

ECE 523
Symmetrical Components

Session 2

02/1
27

U I Off-Line Studies Versus Applying Measurements

ECE523

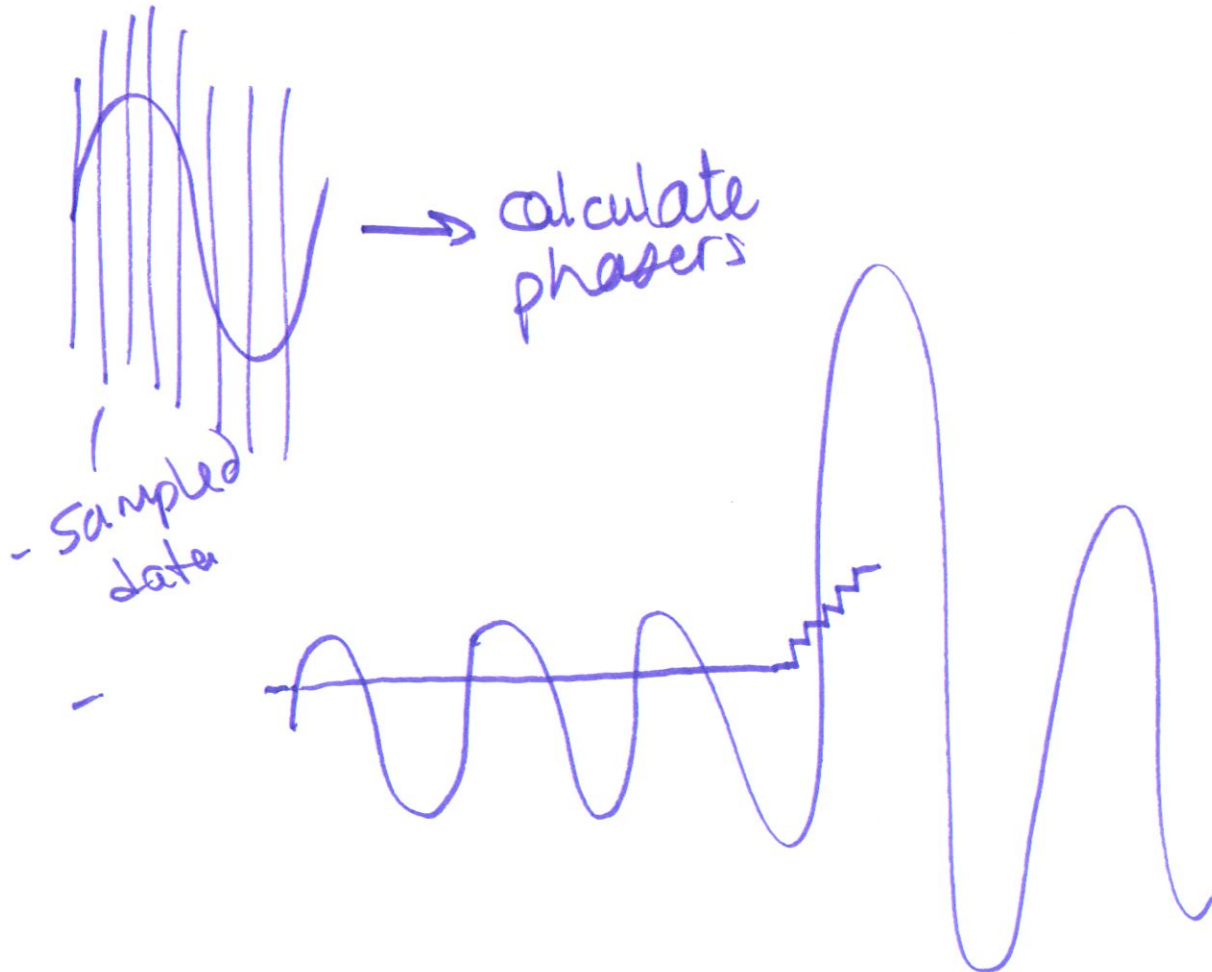
Lecture 1

- Normally applied using phasors
- Phasors have underlying assumption about frame of reference and frequency
- Measurement devices calculate RMS phasors and then transform
- Use of phasors only applies for quasi-steady-state analysis
- Some use of instantaneous terms, especially power electronic controls

Introduction

Fall 2023

5



Off-line applications of power & phase calculations

- planning studies $\left\{ \begin{array}{l} \text{power flow} \\ \text{stability} \\ \text{etc.} \end{array} \right.$
- fault studies
- equipment rating
- setting protective devices
- post event analysis

measurements based applications

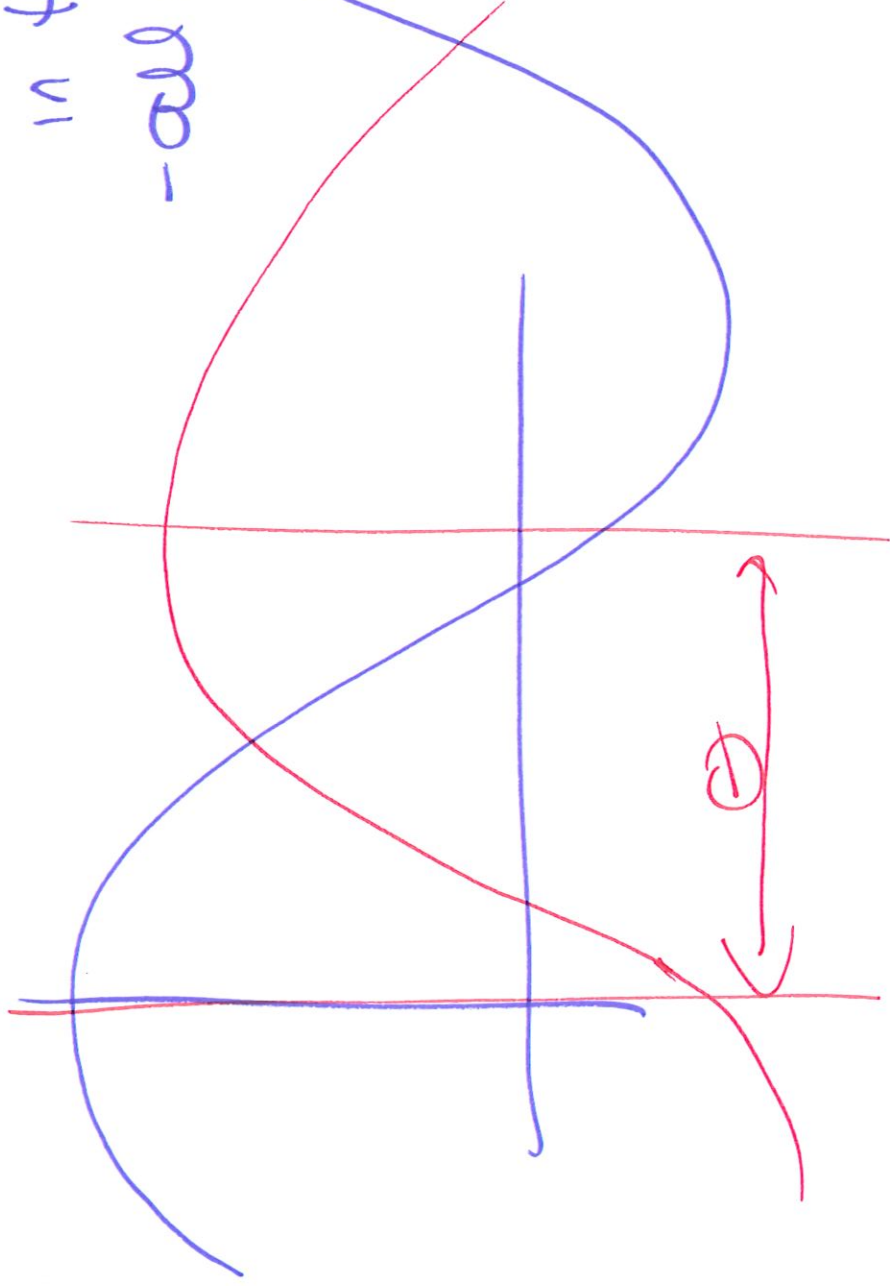
- Real time control & protection
- event recording
- fault locations

Phasors in measurements

- Angle reference?

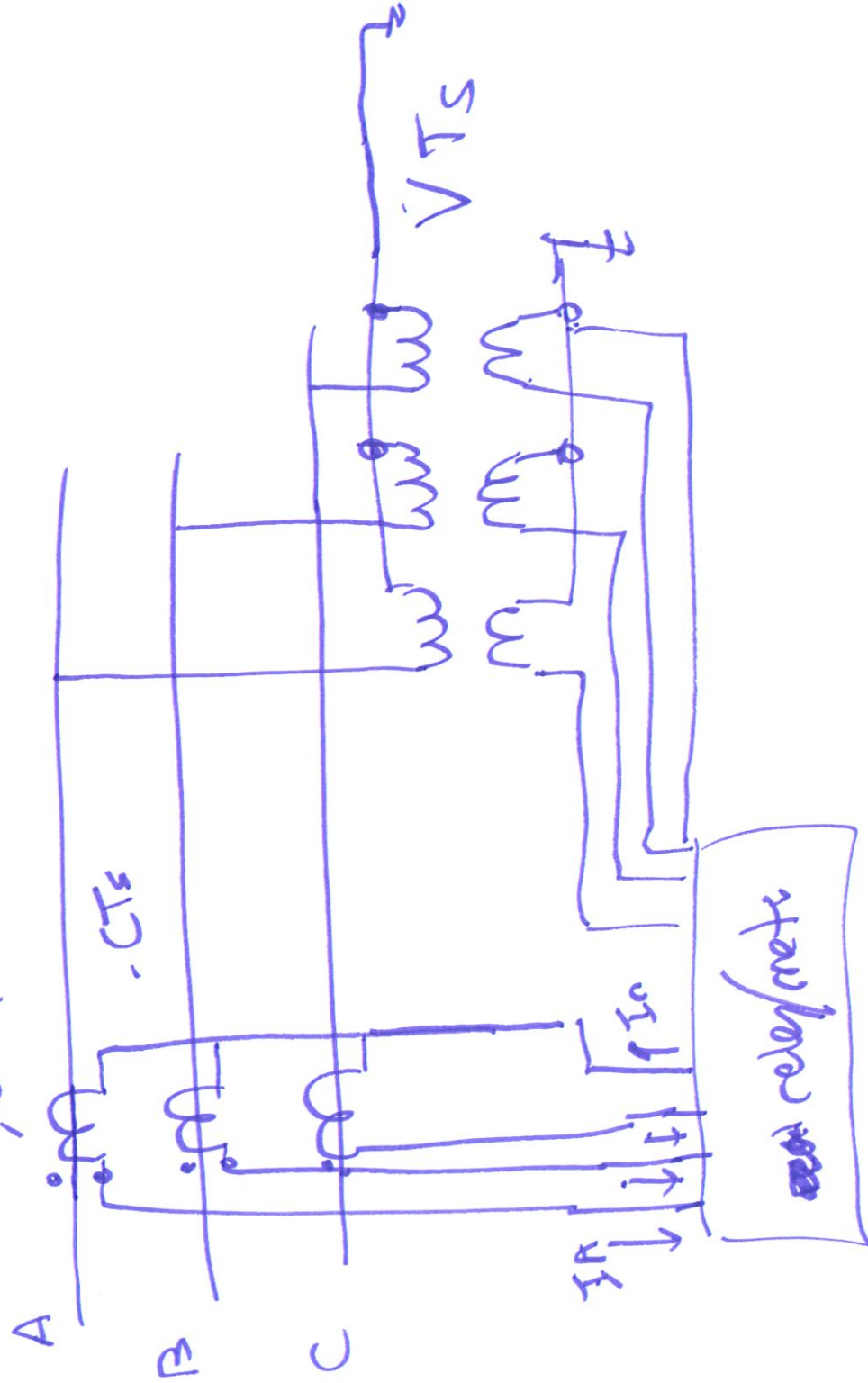
- voltage measurement
in the metering device

- all of phasors are
relative to
that voltage



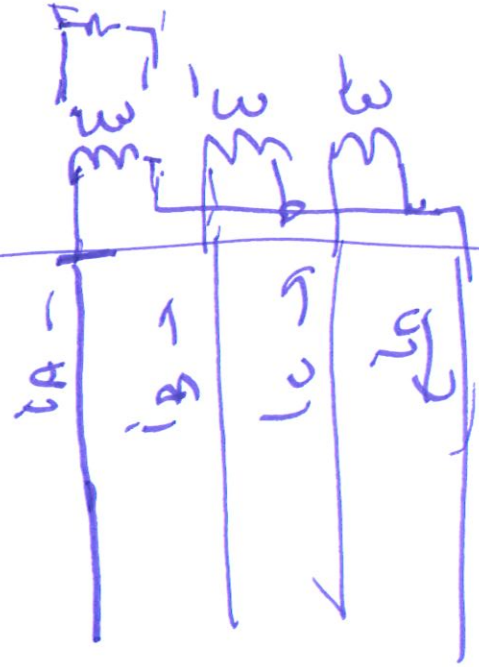
Measurement sequence

Current Transformers

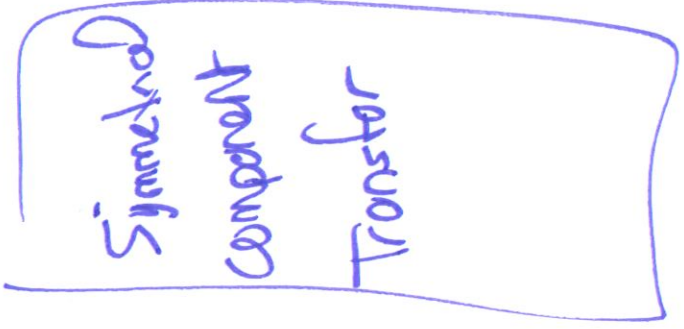


Relay/meter

Analog to Digital



A/D



In a processor

- Lets look at the Cosine Filter Coefficients:

$$k_4 := 0, 1 \dots (4 - 1)$$

$$k_8 := 0, 1 \dots (8 - 1)$$

$$k_{16} := 0, 1 \dots (16 - 1)$$

$$k_{32} := 0, 1 \dots (32 - 1)$$

$$\text{cos}_{\text{coef}}(k, \text{RS}) := \cos\left(\frac{2 \cdot \pi \cdot k}{\text{RS}}\right)$$

$$\text{cos}_{\text{coef}}(k_4, 4) =$$

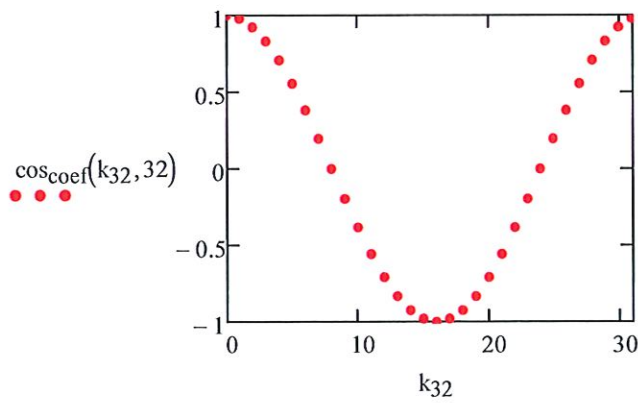
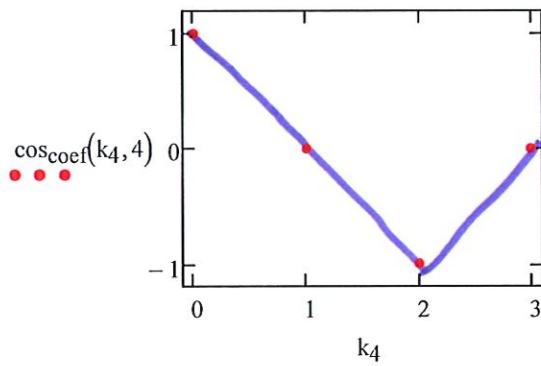
1
0
-1
0

$$\text{cos}_{\text{coef}}(k_8, 8) =$$

1
0.707
0
-0.707
-1
-0.707
0
0.707

$$\text{cos}_{\text{coef}}(k_{16}, 16) =$$

1
0.924
0.707
0.383
0
-0.383
-0.707
-0.924
-1
-0.924
-0.707
-0.383
0
0.383
0.707
0.924



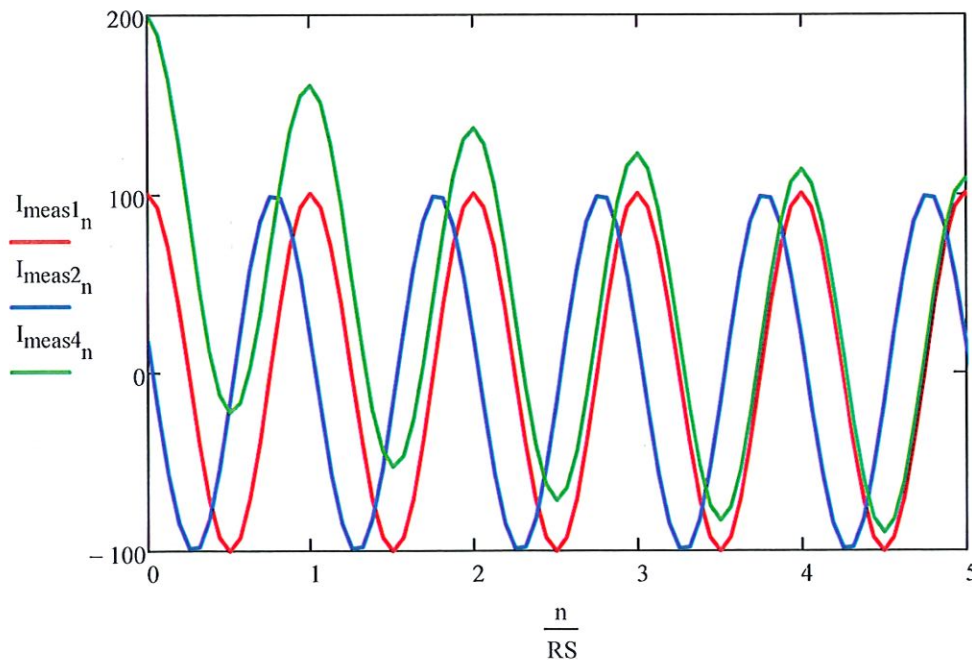
Digital Filter Examples

- Define sampling rate per cycle
RS := 16
- Define length of sample data set, in cycles
D := 8
- Total number of samples:
M := D · RS
- n := 0, 1 .. M - 1
- Create input data signal, sampled at RS per cycle

$$I_{\text{meas}1_n} := 100 \cdot \cos\left(\frac{2 \cdot \pi \cdot n}{RS} + 0\text{deg}\right) \quad I_{\text{meas}2_n} := 100 \cdot \cos\left(\frac{2 \cdot \pi \cdot n}{RS} + 80\text{deg}\right)$$

$$I_{\text{meas}3_n} := 100 \cdot \cos\left(\frac{2 \cdot \pi \cdot n}{RS}\right) + 50 \quad I_{\text{meas}4_n} := 100 \cdot \left(\cos\left(\frac{2 \cdot \pi \cdot n}{RS} + 0\text{deg}\right) + e^{\frac{-n}{2RS}}\right)$$

constant offset *decaying dc offset*



02/16/27

Now define Cosine and Sin filters

$$\text{COSF}(RS, A, q) := \frac{2}{RS} \cdot \sum_{k=0}^{RS-1} [\text{cos}_{\text{coef}}(k, RS) \cdot A_{[q-(RS-1)]+k}]$$

$$\text{SINF}(RS, A, q) := \frac{2}{RS} \cdot \sum_{k=0}^{RS-1} [\text{sin}_{\text{coef}}(k, RS) \cdot A_{[q-(RS-1)]+k}]$$

Sine
weighting function
measurement
over 1 period at sample rate

- Create a filter index, "i" (which includes RS samples of past history (so it starts at (RS - 1))

$$i := (RS - 1) .. M - 1$$

- Create a filter index, "v" (which includes RS/4 samples of past history for delaying cosine filter output put a quarter cycle (so it starts at (RS/4 - 1))

$$v := \left(RS + \frac{RS}{4} - 1 \right) .. M - 1$$

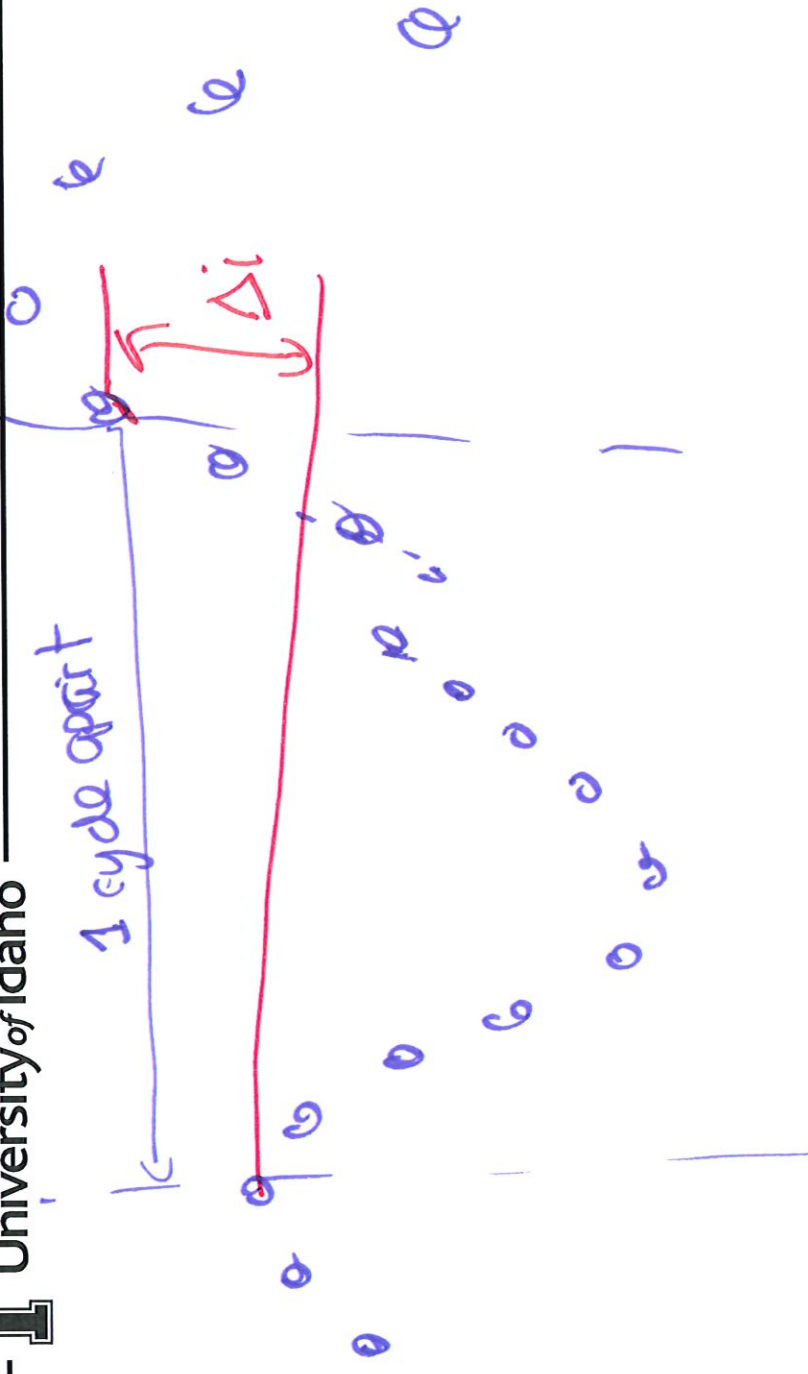
del by 1/4 cycle

$$\text{COSF}(RS, I_{\text{meas1}}, i) =$$

100
92.388
70.711
38.268
0
-38.268
-70.711
-92.388
-100
-92.388
-70.711
-38.268
0
38.268
70.711
92.388
100
92.388
70.711
...

$$\text{SINF}(RS, I_{\text{meas1}}, i) =$$

0
-38.268
-70.711
-92.388
-100
-92.388
-70.711
-38.268
0
38.268
70.711
92.388
100
92.388
70.711
...

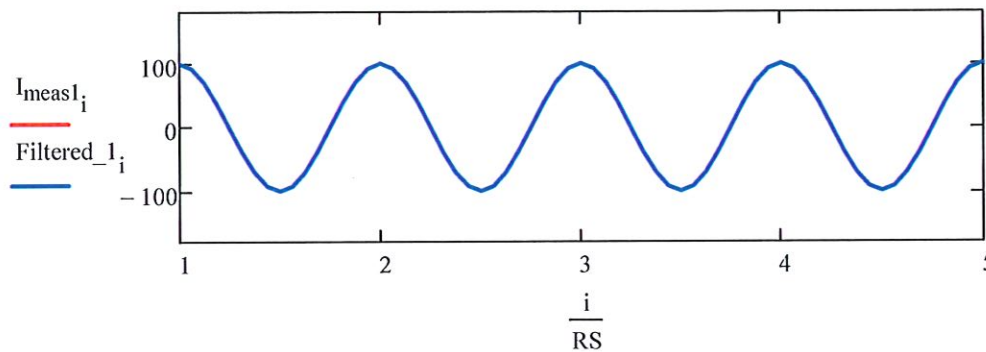


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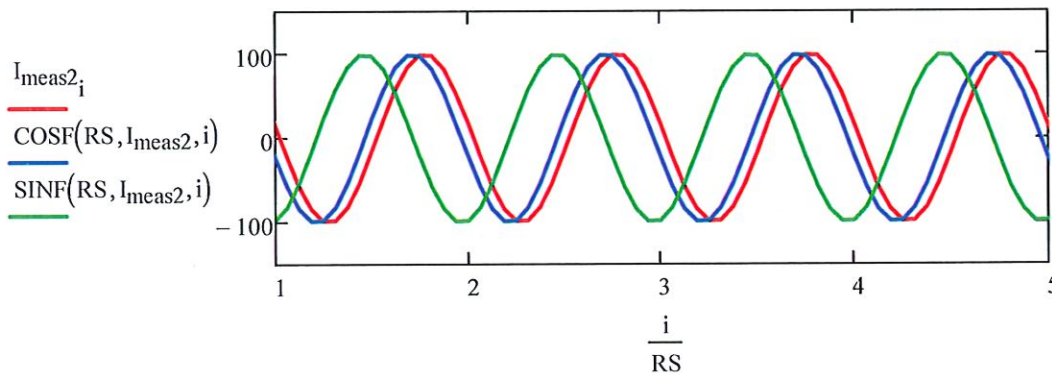
- So we need to compare this angle to a reference. In the case with only one measurement, we compare it to itself.

$$\theta_{1_i} := \text{Angle}1_i - \text{Angle}1_i$$

$$\text{Filtered_}1_i := \sqrt{2} \cdot \text{Mag}1_i \cdot \cos\left[\left(\frac{2 \cdot \pi \cdot i}{RS}\right) + \theta_{1_i}\right]$$



- Now repeat with the second signal, which is phase shifted



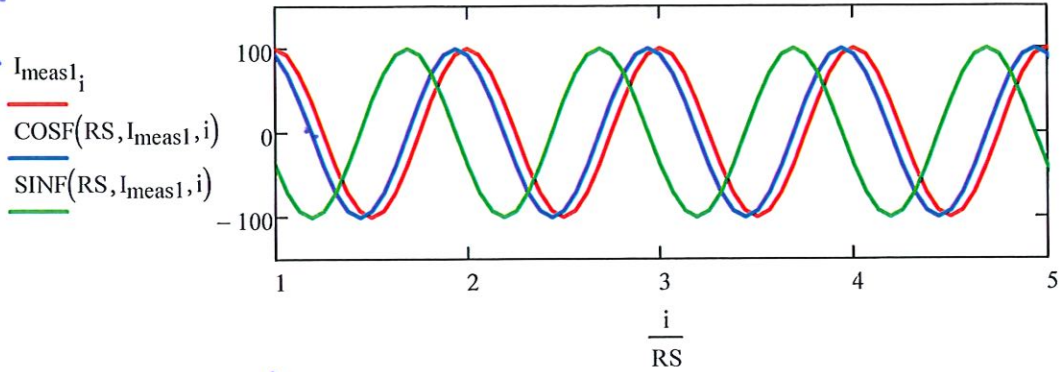
$$\text{Phasor}2_i := \frac{1}{\sqrt{2}} (\text{COSF}(RS, I_{\text{meas}2}, i) - j \cdot \text{SINF}(RS, I_{\text{meas}2}, i))$$

$$\text{Mag}2_i := |\text{Phasor}2_i|$$

$$\text{Angle}2_i := \arg(\text{Phasor}2_i)$$

12/21/21

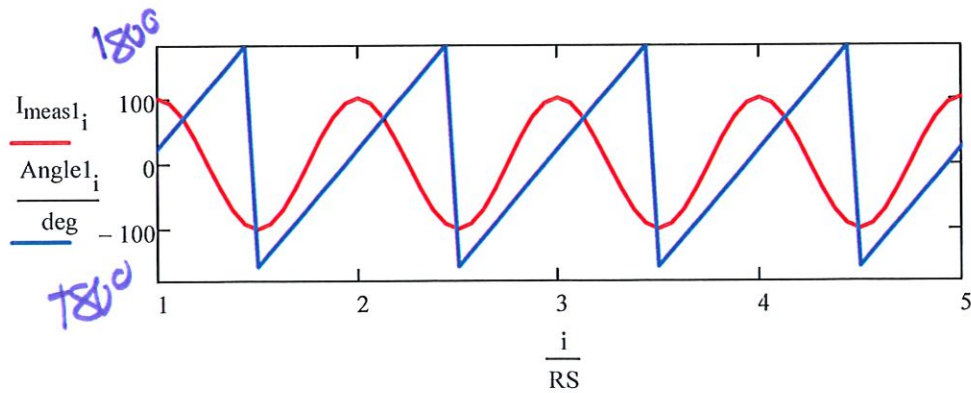
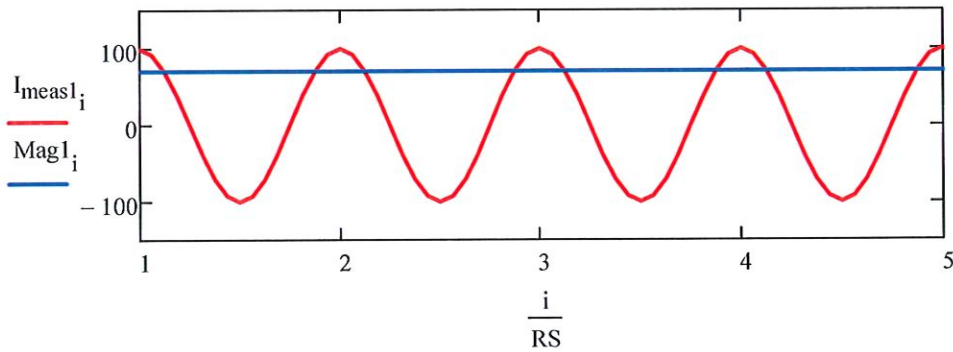
e^j



$$Phasor1_i := \frac{1}{\sqrt{2}} (COSF(RS, I_{meas1,i}) - j \cdot SINF(RS, I_{meas1,i}))$$

$$Mag1_i := |Phasor1_i|$$

$$Angle1_i := \arg(Phasor1_i)$$

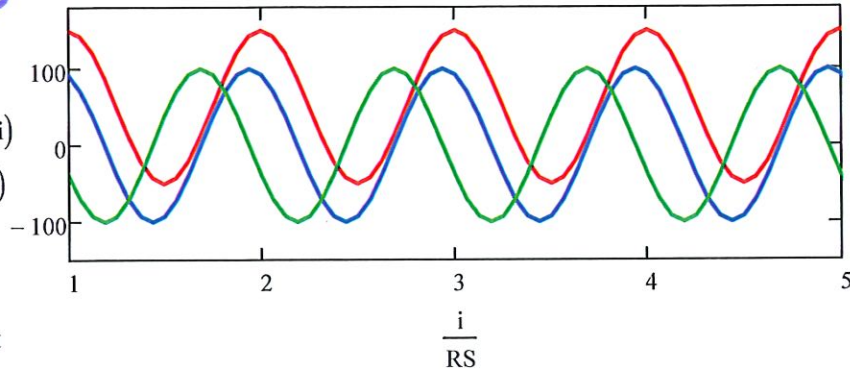


- Now repeat with the third signal, which has a constant dc offset

I_{meas3_i}

$\text{COSF}(RS, I_{meas3}, i)$

$\text{SINF}(RS, I_{meas3}, i)$

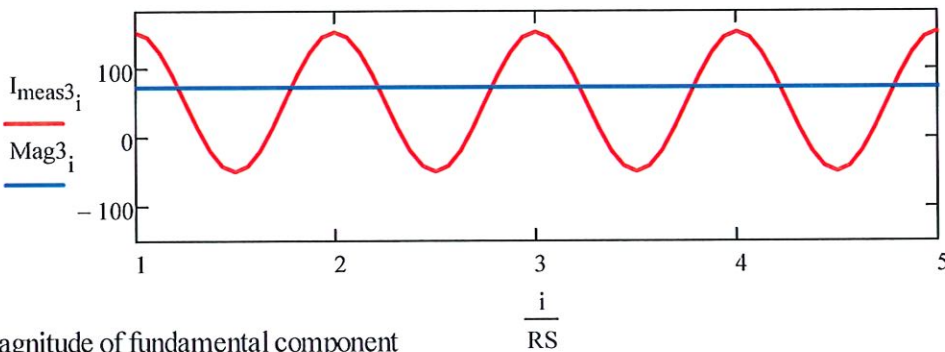


- Rejects DC offset

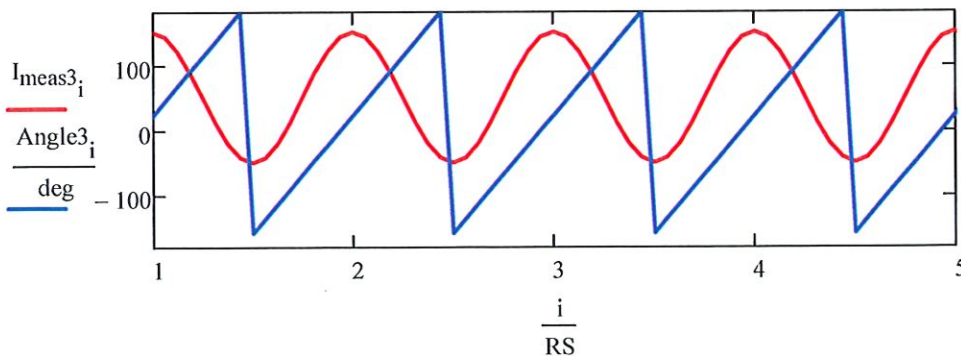
$$\text{Phasor3}_i := \frac{1}{\sqrt{2}} (\text{COSF}(RS, I_{meas3}, i) - j \cdot \text{SINF}(RS, I_{meas3}, i))$$

$$\text{Mag3}_i := |\text{Phasor3}_i|$$

$$\text{Angle3}_i := \arg(\text{Phasor3}_i)$$



RMS magnitude of fundamental component

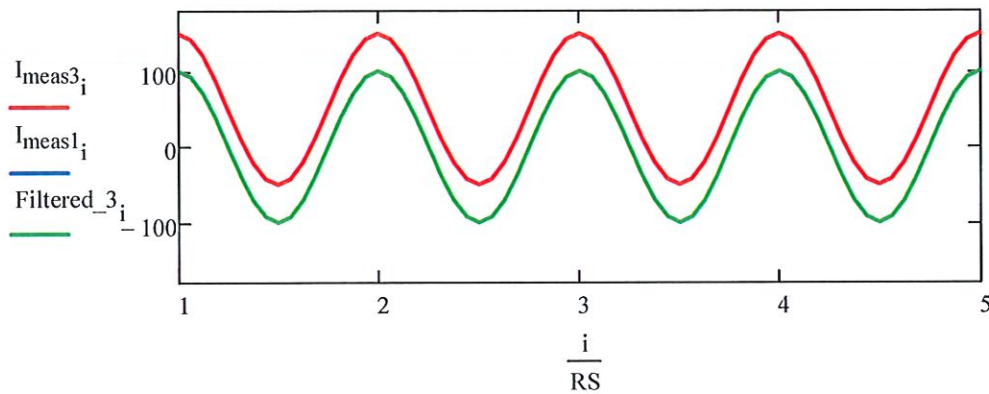


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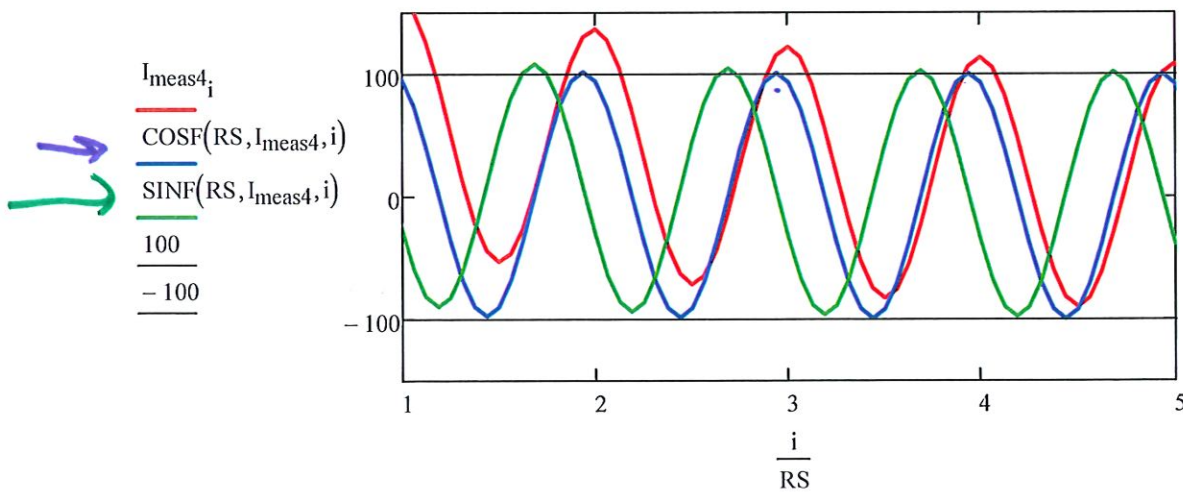
- So we need to compare this angle to a reference. In the case we'll use the first signal as a reference

$$\theta_{3_i} := \text{Angle}_{3_i} - \text{Angle}_{1_i}$$

$$\text{Filtered_3}_i := \sqrt{2} \cdot \text{Mag}_{3_i} \cdot \cos\left[\left(\frac{2 \cdot \pi \cdot i}{RS}\right) + \theta_{3_i}\right]$$



- Now repeat with the fourth signal, which has a decaying DC offset.

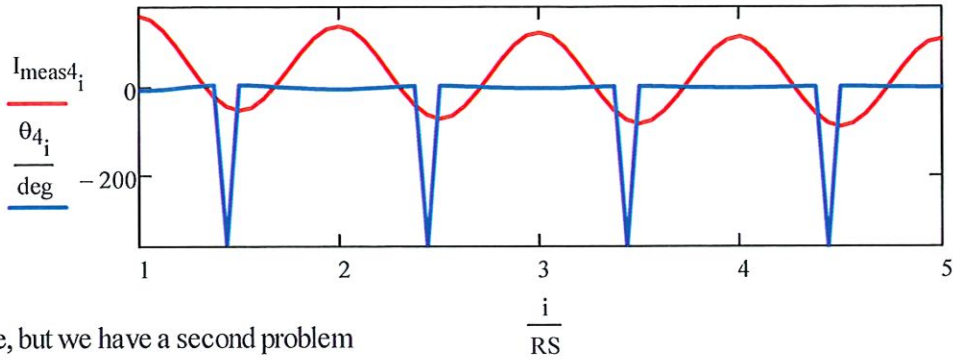


Sine filter passing some DC offset, but not cosine

$$\text{Phasor}_{4_i} := \frac{1}{\sqrt{2}} (\text{COSF}(RS, I_{\text{meas}4, i}) - j \cdot \text{SINF}(RS, I_{\text{meas}4, i}))$$

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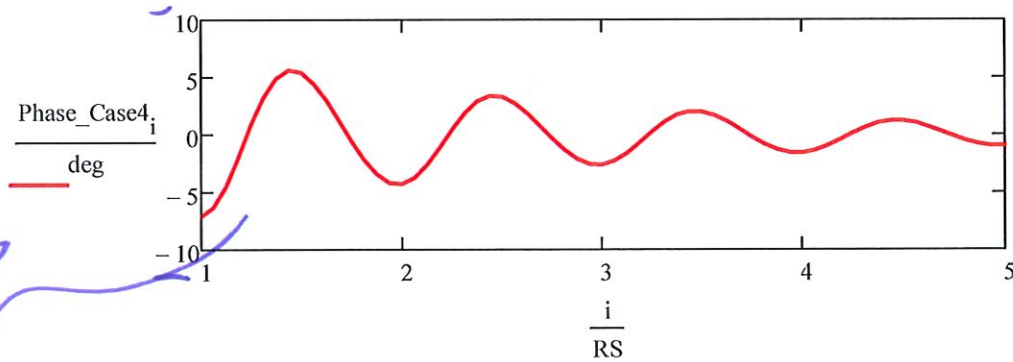
$$\theta_{4_i} := \text{Angle}_{4_i} - \text{Angle}_{1_i}$$



As does angle, but we have a second problem due to reset times

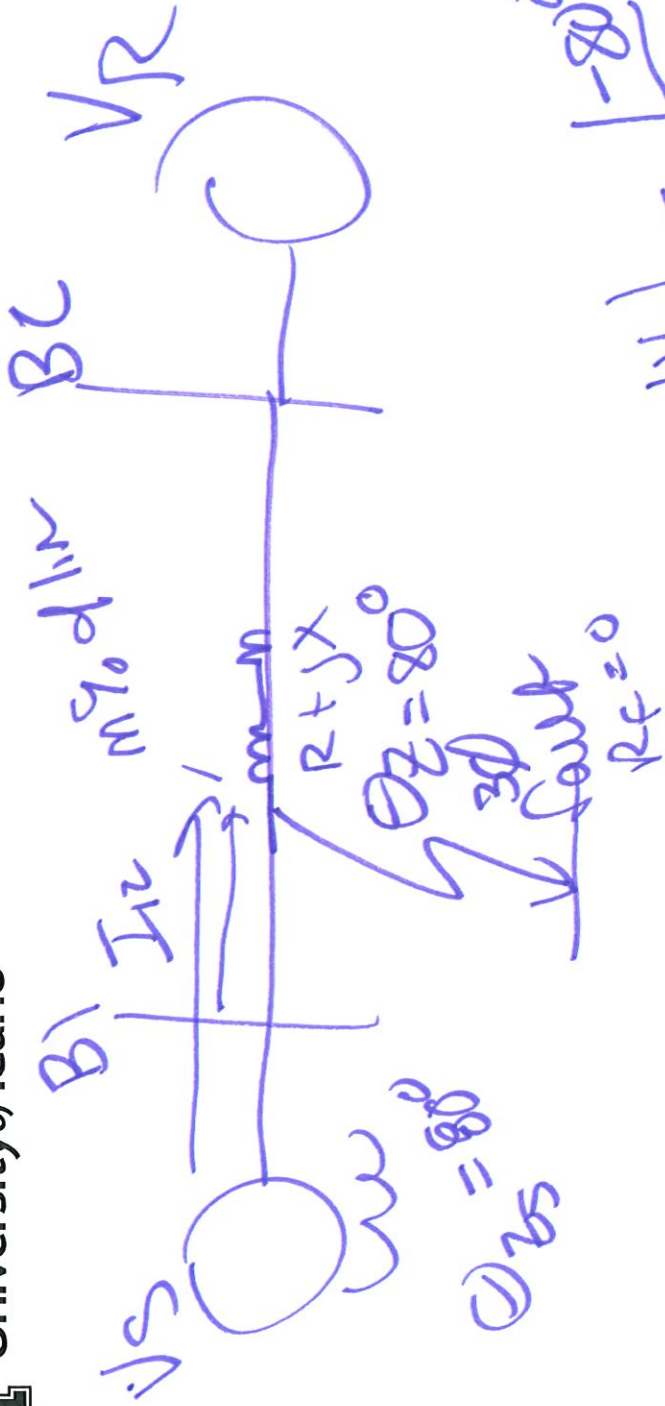
- Fix for the reset time issue:

$$\text{Phase_Case}_{4_i} := \begin{cases} \text{Angle}_{4_i} - \text{Angle}_{1_i} & \text{if } |\text{Angle}_{4_i} - \text{Angle}_{1_i}| < \pi \\ \text{Angle}_{4_i} - \text{Angle}_{1_i} - 2 \cdot \pi & \text{if } (\text{Angle}_{4_i} - \text{Angle}_{1_i}) > \pi \\ \text{Angle}_{4_i} - \text{Angle}_{1_i} + 2 \cdot \pi & \text{if } \text{Angle}_{4_i} - \text{Angle}_{1_i} < -(\pi) \end{cases}$$



So still see decaying dc offset problem in angle calculation.

angle varies with time due to decaying dc offset



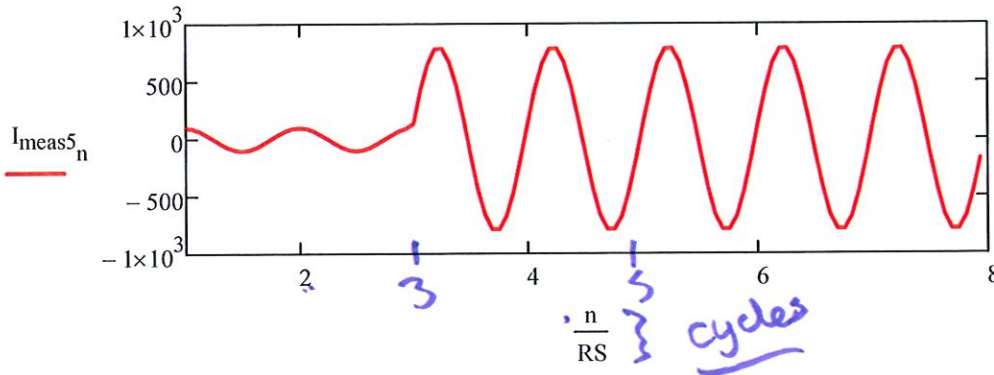
$$I_{12} = \frac{|V_s| \angle 0}{|z_{s1} + n z_u|}$$

$|z_{s1}| \angle 80^\circ$ $|z_u| \angle 60^\circ$

$$|V_s| = \frac{|V_s|}{|z_{s1} + n z_u|} \angle -80^\circ$$

A few more cases:

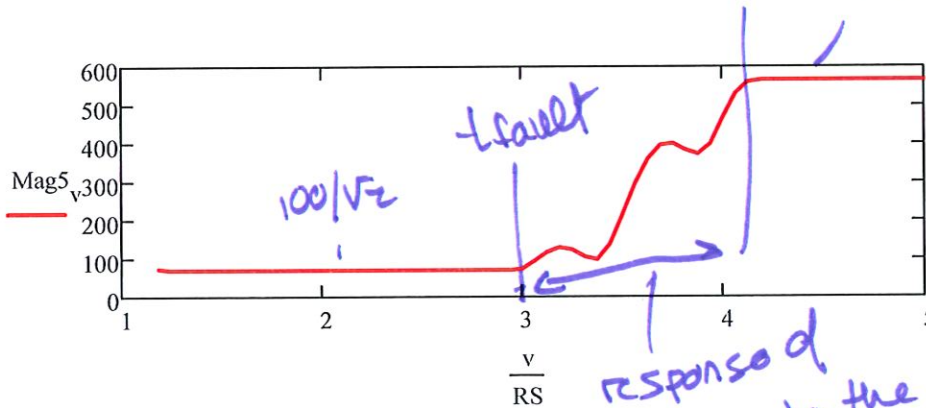
$$I_{meas5_n} := \begin{cases} 100 \cdot \cos\left(\frac{2 \cdot \pi \cdot n}{RS} + 0\text{deg}\right) & \text{if } 0 < n < 3 \cdot RS \\ 800 \cdot \cos\left[\frac{2 \cdot \pi \cdot (n + 2 \cdot RS)}{RS} - 80\text{deg}\right] & \text{otherwise} \end{cases}$$



$$\text{Phasor5}_v := \frac{1}{\sqrt{2}} \left(\text{COSF}\left(RS, I_{meas5}, v\right) + j \cdot \text{COSF}\left(RS, I_{meas5}, v - \frac{RS}{4}\right) \right)$$

$$\text{Mag5}_v := |\text{Phasor5}_v|$$

$$\text{Angle5}_v := \arg(\text{Phasor5}_v)$$

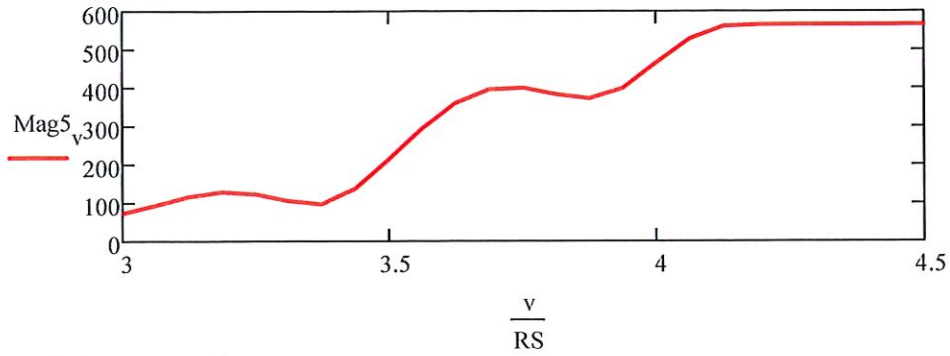


- Notice the filter response time

response of filter to the change in current

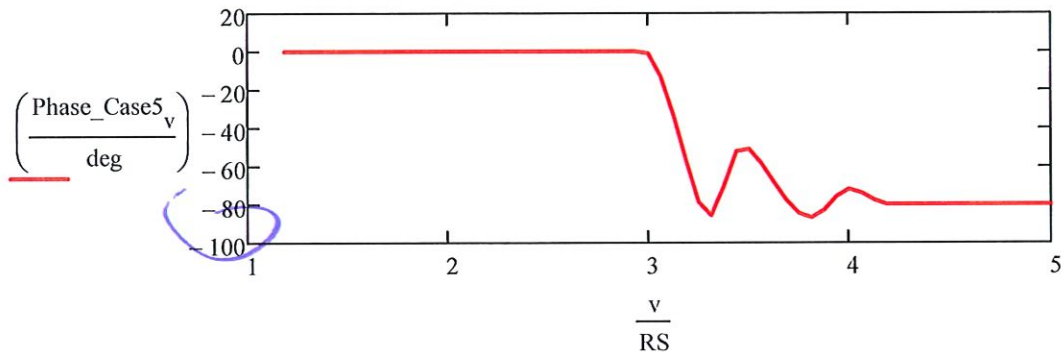
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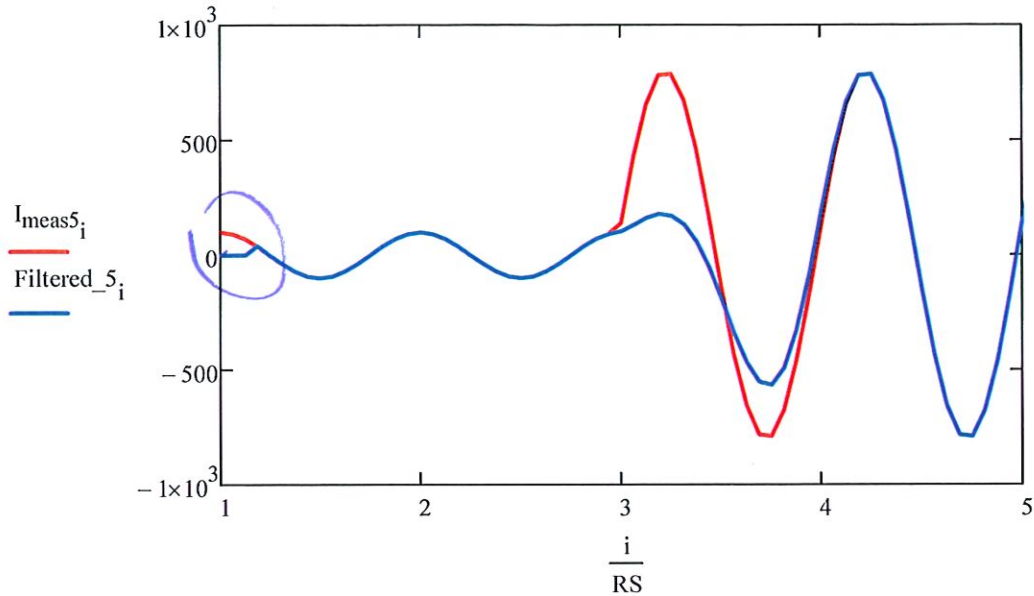
Takes a little over a cycle

$$\text{Phase_Case}_{5_v} := \begin{cases} \text{Angle}_{5_v} - \text{Angle}_{1_v} & \text{if } |\text{Angle}_{5_v} - \text{Angle}_{1_v}| < \pi \\ \text{Angle}_{5_v} - \text{Angle}_{1_v} - 2 \cdot \pi & \text{if } (\text{Angle}_{5_v} - \text{Angle}_{1_v}) > \pi \\ \text{Angle}_{5_v} - \text{Angle}_{1_v} + 2 \cdot \pi & \text{if } \text{Angle}_{5_v} - \text{Angle}_{1_v} < -(\pi) \end{cases}$$



$$\text{Filtered}_{5_v} := \sqrt{2} \cdot \text{Mag}_{5_v} \cdot \cos \left[\left(\frac{2 \cdot \pi \cdot v}{RS} \right) + \text{Phase_Case}_{5_v} \right]$$

12/19/20

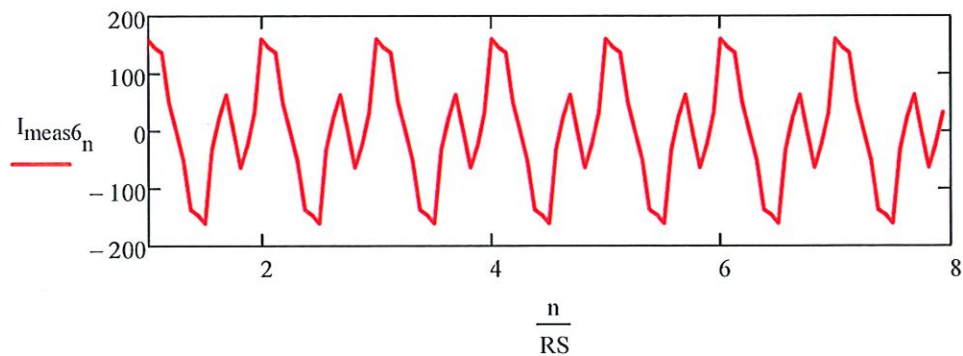


Notice delay in filter response

- Now add some harmonics.

First, integer harmonics

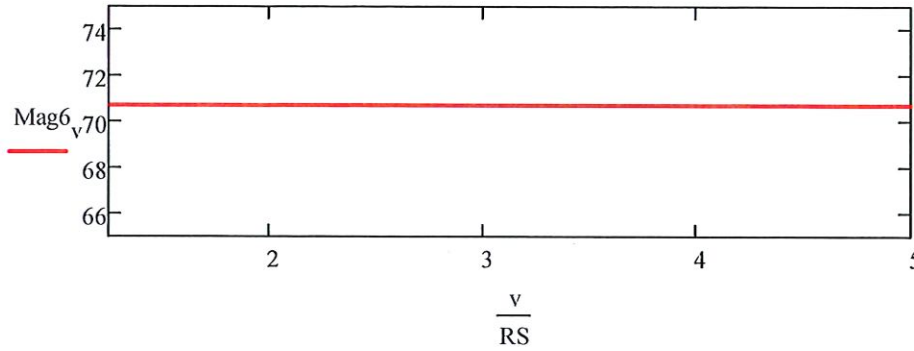
$$I_{meas6_n} := 100 \cdot \cos\left(\frac{2 \cdot \pi \cdot n}{RS}\right) + 80 \cdot \sin\left[2 \cdot \left(\frac{2 \cdot \pi \cdot n}{RS}\right)\right] + 40 \cdot \cos\left[3 \cdot \left(\frac{2 \cdot \pi \cdot n}{RS}\right)\right] + 20 \cdot \cos\left[7 \cdot \left(\frac{2 \cdot \pi \cdot n}{RS}\right)\right]$$



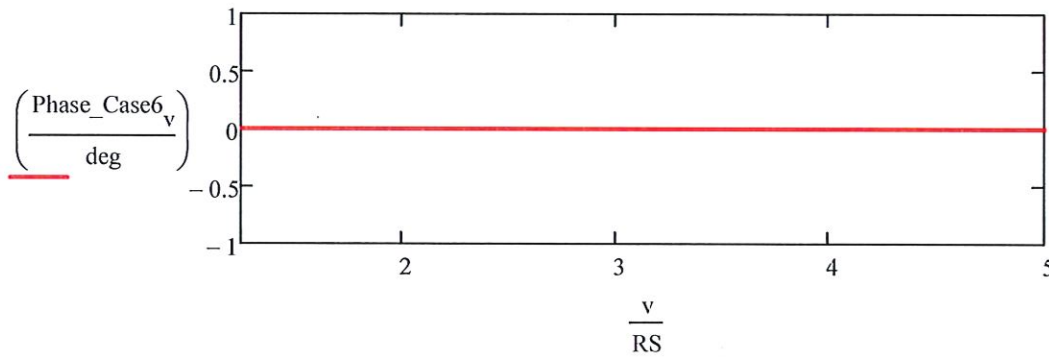
$$\text{Phasor6}_v := \frac{1}{\sqrt{2}} \left(\text{COSF}\left(RS, I_{meas6}, v\right) + j \cdot \text{COSF}\left(RS, I_{meas6}, v - \frac{RS}{4}\right) \right)$$

L2 20/20

$$\text{Mag6}_v := |\text{Phasor6}_v| \quad \text{Angle6}_v := \arg(\text{Phasor6}_v)$$



$$\text{Phase_Case6}_v := \begin{cases} \text{Angle6}_v - \text{Angle1}_v & \text{if } |\text{Angle6}_v - \text{Angle1}_v| < \pi \\ \text{Angle6}_v - \text{Angle1}_v - 2 \cdot \pi & \text{if } (\text{Angle6}_v - \text{Angle1}_v) > \pi \\ \text{Angle6}_v - \text{Angle1}_v + 2 \cdot \pi & \text{if } \text{Angle6}_v - \text{Angle1}_v < -(\pi) \end{cases}$$



$$\text{Filtered_6}_v := \sqrt{2} \cdot \text{Mag6}_v \cdot \cos\left[\left(\frac{2 \cdot \pi \cdot v}{\text{RS}}\right) + \text{Phase_Case6}_v\right]$$

