

ECE 525

POWER SYSTEM PROTECTION  
AND RELAYING

SESSION no. 15

- Determine the relay R2 response time

$$M_{R2\_If\_max} := \frac{\left( \frac{I_{3ph\_bus1}}{CTR_{R2}} \right)}{I_{pu\_R2}} \quad M_{R2\_If\_max} = 10.69$$

$$t_{pu\_R2\_If\_max} := t_{VI}(TD_{R2}, M_{R2\_If\_max}) \quad t_{pu\_R2\_If\_max} = 0.065 \text{ s}$$

- Desired minimum pick up time relay 1 for a bus 1 fault:

$$t_{pu\_R1\_desired} := t_{pu\_R2\_If\_max} + CTI \quad t_{pu\_R1\_desired} = 0.365 \text{ s}$$

- Now find M for relay 1 for this fault

$$M_{R1\_If\_max} := \frac{\left( \frac{I_{3ph\_bus1}}{CTR_{R1}} \right)}{I_{pu\_R1}} \quad M_{R1\_If\_max} = 6.84$$

- Now rewrite the response time equation so we can solve for time dial setting
- Note that we could also do this step graphically

$$TD_{VI}(t_{req}, M) := \frac{\frac{t_{req}}{\text{sec}}}{\left( \frac{3.88}{M^2 - 1} + 0.0963 \right)}$$

$$TD_{R1} := TD_{VI}(t_{pu\_R1\_desired}, M_{R1\_If\_max})$$

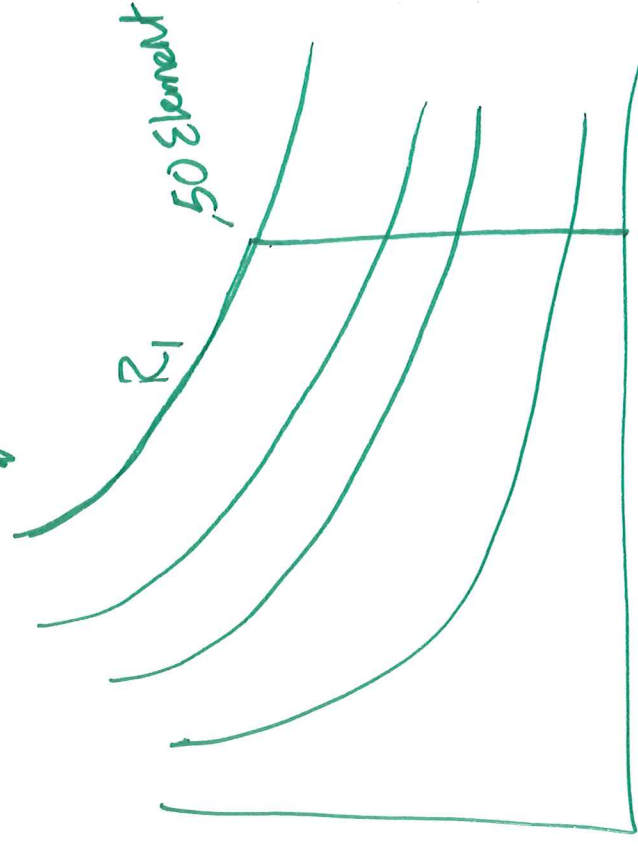
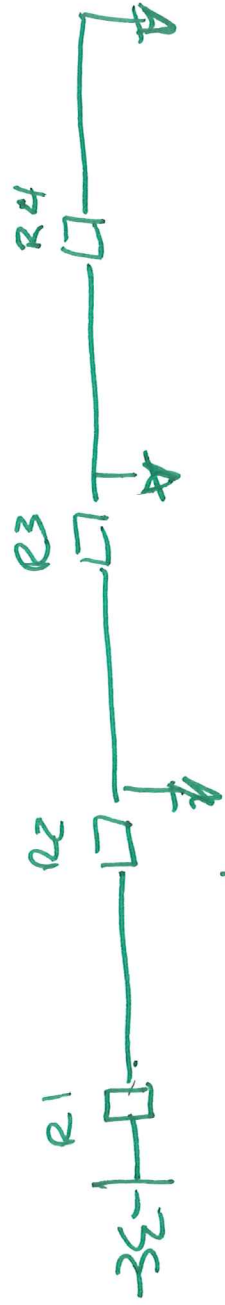
$$TD_{R1} = 2.02$$

Set TD to nearest 0.1:

$$TD_{R1\_set} := 2.1$$

$$t_{VI}(TD_{R1\_set}, M_{R1\_If\_max}) = 0.38 \text{ s}$$

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So we see a time interval of:

$$t_{VI}(TD_{R1\_set}, M_{R1\_If\_max}) - t_{VI}(TD_{R2}, M_{R2\_If\_max}) = 0.315 \text{ s} \quad \text{Meets criteria}$$

- Now check the coordination with the other extreme:

$$M_{R1\_If\_min} := \frac{\left( \frac{I_{LL\_bus2}}{CTR_{R1}} \right)}{I_{pu\_R1}} \quad M_{R1\_If\_min} = 1.97$$

$$M_{R2\_If\_min} := \frac{\left( \frac{I_{LL\_bus2}}{CTR_{R2}} \right)}{I_{pu\_R2}} \quad M_{R2\_If\_min} = 3.09$$

$$t_{VI}(TD_{R1\_set}, M_{R1\_If\_min}) - t_{VI}(TD_{R2}, M_{R2\_If\_min}) = 2.74 \text{ s}$$

### Other types of elements:

- Ground elements: set  $I_{pu}$  based on the worst case zero sequence load current  
- Make sure you are clear on whether you are using  $I_0$  or  $I_R = 3I_0$  (residual current)
- Negative sequence elements use a similar criteria.

$$\bar{I}_A + \bar{I}_B + \bar{I}_C$$

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**Adding an instantaneous element at B1 to increase response time for a close-in, high current faults.**

- Calculate 3 phase fault current 60% of the length of the feeder.

$$I_{f3phpu60\%} := \frac{1}{Z_{S1} + 0.6 \cdot Z_{fd11}} \quad I_{f3phpu60\%} = -0.91i \quad I_{f3ph60\%} := |I_{f3phpu60\%}| \cdot I_b$$

$$I_{f3ph60\%} = 2186.93 \text{ A}$$

- Convert secondary amps

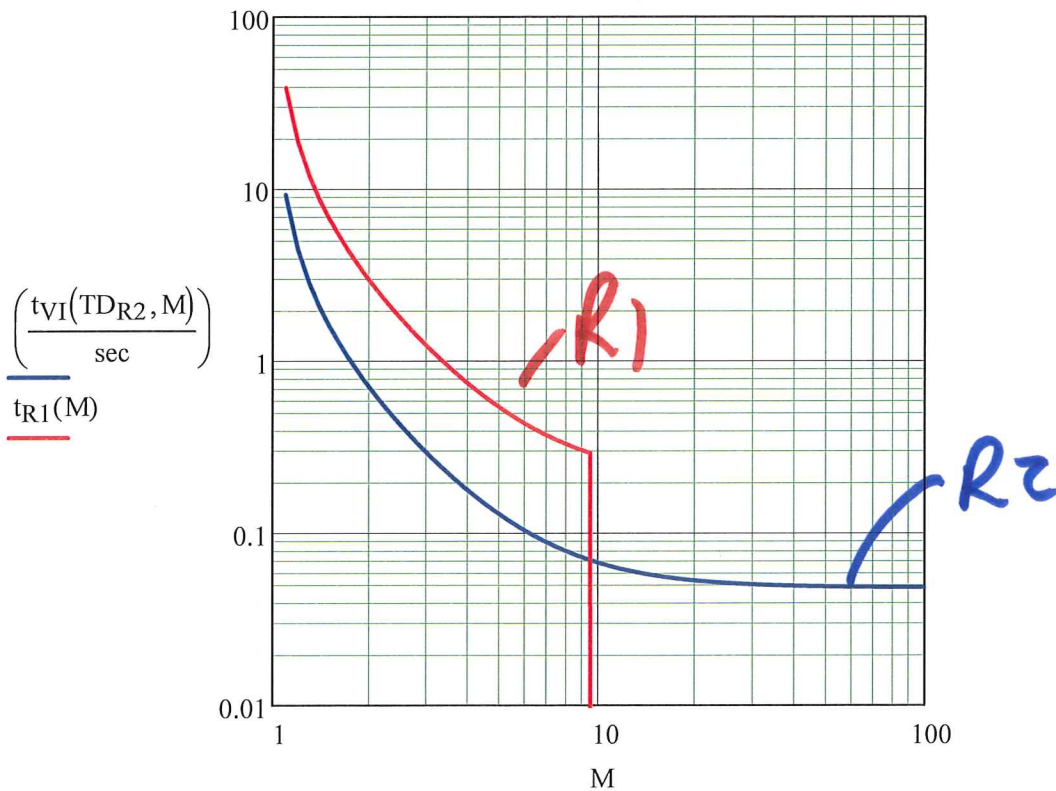
$$I_{f3ph60\%\_sec} := \frac{I_{f3ph60\%}}{CTR_{R1}} \quad I_{f3ph60\%\_sec} = 68.34 \text{ A}$$

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- Round this value up and use this as the pick up setting for the 50P (instantaneous) element
  - $I_{R1\_50\_set} := 70A$
- Combine this with the output for the 51 element for R1 using a Mathcad If-Then-Else element
- Also convert the response of the 50 element to be functions of M (not generally done otherwise)

$$t_{R1}(M) := \begin{cases} \frac{t_{VI}(TD_{R1\_set}, M)}{\text{sec}} & \text{if } 0 \leq M \leq \frac{I_{R1\_50\_set}}{I_{pu\_R1}} \\ 0.00001 & \text{otherwise} \end{cases}$$

M := 1, 1.1 .. 100



→ Inverse time overcurrent elements

- Assumptions

- ~~Assumed~~ No R<sub>f</sub>
  - Kind of adopted
- Fault current varies significantly with location
  - coordination based on current magnitude
- can also do with 50 elements and time delays for backup zones



- Also assumed fault current flows 1 direction
- directional supervision later

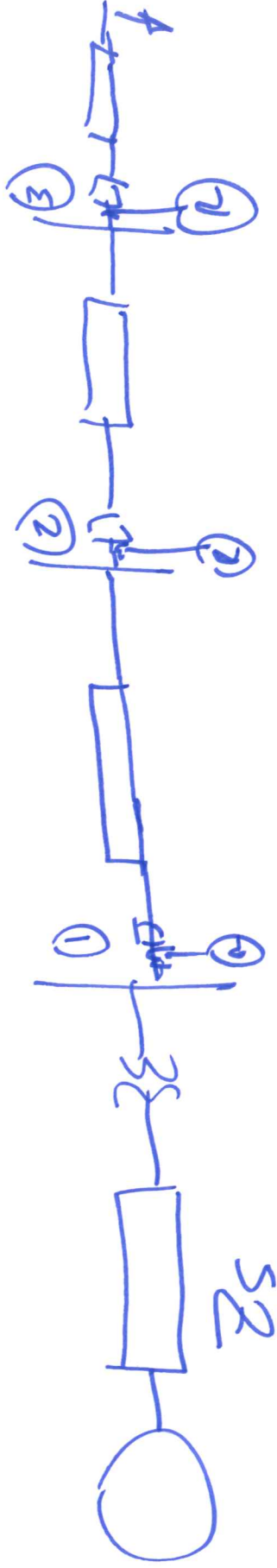
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What if fault current doesn't vary much with fault location?

- high source impedance compared to line impedance

- ① Try use extremely inverse elements
- ② Time graded protection
- ③ Use communication

Time graded protection



If a fault is detected  $R1, R2 + R3$  have set time delays

$$(R3) - T_{delay} = 0$$

$$(R2) T_{delay} = CTI$$

$$(R1) T_{delay} = 2 \cdot CTI$$



# SOV (SIV)

- Voltage supervised overcurrent element

- Generator relays acting as backup for line protection

- If  $V$  below threshold the overcurrent element is enabled

Generators connected to distributed-coordinated overcurrent elements

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<h1>Symmetrical Components</h1>		<small>ECE525 Lecture 15</small>
<ul style="list-style-type: none"><li>● Review of basics</li><li>● Sequence Equivalents</li><li>● Fault Analysis</li></ul>		
<small>Symmetrical Components</small>		<small>Fall 2018</small>

<h1>References</h1>		<small>ECE525 Lecture 15</small>
<ul style="list-style-type: none"><li>● Your power systems analysis class text book</li><li>● NPAG: Chapter 4 (analysis) Chapter 5 (equipment models)</li><li>● J.L. Blackburn, <i>Protective Relaying: Principles and Applications</i>, Any Edition: Chapter 4</li><li>● P.M. Anderson, <i>Analysis of Faulted Power Systems</i>, IEEE Press 1995</li><li>● J.L. Blackburn, <i>Symmetrical Components for Power Systems Engineering</i>, Marcel-Dekker, 1993.</li><li>● Nasser Tleis, <i>Power Systems Modelling and Fault Analysis: Theory and Practice</i>. Newnes Power Engineering Series. 2008</li></ul>		
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## History

- Fortescue, 1918
  - » Unbalanced n-phase system can be broken down into sets of balanced n-phase systems
  - » Add using superposition

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## What is it?

- Method for analysis of multiphase systems under unbalanced conditions
  - » Steady-state conditions
  - » Phasor Analysis
  - » Visualization
- Allows a fast, efficient way to analyze unbalanced condition in real time
- Relays set to look at specific components

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# Basic Equations

- De-couple voltage or current into 3 balanced 3 phase sets
  - » Positive phase sequence (ABCABC...):  $V_1$
  - » Negative phase sequence (ACBACB...):  $V_2$
  - » Zero phase sequence (A=B=C),  $V_0$
  - » All RMS phasors
  - » Per phase analysis

# Per Phase Symmetrical Component Equations

$$a = 1 @ 120^\circ$$

$$V_{A_G} = V_{A0} + V_{A1} + V_{A2}$$

- phase A ref

$$V_{B_G} = V_{B0} + V_{B1} + V_{B2}$$

$$= V_{A0} + a^2 V_{A1} + a V_{A2}$$

- phase B ref

$$V_{C_G} = V_{C0} + V_{C1} + V_{C2}$$

$$= V_{A0} + a V_{A1} + a^2 V_{A2}$$

← phase C ref  
consequence

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<h1>Basic Sequence Networks</h1>		<small>ECE525 Lecture 15</small>
<ul style="list-style-type: none"><li>• Impedance will differ between sequences</li><li>• Zero sequence will also include ground impedance</li><li>• Connect them as appropriate for different fault types</li></ul>		
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<h1>Fault Analysis</h1>		<small>ECE525 Lecture 15</small>
<ul style="list-style-type: none"><li>• Fault Types:<ul style="list-style-type: none"><li>» Single line to ground</li><li>» Line to line</li><li>» Double line to ground</li><li>» Three phase (positive sequence unless unbalanced fault impedances)</li><li>» Phase open — 1 or 2 <math>\frac{1}{3}</math> series imbalance</li><li>» Phase open and line to ground</li><li>» Simultaneous faults</li></ul></li></ul>		
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Shunt fault  
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# Fault Detection For Protection Purposes

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setting [

- Basic fault analysis techniques calculate currents/voltages at fault location
  - » ABC or symmetrical components
- Need fault signature as seen at the relay location
  - » Rough location of fault for correct response

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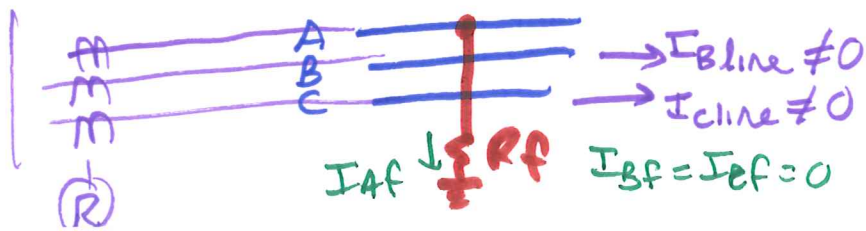
# Single Line to Ground Connections

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- Constraints at fault location (phase A):
  - »  $V_A = 0$  (If  $R_f = 0$ ,  $V_f = I_f \cdot R_f$ )
  - »  $I_B = I_C = 0$
- Therefore:
  - ① »  $V_A = V_0 + V_1 + V_2 = 0$  - phase A ref
  - »  $I_0 = (I_A + 0 + 0)/3$  and
  - »  $I_1 = I_2 = (I_A + 0 + 0)/3$  so
  - ② »  $I_0 = I_1 = I_2 = (I_A)/3$

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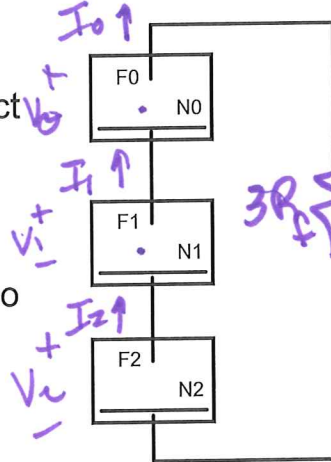




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# SLG Connections

- To Satisfy these constraints we connect the three networks in series
- Connect reference point of one network to fault location of next one



$$V_0 + V_1 + V_2 = I_A R_f$$

$$3 I_0 \cdot R_f$$

$$I_A R_f = 0$$

# SLG Faults

- Solve for  $I_0$ , can calculate  $I_A$
- Next solve for  $V_1$ ,  $V_2$ , and  $V_0$  and calculate phase voltage
- Note that in general  $jX_0$  will be replaced with  $Z_0 = jX_0 + 3Z_{gr} + 3Z_f$ 
  - » The factor of 3 results since 0 sequence is the same to all 3 phases

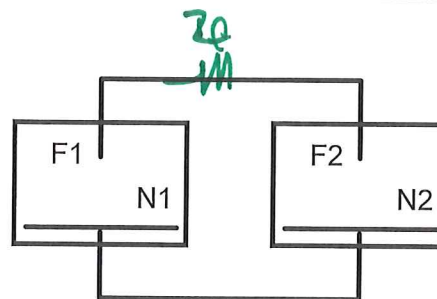
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# Phase to Phase Faults

- Two phases (often B and C for analysis) shorted together
  - » Not shorted to ground
  - »  $V_B = V_C$
  - »  $I_B = -I_C$
- From symmetrical component equations:
  - »  $I_0 = 0$
  - »  $I_1 = -I_2$  and  $V_1 = V_2$

# Phase to Phase Faults

- Fault impedance (if any) appears between the networks
- No Zero Sequence Network
- $V_B = I_B * Z_f + V_C$



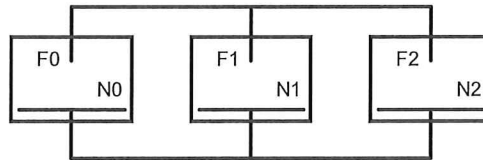
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## Double Line to Ground

- Two phases shorted together and to ground
- Could have several impedances
  - »  $I_A \cong 0$
  - »  $V_B = (Z_f + Z_{gr}) * I_B + Z_f * I_f$
  - »  $V_C = (Z_f + Z_{gr}) * I_C + Z_f * I_f$



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## Fault Detection For Protection Purposes

- Basic fault analysis techniques calculate currents/voltages at fault location
  - » ABC or symmetrical components
- Need fault signature as seen at the relay location
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measurements

$I_A$

$I_B$

$I_C$

$V_{AG}$

$V_{BG}$

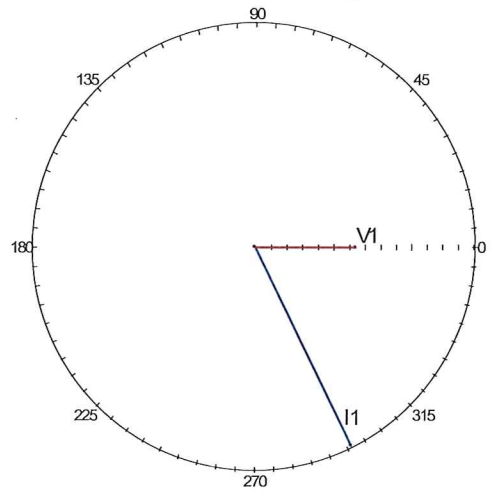
$V_{CG}$

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# A Symmetrical Component View of an Three-Phase Fault

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A-Ground Fault		
Component	Magnitude	Angle
Ia0	7.6	175
Ia1	2790	-64
Ia2	110	75.8
Va0	0	0
Va1	18.8	0

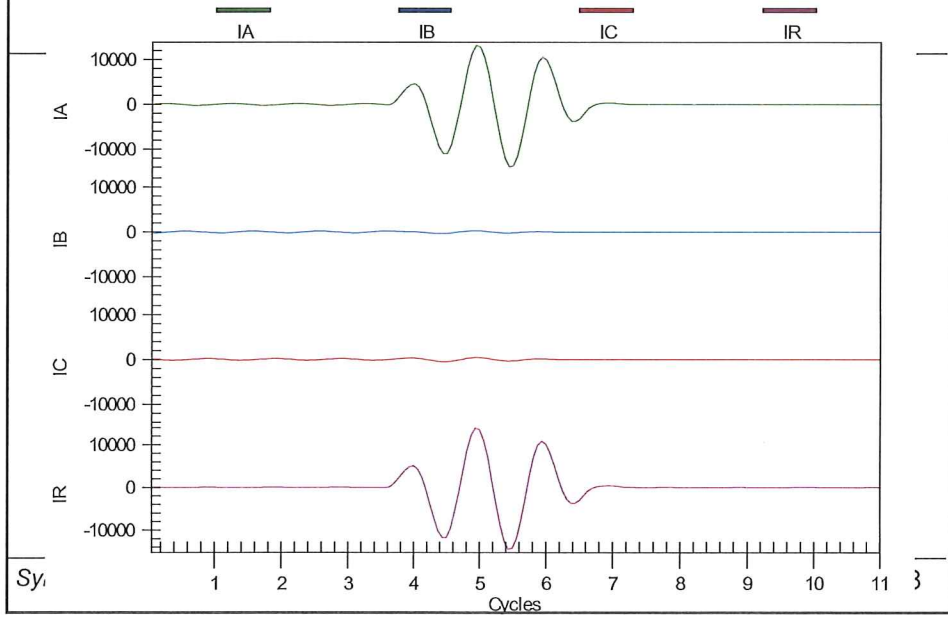


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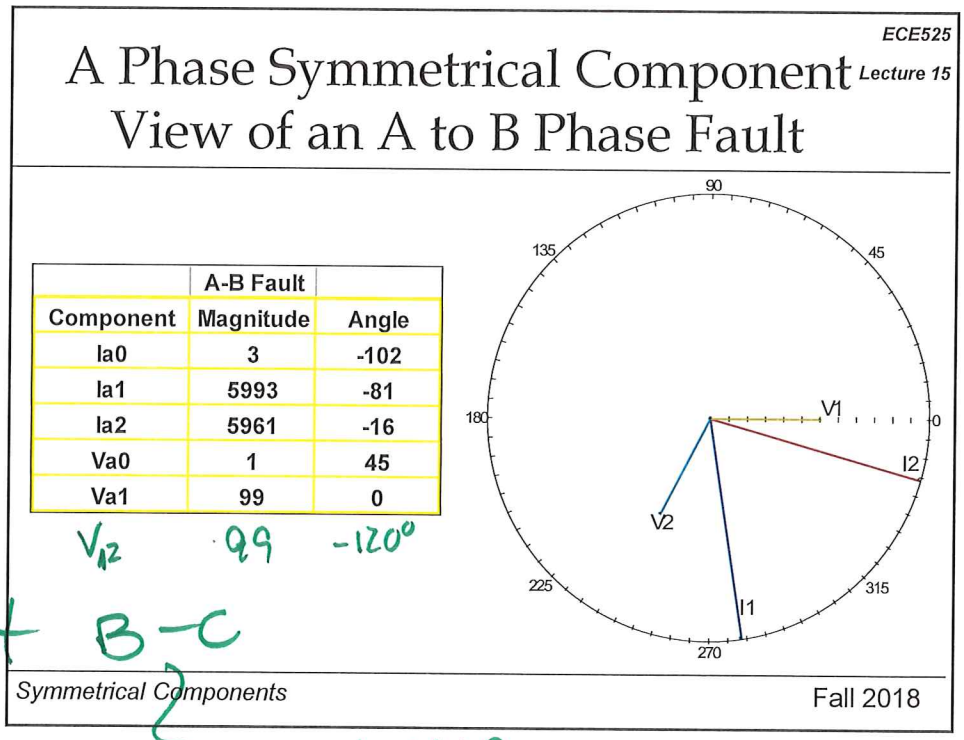
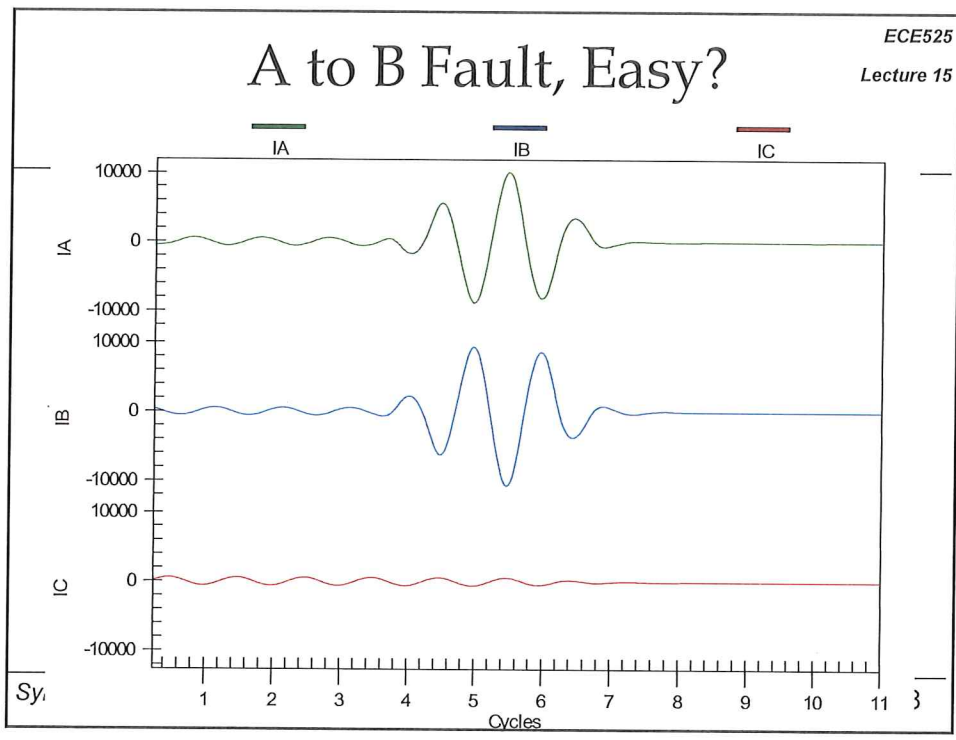
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# A to Ground Fault, Okay?

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not B-C

we can't use phase A ref