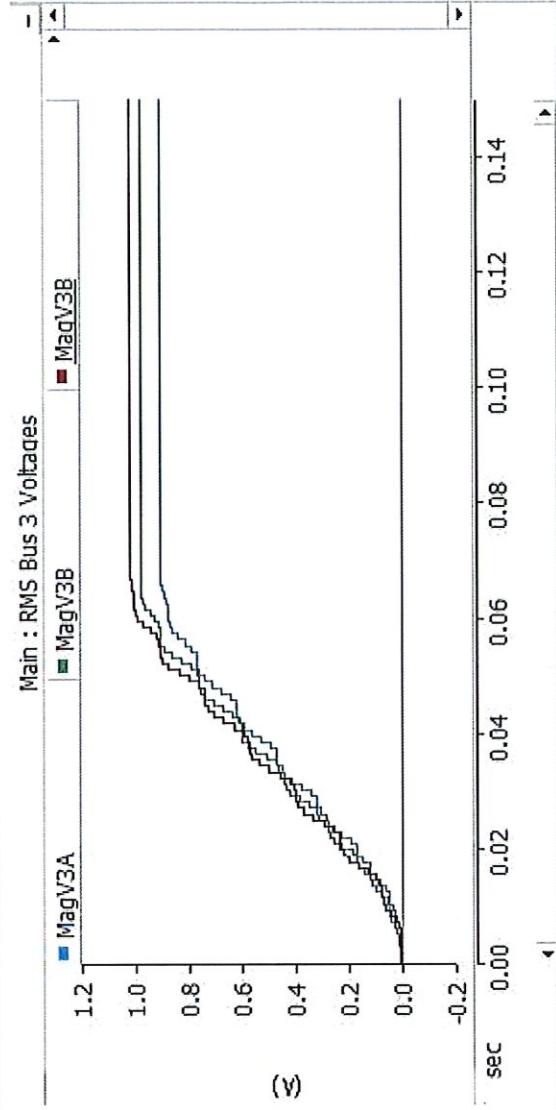
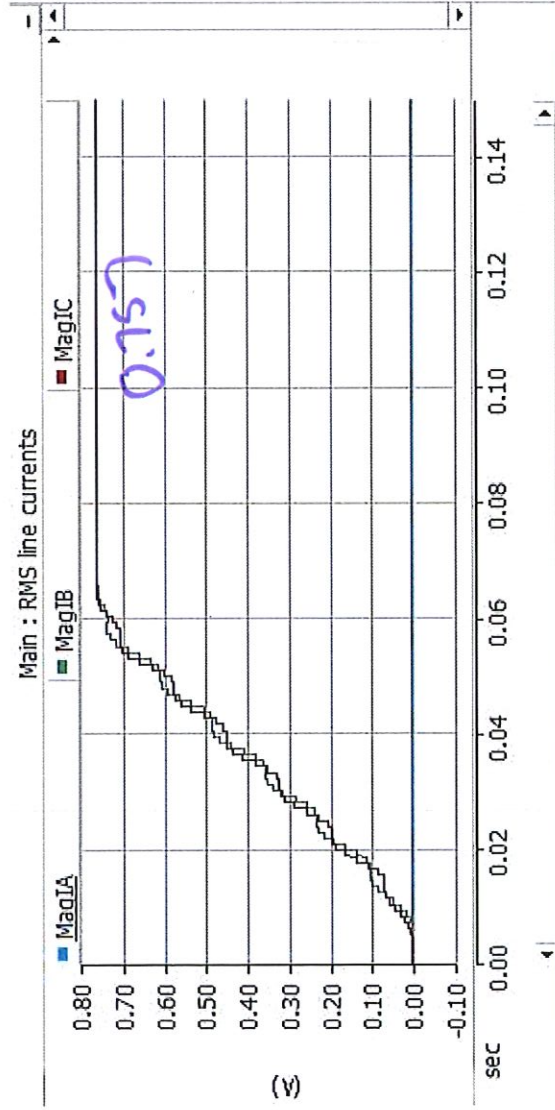
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PSCAD/EMTDC implementation



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General Series Fault Case

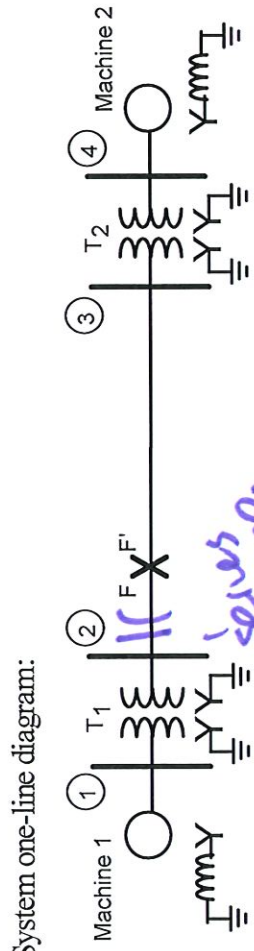
pu := 1 MVA := 1000kW

$$a := 1e^{j \cdot 120 \text{deg}}$$

$$A_{012} := \begin{pmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{pmatrix}$$

Suppose that a series compensator is added to the line at the Bus 2 end with each phase having a capacitive impedance of $-j0.1 \text{ pu}$. The capacitor on phase A is bypassed by a bypass breaker while phases B and C remain inserted. Calculate the currents from Bus 1 to Bus 2 and the voltage at Bus 3 (assuming the voltage is 1.0 pu before the condition occurs).

*closed on A
not on the others*



- System one-line diagram:

Machines 1 and 2: $S_{Mach} := 100 \text{MVA}$ $V_{machine} := 20 \text{kV}$
 $X_{dMach} := 20\%$ $X_{1Mach} := X_{dMach}$ $X_{2Mach} := X_{1Mach}$
 $X_{0Mach} := 4\%$ $X_{nMach} := 5\%$

Transformers T1 and T2: $S_{Tran} := 1000 \text{MVA}$ $V_{HV} := 345 \text{kV}$ $V_{LV} := 20 \text{kV}$ $X_T := 8\%$

Transmission Line $X_{L1} := 15\%$ $X_{L2} := X_{L1}$ $X_{L0} := 50\%$

$X_c := 0.1 \text{pu}$

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$$V_{B_{line}} := 345kV \quad V_{B_{mach}} := V_{B_{line}} \left(\frac{V_{LV}}{V_{HV}} \right) \quad V_{B_{mach}} = 20 \cdot kV$$

No change of base calculations are needed for this system.

Determine internal source voltages:

$$\text{mag}S_{pre} := 100MVA \quad pf_{pre} := 0.85 \text{ lagging} \quad \theta_{pre} := \text{acos}(pf_{pre}) \quad \theta_{pre} = 31.79 \cdot \text{deg}$$

$$S_{Base} := 100MVA$$

$$S_{pre} := \frac{\text{mag}S_{pre} \cdot j \cdot \theta_{pre}}{S_{Base}} \quad S_{pre} = (0.85 + 0.53i) \cdot pu \quad |S_{pre}| = 1 \cdot pu$$

Assume bus 3 voltage is 1.0 pu at and angle of 0 degrees.

$$V_3 := 1.0$$

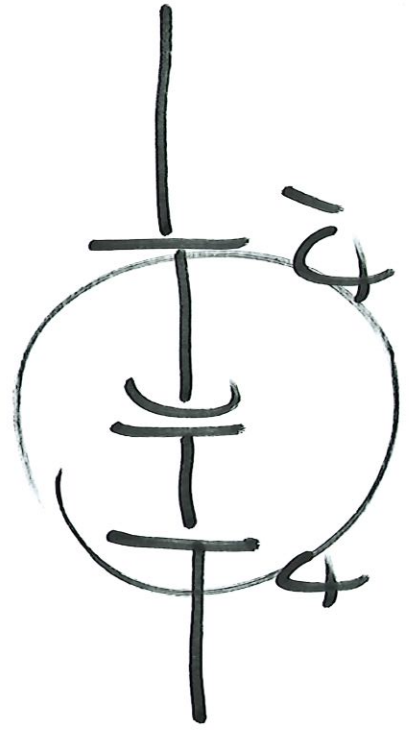
$$I_{load} := \left(\frac{S_{pre}}{V_3} \right) \quad I_{load} = 0.85 - 0.53i \quad |I_{load}| = 1 \cdot pu \quad \arg(I_{load}) = -31.79 \cdot \text{deg}$$

Internal voltage on the motor (since we don't know steady-state synchronous reactance, use X1):

$$E_2 := V_3 - I_{load} \cdot j(X_T + X_{IMach}) \quad |E_2| = 0.89 \quad \phi_2 := \arg(E_2) \quad \phi_2 = -15.6 \cdot \text{deg}$$

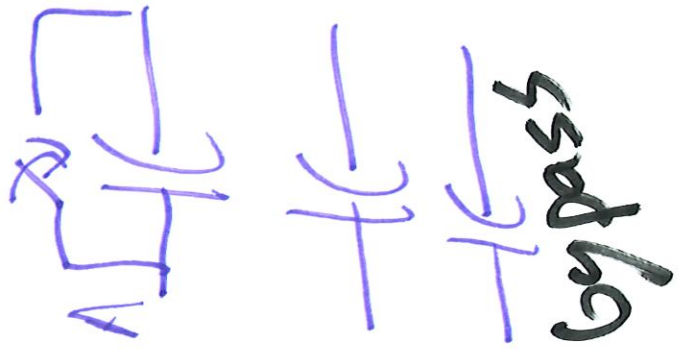
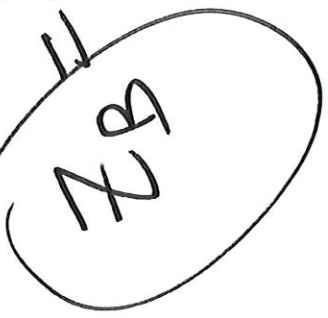
Generator internal voltage:

$$E_1 := V_3 + I_{load} \cdot (j \cdot X_{L1} - j \cdot X_c + j \cdot X_T + j \cdot X_{IMach}) \quad |E_1| = 1.21 \cdot pu \quad \phi_1 := \arg(E_1) \quad \phi_1 = 13.44 \cdot \text{deg}$$

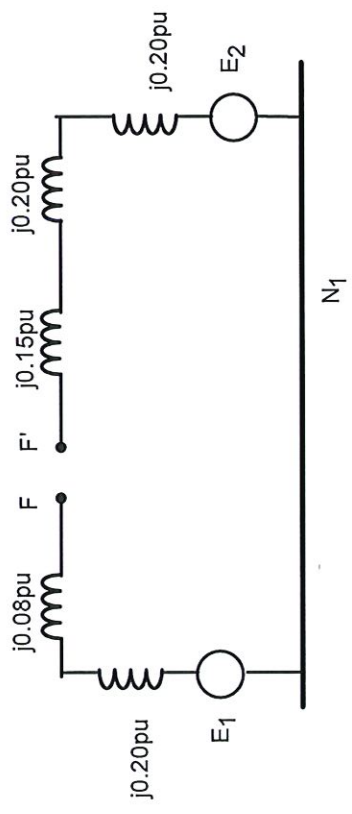


closed

$$Z_A = 0 \rightarrow X_C$$



- Positive sequence equivalent circuit (with phase open point indicated). Capacitor is not part of the equivalent. It is between F and F'



Find total impedance counterclockwise around loop from F to F'

$$Z_{1total} := j \cdot (X_{1Mach} + X_T + X_{L1} + X_T + X_{1Mach})$$

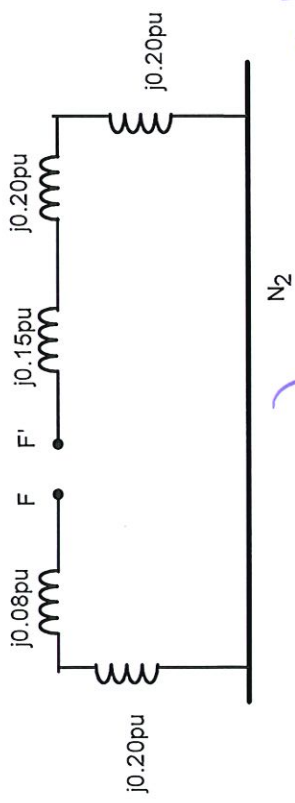
$$Z_{1total} = 0.71i \cdot pu$$

$$Z_{1FF'} := Z_{1total}$$

$$V_{equiv} := E_1 - E_2$$

result depends on E2 with sign since different capacitor

- Negative sequence equivalent circuit:



Find total impedance counterclockwise around loop from F to F'

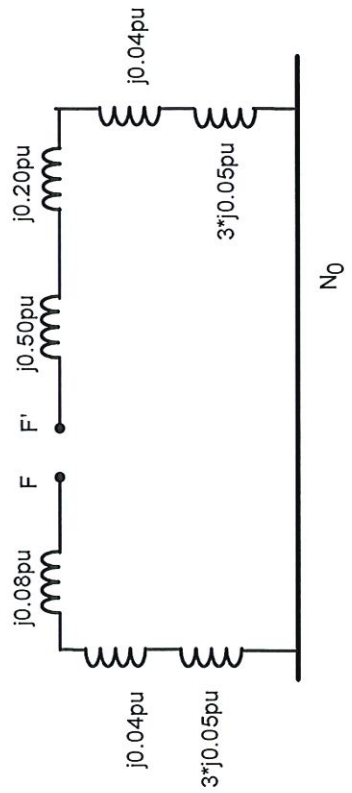
$$Z_{2total} := j \cdot (X_{2Mach} + X_T + X_{L2} + X_T + X_{2Mach})$$

$$Z_{2total} = 0.71i \cdot pu$$

$$Z_{2FF'} := Z_{2total}$$

unchanged cap since symmetrical

- Zero sequence equivalent:



Find total impedance counterclockwise around loop from F to F'

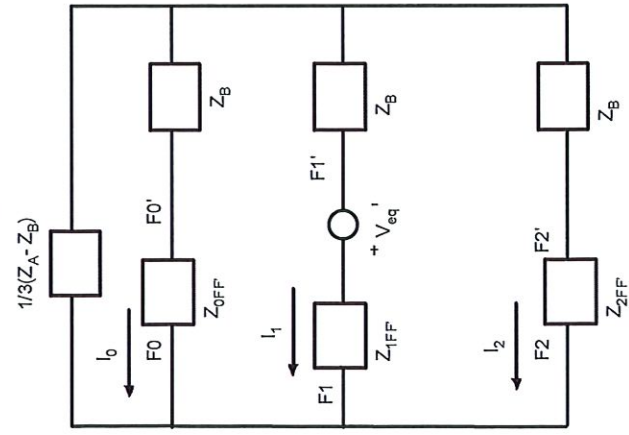
$$Z_{0total} := j \cdot (2 \cdot X_{0Mach} + 2 \cdot X_T + X_{L0} + 2 \cdot 3 \cdot X_{nMach})$$

$$Z_{0total} = 1.04i \cdot pu$$

$$Z_{0FF'} := Z_{0total}$$

Now solve for the single phase open circuit currents and voltages:

$$Z_A := 0pu \quad \text{shorted capacitor} \quad Z_B := -j \cdot X_c$$

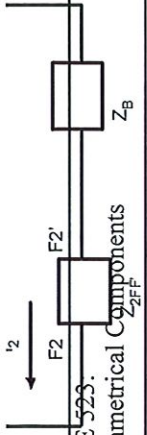


$$I_{1pp'_f} := \frac{V_{equiv}}{\left(\frac{1}{Z_{1FF'} + Z_B} \right) + \left[\frac{1}{(Z_{2FF'} + Z_B)} + \frac{1}{Z_{0FF'} + Z_B} \right] + \frac{1}{\frac{1}{3} \cdot (Z_A - Z_B)}}^{-1}$$

$$|I_{1pp'_f}| = 0.95 \cdot pu$$

$$\arg(I_{1pp'_f}) = -31.79 \cdot deg$$

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$Z_{0FF'} = \frac{1}{3}(Z_A + Z_B)$

$$I_{2pp_f} := -I_{1pp_f} \cdot \frac{\left[\frac{1}{Z_{0FF'} + Z_B} + \frac{1}{\frac{1}{3}(Z_A - Z_B)} \right]^{-1}}{(Z_{2FF'} + Z_B) + \left[\frac{1}{Z_{0FF'} + Z_B} + \frac{1}{\frac{1}{3}(Z_A - Z_B)} \right]^{-1}}$$

$$|I_{2pp_f}| = 0.05 \cdot \text{pu}$$

$$\arg(I_{2pp_f}) = 148.21 \cdot \text{deg}$$

$$I_{0pp_f} := -I_{1pp_f} \cdot \frac{\left[\frac{1}{Z_{2FF'} + Z_B} + \frac{1}{\frac{1}{3}(Z_A - Z_B)} \right]^{-1}}{(Z_{0FF'} + Z_B) + \left[\frac{1}{Z_{2FF'} + Z_B} + \frac{1}{\frac{1}{3}(Z_A - Z_B)} \right]^{-1}}$$

$$|I_{0pp_f}| = 0.03 \cdot \text{pu}$$

$$\arg(I_{0pp_f}) = 148.21 \cdot \text{deg}$$

- Although we don't use it, here is the current in the $\frac{1}{3}(Z_A - Z_B)$ branch

$$I_{a_b} := -I_{1pp_f} \cdot \frac{\left(\frac{1}{Z_{2FF'} + Z_B} + \frac{1}{Z_{0FF'} + Z_B} \right)^{-1}}{\left(\frac{1}{Z_{2FF'} + Z_B} + \frac{1}{Z_{0FF'} + Z_B} \right)^{-1} + \frac{1}{\frac{1}{3}(Z_A - Z_B)}}$$

$|I_{a_b}| = 0.87 \cdot \text{pu}$

$$\arg(I_{a_b}) = 148.21 \cdot \text{deg}$$

- Notice that is the largest component of the current.

$$I_{L2_ABC_f} := A_{012} \cdot \begin{pmatrix} I_{0pp_f} \\ I_{1pp_f} \\ I_{2pp_f} \end{pmatrix}$$

$$|I_{L2_ABC_f}| = \begin{pmatrix} 0.8736 \\ 0.9917 \\ 0.9917 \end{pmatrix} \cdot pu$$

$$\arg(I_{L2_ABC_f}) = \begin{pmatrix} -31.79 \\ -150.95 \\ 87.37 \end{pmatrix} \cdot deg$$

- Phase A has a smaller current than B and C, but not zero.
- Good match with ATP results

Using the right hand sequence equivalent circuits:

$$V_{3new1} := E_2 + I_{1pp_f} \cdot j \cdot (X_{1Mach} + X_T) \quad |V_{3new1}| = 0.99 \cdot pu \quad \arg(V_{3new1}) = -0.66 \cdot deg$$

$$V_{3new2} := 0 + I_{2pp_f} \cdot j \cdot (X_{2Mach} + X_T) \quad |V_{3new2}| = 0.01 \cdot pu \quad \arg(V_{3new2}) = -121.79 \cdot deg$$

$$V_{3new0} := 0 + I_{0pp_f} \cdot j \cdot (X_{0Mach} + X_T + 3 \cdot X_{nMach}) \quad |V_{3new0}| = 0.01 \cdot pu \quad \arg(V_{3new0}) = -121.79 \cdot deg$$

$$V_{3newABC} := A_{012} \cdot \begin{pmatrix} V_{3new0} \\ V_{3new1} \\ V_{3new2} \end{pmatrix} \quad |V_{3newABC}| = \begin{pmatrix} 0.98 \\ 1 \\ 1 \end{pmatrix} \cdot pu \quad \arg(V_{3newABC}) = \begin{pmatrix} -1.74 \\ -119.99 \\ 119.75 \end{pmatrix} \cdot deg$$

Equivalent circuit hold for
almost all series faults

— except for 2 phases open

$$Z_A = 0 \quad Z_B = Z_C = \infty$$



$$Z_B = Z_C = \infty$$



$$I_B = I_C = 0$$



$$V_{AA'} = Z_A \cdot I_A$$

In sequence domain

$$\begin{bmatrix} I_0 \\ I_1 \\ I_2 \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 1 & 1 & 1 \\ a & a^2 & 1 \\ a^2 & a & 1 \end{bmatrix} \begin{bmatrix} I_A \\ 0 \\ 0 \end{bmatrix}$$

$$I_0 = I_1 = I_2 = \frac{I_A}{3}$$

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Two phase open sequence connections

$$Z_B = Z_C = \infty$$

- Boundary conditions in ABC domain:

$$I_b = I_c = 0$$

$$V_{aa'} = Z_A \cdot I_a$$

- Transform boundary conditions to sequence domain

- Result for currents is similar to that for a SLG fault:

$$I_0 = I_1 = I_2 = \frac{I_a}{3}$$

- implies series connection of sequence blocks

- voltage equation mapped to sequence domain:

$$V_{AG} = V_{aa'0} + V_{aa'1} + V_{aa'2} = Z_A \cdot (I_0 + I_1 + I_2)$$

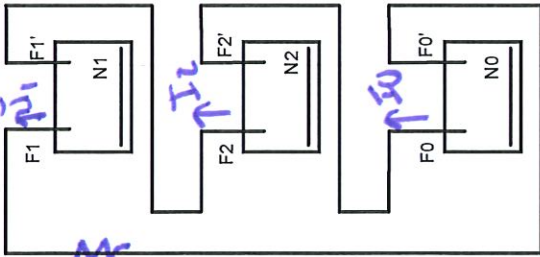
- Rearrange equation grouping terms:

$$(V_{aa'0} - Z_A \cdot I_0) + (V_{aa'1} - Z_A \cdot I_1) + (V_{aa'2} - Z_A \cdot I_2) = 0$$

$$V_{aa'0} + V_{aa'1} + V_{aa'2} = 3Z_A I_0$$

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Now solve the two phase open circuit below for the sequence currents:



$$I_1 := \frac{V_{\text{equiv}}}{Z_{1FF'} + Z_{2FF'} + Z_{0FF'}}$$

$$I_1 = (0.2 - 0.12i) \cdot \text{pu}$$

$$|I_1| = 0.23 \cdot \text{pu}$$

$$\arg(I_1) = -31.79 \cdot \text{deg}$$

$$I_2 := I_1 \quad I_0 := I_1$$

$$I_{\text{abc}} := A_{012} \cdot \begin{pmatrix} I_0 \\ I_1 \\ I_2 \end{pmatrix}$$

$$|I_{\text{abc}}| = \begin{pmatrix} 0.69 \\ 0 \\ 0 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{\text{abc}}) = \begin{pmatrix} -31.79 \\ 81.87 \\ 81.87 \end{pmatrix} \cdot \text{deg}$$

prefault was 0.8 at -31.79

$$V_{3\text{new}1} := E_2 + I_1 \cdot j \cdot (X_{1\text{Mach}} + X_T)$$

$$V_{3\text{new}1} = (0.92 - 0.14i) \cdot \text{pu}$$

$$V_{3\text{new}2} := 0 + I_2 \cdot j \cdot (X_{2\text{Mach}} + X_T)$$

$$V_{3\text{new}2} = (0.03 + 0.05i) \cdot \text{pu}$$

$$V_{3\text{new}0} := 0 + I_0 \cdot j \cdot (X_{0\text{Mach}} + X_T + 3 \cdot X_{\text{nmMach}})$$

$$V_{3\text{new}0} = (0.03 + 0.05i) \cdot \text{pu}$$

$$V_{3\text{newABC}} := A_{012} \cdot \begin{pmatrix} V_{3\text{new}0} \\ V_{3\text{new}1} \\ V_{3\text{new}2} \end{pmatrix}$$

$$|V_{3\text{newABC}}| = \begin{pmatrix} 0.983 \\ 0.905 \\ 0.901 \end{pmatrix} \cdot \text{pu}$$

$$\arg(V_{3\text{newABC}}) = \begin{pmatrix} -1.6 \\ -132.16 \\ 107.93 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{\text{ABC}} := 1.0 \cdot \begin{pmatrix} 1 \\ 2 \\ a \end{pmatrix} - V_{3\text{newABC}}$$

$$|\Delta V_{\text{ABC}}| = \begin{pmatrix} 0.03 \\ 0.22 \\ 0.22 \end{pmatrix} \cdot \text{pu}$$

$$\arg(\Delta V_{\text{ABC}}) = \begin{pmatrix} 58.21 \\ -61.27 \\ 177.7 \end{pmatrix} \cdot \text{deg}$$