

ECE 523
Symmetrical Components

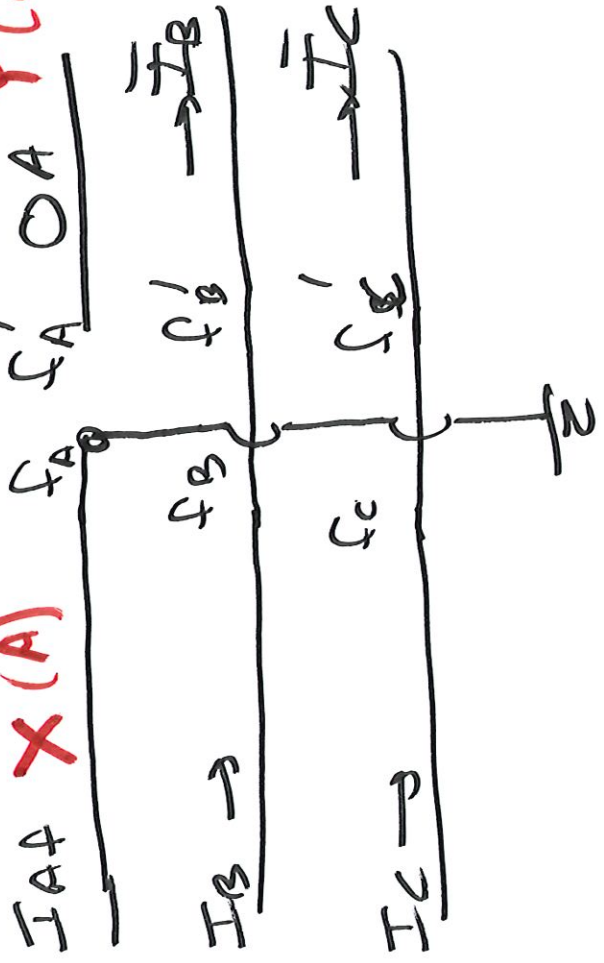
Session 21

- Simultaneous SLG with broken conductor

→ conductor fault to the ground

$I_{AF} \times (A)$ f_A f'_A O_A $Y(A')$

A-reference symmetrical components



Boundary conditions

Phase A open: $Z_A = \infty$

$Z_B = Z_C = 0$

$I_A = I_{A'} = 0$ (access open)

$$\overline{SLG} \quad I_{Bf} = I_{Cf} = 0$$

$$I_{Af} = I_{A'} = I_{A1} + I_{A2} + I_{A0}$$

$$V_{AfG} = 0 \quad (R_f = 0)$$

$$V_{A'fG} = ?$$

SLG (X-side)

$$I_{A1X} = I_{A2X} = I_{A0} \quad (\text{fault itself})$$



But will also have pos sequence line current - load flow

-and $I_2 + I_0$ on line due to phase open

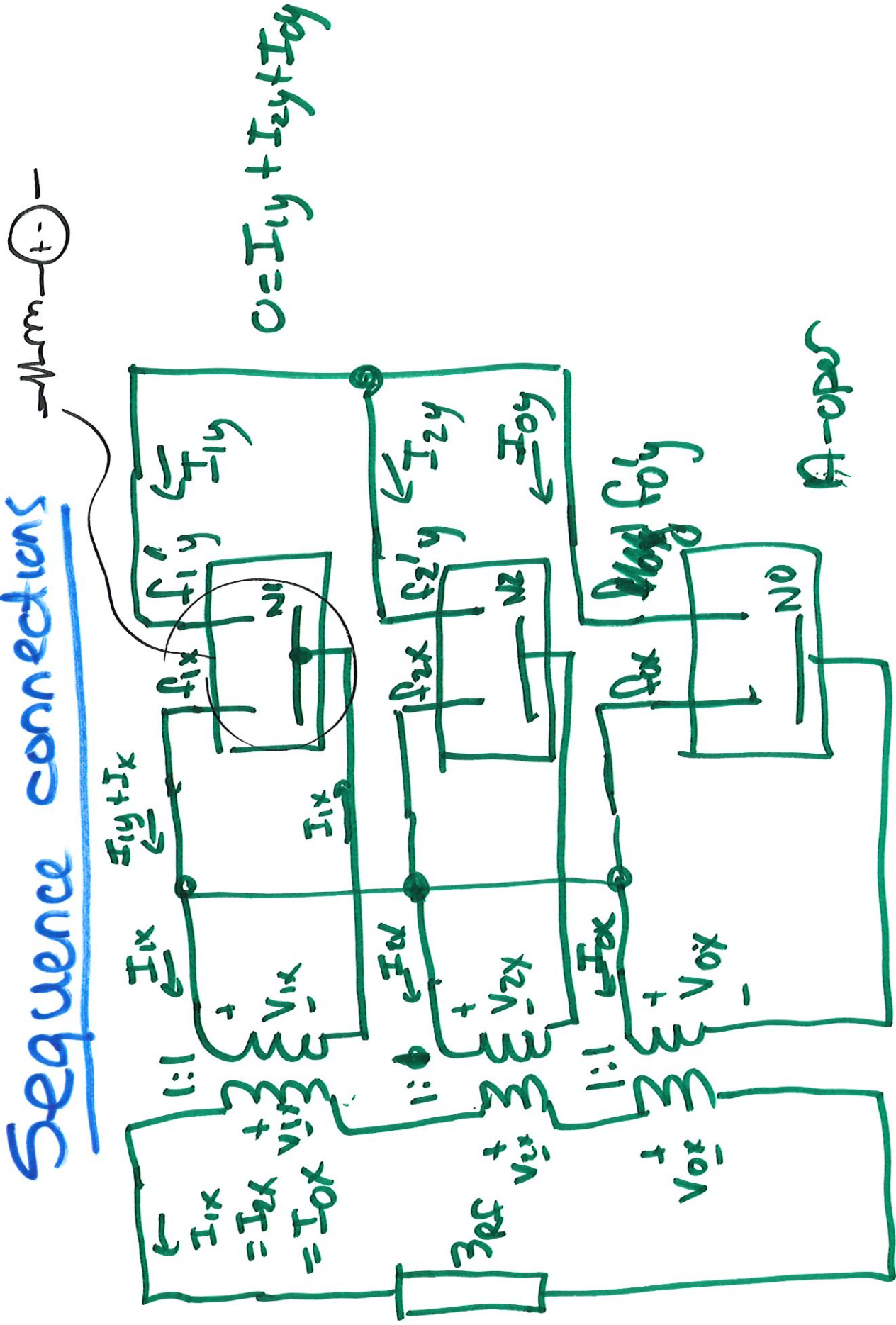
$$V_{A0X} + V_{A1X} + V_{A2X} = 0 = 3 I_0 R_f$$

I phase open

$$V_{1ff'} = V_{2ff'} = V_{0ff'}$$

$$I_{1Y} + I_{2Y} + I_{0Y} = 0$$

Sequence connections



Rest of Semester

Models of power apparatus
in sequence domain for day studies

- Transmission/distribution lines

↳ mutual coupling

- cables

- Transformers (external faults)

- Rotating machines - external faults

- Inverter based generation

(wind, PV, storage) - impact on

solution technique

- Specialized connections

- 3 winding

- Tap changers

- Grounding transformers

Overhead Line Models / cable models

(1) models

(2) calculating model data

$$- Z_0$$

$$\frac{Z_0}{\mu}$$

Models - Steady state
 or quasi-steady state
 (phaser models)

short, medium, long

PI

reduced to
 modified PI

equal

⇒ can apply in pos, negative and

zero sequence

R, L, C per length

Short line model



$R_0, R_1, R_2 \quad X_0, X_1, X_2$

- overhead lines for

power flow

~ 50 km or less

- cables

~ 5 km or less

(less L per length,
more C per length)

- fault analysis most

likely used this unless
system high resistance

grounded or
ungrounded



\Rightarrow If that is case
MUST USE medium
or long with
capacitances



medium length

OH: 50km - 150km

S - 15 (20) for cables

(150km) based on frequency

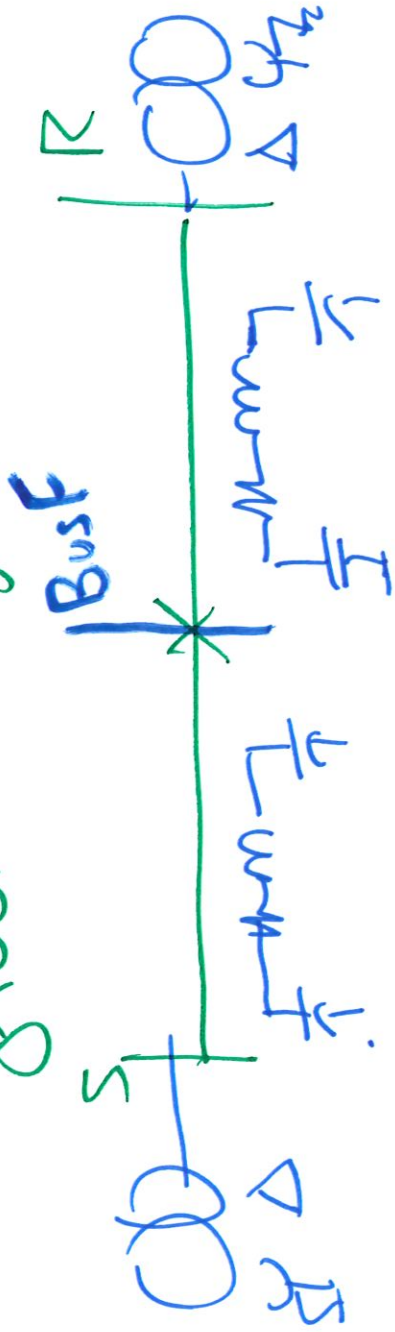
PI model ✓ same as short lin



$$\left(j\omega C \frac{C_0, C_1, C_2}{2} \right) \cdot \text{length}$$

for longer underground cables this capacitance can impact fault currents

for fault studies with ~~etc.~~
 ungrounded or high resistance
 grounded systems...



T-model instead of PI



Long Line model



> (sum) (rare in cables)

- If not an ungrounded system

→ primarily want R', jX'

$$Z_{in} = \frac{Z_0 \cosh \gamma l}{\sinh \gamma l} \quad (R + j\omega L) \cdot \text{length}$$

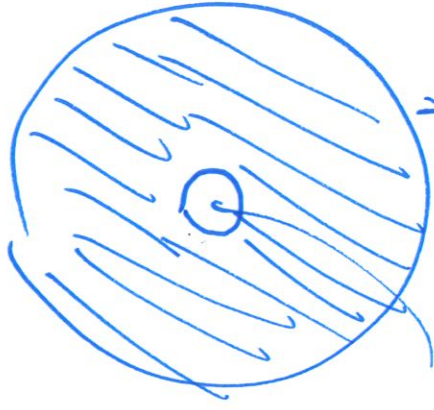
Calculating parameters for overhead lines



$\rightarrow \Omega / \text{length}$

- accounts for skin effect

$$R_{DC} = \frac{\rho \ell}{A}$$



no current

get from tables
or test data

or
line constants
program that
calculates from
dimensional data

Intro to power systems
course

$L' = \frac{\mu_0}{2\pi} \ln\left(\frac{D_m}{R_b}\right)$ in H/length

μ_0 = permeability of free space

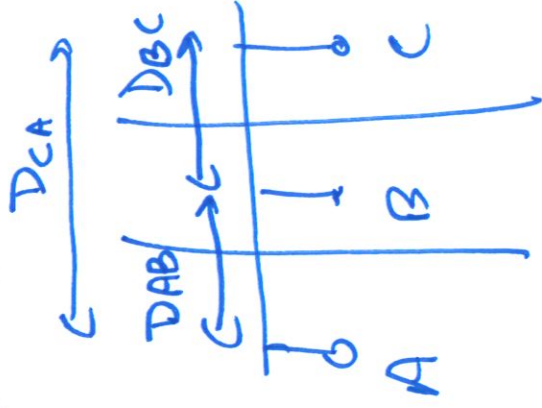
$(\mu = \mu_r \mu_0)$

μ_r relative permeability

= 1 for overhead lines

$D_m = \sqrt[3]{D_{AB} \cdot D_{BC} \cdot D_{CA}}$ → Geometric mean distance

$R_b \Rightarrow$ geometric mean ~~radius~~ radius → $\begin{cases} \text{Single conductor} \\ \text{Bundled conductor} \end{cases}$



single conductor

→ Geometric mean radius of conductor

⇒ Accounts for skin effect

- Accounts for magnetic flux linkage

- Stranding

get from
data sheet/
table

$$\omega L' \cdot \text{length} = \omega \cdot \text{length} \cdot \frac{\mu_0 \ln\left(\frac{D_m}{R_{lo}}\right)}{2\pi}$$

$$\underline{\underline{Z_1 = R_{AC} \cdot \text{length} + j\omega L' \cdot \text{length}}}$$

