

ECE 523: Homework #2

Due Session 9 (September 19)

1. Determine the symmetrical components for the following currents and sketch a phasor diagram, based on

- (a) Phase "a" referenced components
- (b) Phase "b" referenced components
- (c) Phase "c" referenced components

$$I_A := 0A \cdot e^{0\text{deg}}$$

$$I_B := 0A \cdot e^{-j \cdot 120\text{deg}}$$

$$I_C := 2500A \cdot e^{j \cdot 30\text{deg}}$$

2. Repeat problem 1. with the following currents:

$$I_A := 4500A \cdot e^{-j \cdot 25.84\text{deg}}$$

$$I_B := 8503A \cdot e^{-j \cdot 229.5\text{deg}}$$

$$I_C := 4500A \cdot e^{j \cdot 94.16\text{deg}}$$

3. Determine the phase voltage given the following phase "a" referenced symmetrical components.

Repeat assuming they are instead phase "b" and then phase "c" referenced symmetrical components

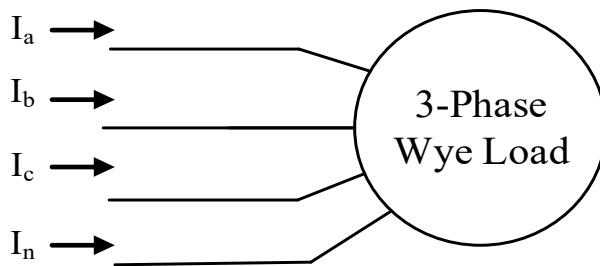
$$\text{pu} := 1$$

$$V_0 := 0.274\text{pu} \cdot e^{-j \cdot 90\text{deg}}$$

$$V_1 := 0.709\text{pu} \cdot e^{j \cdot 90\text{deg}}$$

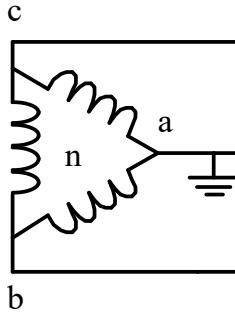
$$V_2 := 0.299\text{pu} \cdot e^{-j \cdot 90\text{deg}}$$

4. If the load is unbalanced, neutral current will exist. Find the relationship between the neutral current I_n and the phase a zero sequence current I_{a0}



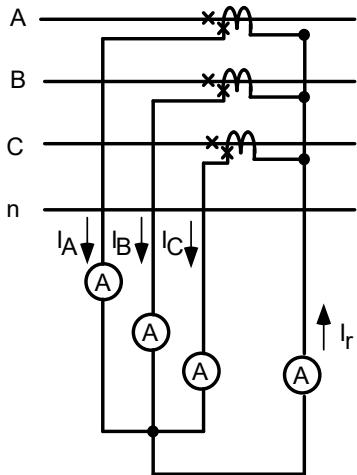
5. The ungrounded system below has a phase to ground fault on phase "a". Assume that the line to ground (and line to neutral voltages) were balanced three phase set before the fault occurred. Do the following:

- (a) Find the symmetrical components of the phase a line-to-neutral voltages when a ground fault is applied (V_{an0} , V_{an1} , V_{an2}).
- (b) Repeat part (a) using line to ground voltages instead of the line to neutral voltages and find (V_{ag0} , V_{ag1} , V_{ag2}).



6. Do the following:

- (a) A set of current transformers reads the following currents (in Amperes). If the current transformers each have a turns ratio of 5:500 (usually referred to as a current transformation ratio or CTR of 500:5) calculate the primary currents in amps.



Note that the symbol:
is equivalent to:

$$I_A := 12e^{-j \cdot 87\text{deg}}$$

$$I_B := 4 \cdot e^{-j \cdot 120\text{deg}}$$

$$I_C := 4 \cdot e^{j \cdot 120\text{deg}}$$

- (b) Calculate the symmetrical components of the secondary currents (I_{a0} , I_{a1} , I_{a2}).
- (c) Calculate the current measured by the fourth ammeter (I_r) and compare it to the zero sequence current calculated in part (b). How do they compare?
- (d) Using the primary current calculated in part (a), repeat part (b) if the CTs are connected in delta (relay currents should lag the primary line currents by 30 degrees).