

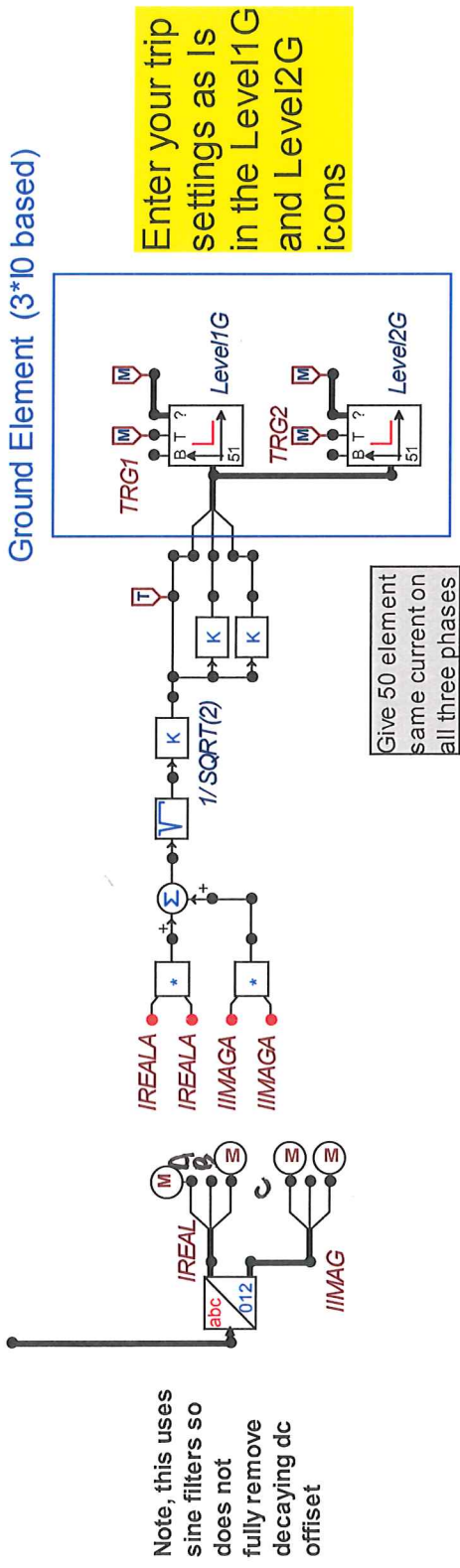
ECE 525

POWER SYSTEM PROTECTION  
AND RELAYING

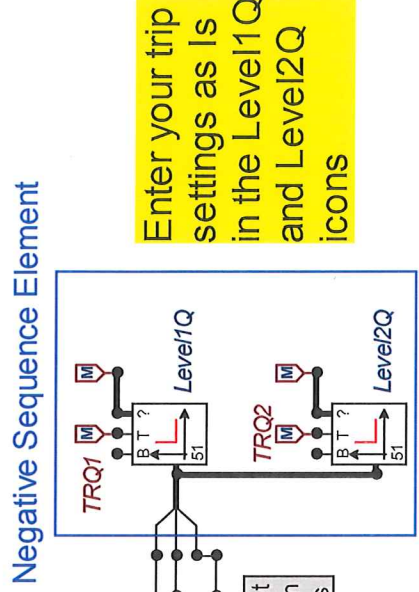
SESSION no. 21

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- Negative Sequence and Ground Elements



A = zero sequence,  
B = positive sequence,  
C = negative sequence



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[coupled\_3lines] mutually coupled 3 wires

Sequence Components

|                              |              |
|------------------------------|--------------|
| Positive Sequence Resistance | 0.8 [ohm]    |
| Positive Sequence Inductance | 0.021221 [H] |
| Zero Sequence Resistance     | 2.4 [ohm]    |
| Zero Sequence Inductance     | 0.063662 [H] |

OK Cancel Help...

[faultn] Timed Fault Logic

Configuration

|                     |          |
|---------------------|----------|
| Time to Apply Fault | 0.2 [s]  |
| Duration of Fault   | 0.05 [s] |

OK Cancel Help...

[fft] On-Line Frequency Scanner

Configuration

|                                  |             |
|----------------------------------|-------------|
| Type                             | 1 Phase     |
| Number of Harmonics              | n=7         |
| Base frequency                   | 60.0 [Hz]   |
| Magnitude Output                 | RMS         |
| Phase Output Units               | Radians     |
| Phase Output reference           | Cosine wave |
| Anti-aliasing filter?            | yes         |
| Frequency tracking?              | no          |
| Frequency Tracking Enable Signal | 1           |

OK Cancel Help...

4A (over A) (over B)

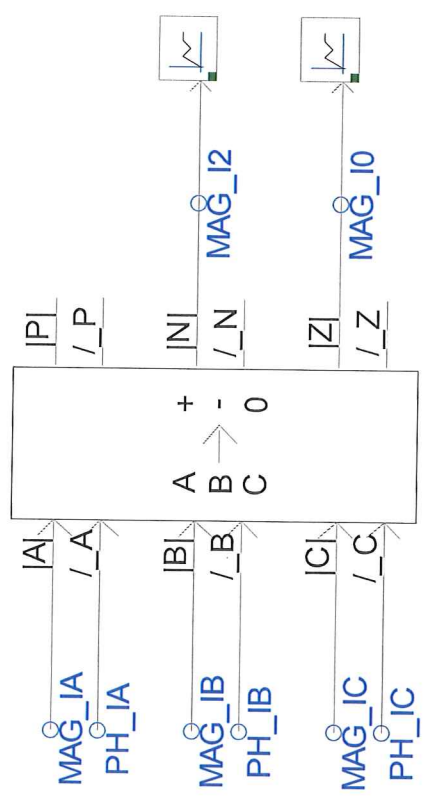
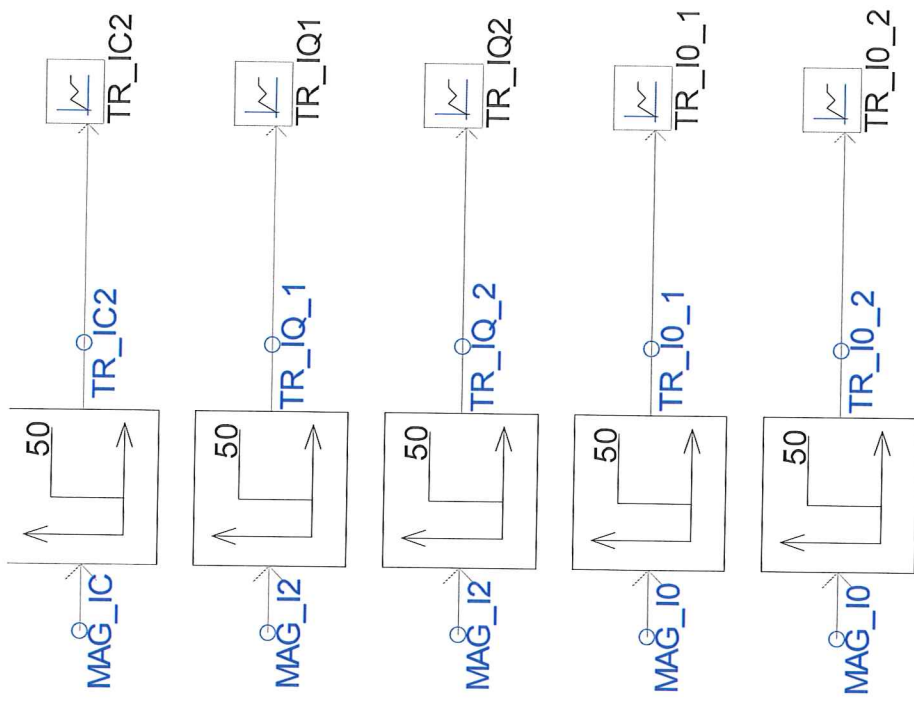
[over\_current] Over current detection block

Configuration

|                         |           |
|-------------------------|-----------|
| Over Current Limit      | 0.004     |
| Preprocessing ?         | None      |
| Smoothing Time Constant | 0.02 [s]  |
| Frequency               | 60.0 [Hz] |
| Delay Time              | 0.0 [s]   |

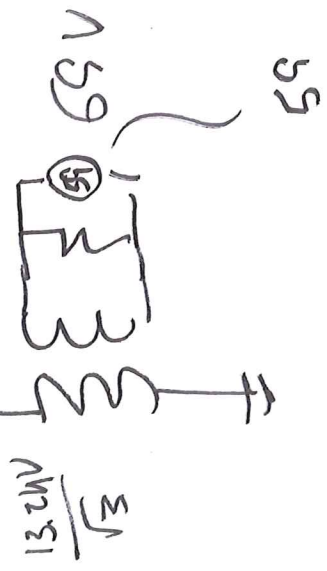
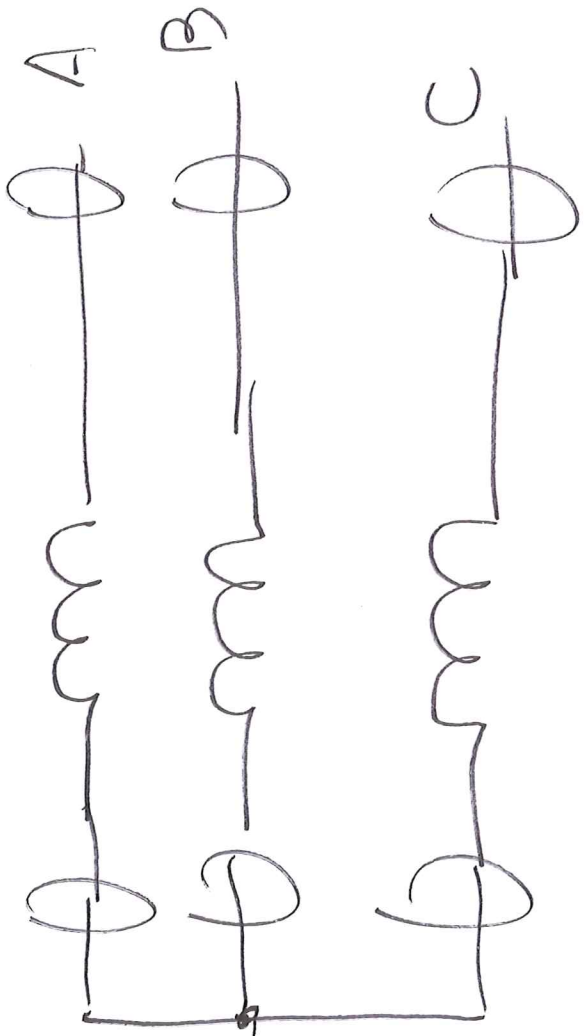
OK Cancel Help...

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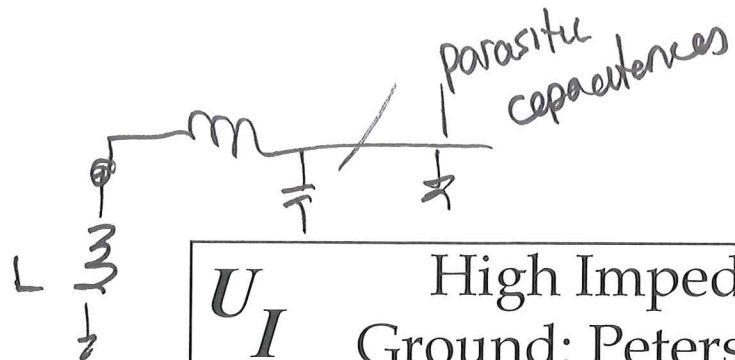
These use I0,  
not 3\*I0

13.2kV





L/S  
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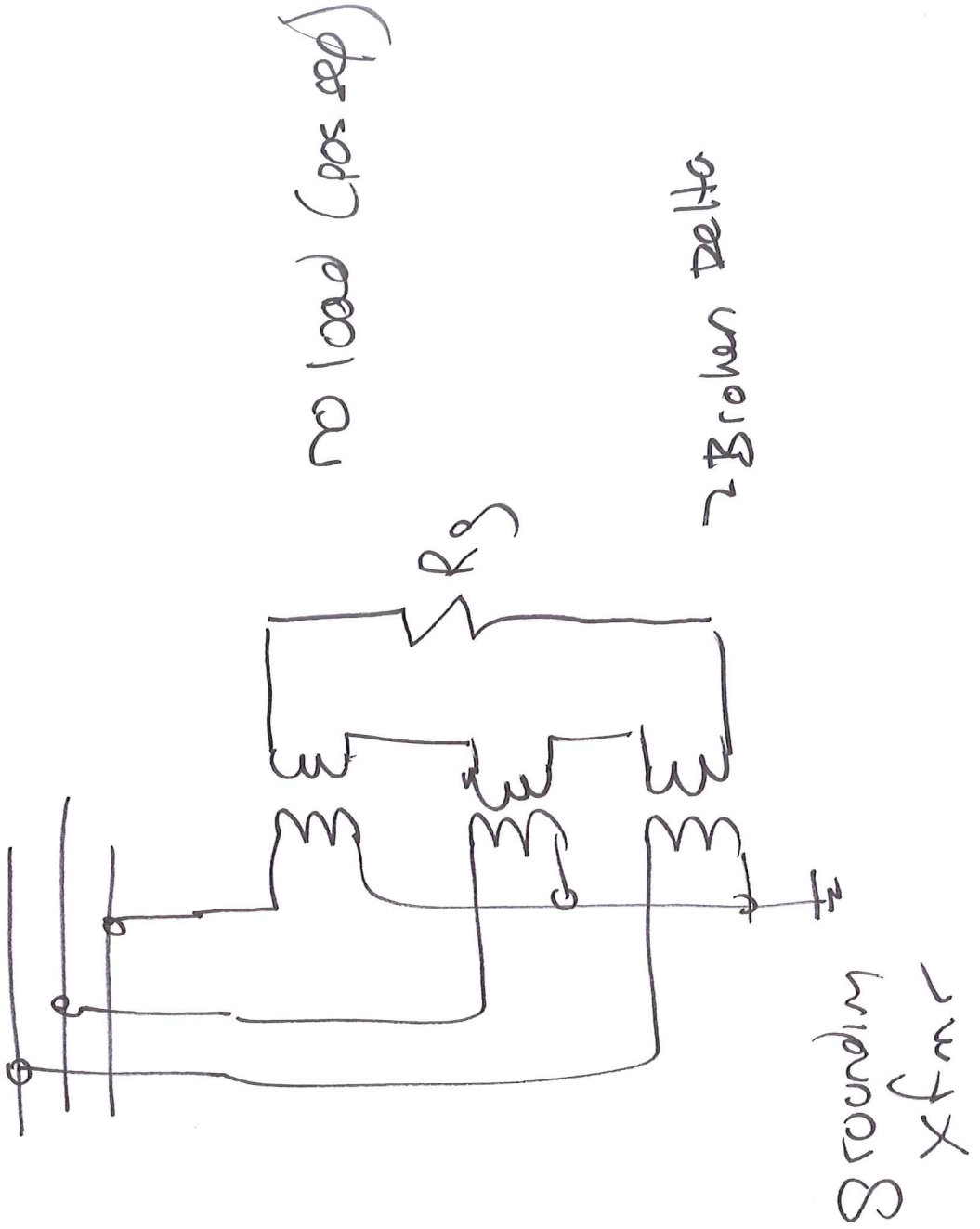
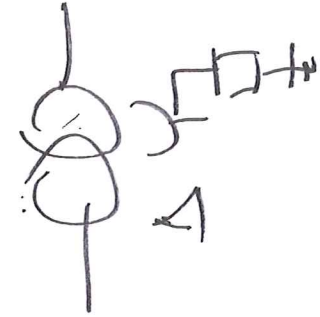
**U**  
**I** High Impedance Ground: Peterson Coil ECE525  
Lecture 19

- Normal unbalanced operation on distribution line poses problems
- Still need line to line rating on insulation
  - Ground fault neutralizer
  - Resonant ground

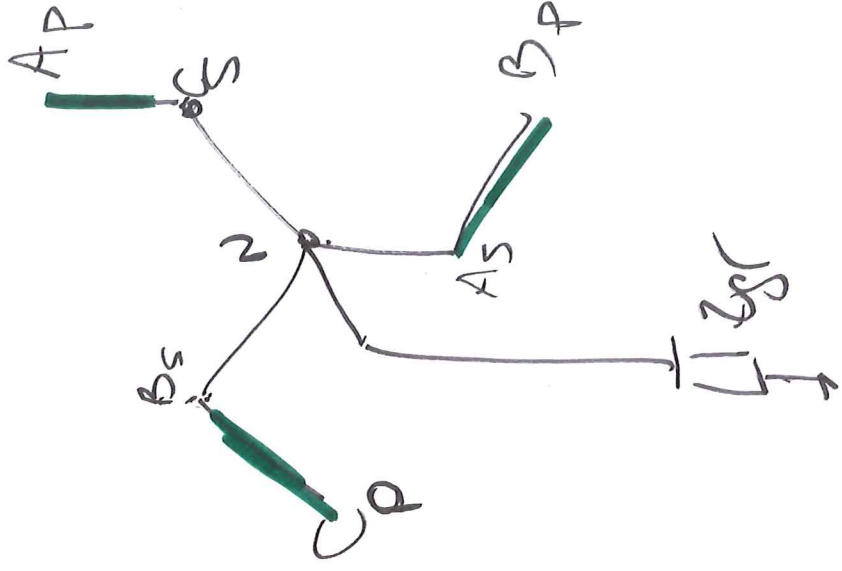
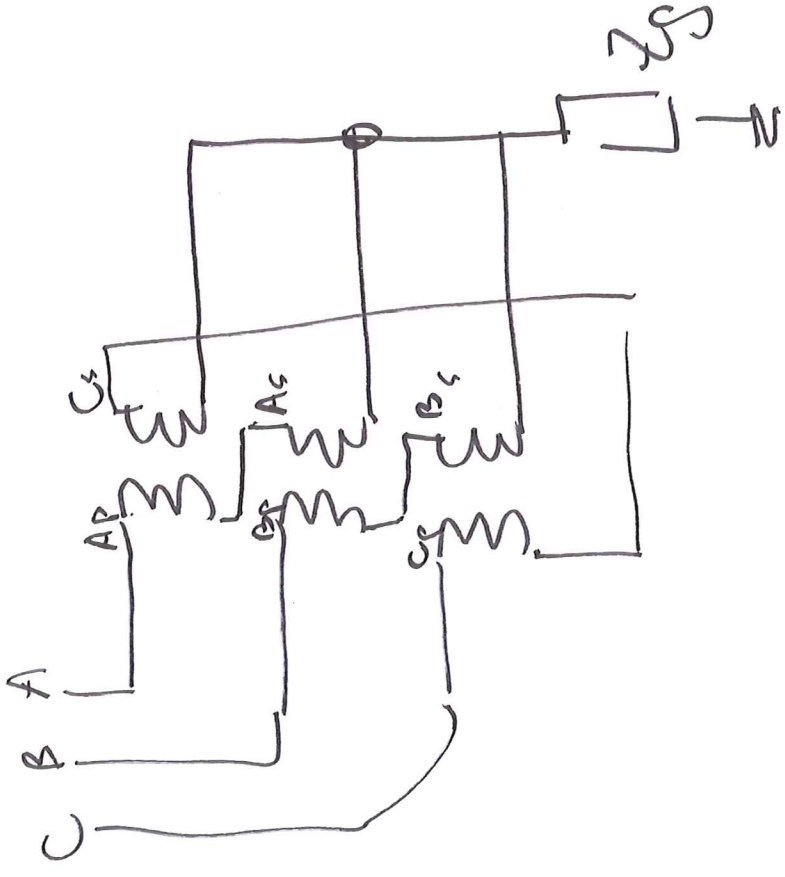
**U**  
**I** Impedance Ground ECE525  
Lecture 19

- Resistance Ground
    - » High R: ( $I_f < 10 \text{ A}$ )
    - » Low R: ( $10 \text{ A} < I_f < 1000 \text{ A}$ )
  - Inductive Ground
    - » Zig-zag transformer
    - » Poor performance in general
  - Resonant Ground (ground fault neutralizer)
- } large inductance

Low impedance ground configs



# Zig Zag transformer





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**U**  
**I** Low Impedance Ground: ECE525  
Lecture 19

- Limit fault current to 50-600 A  $\sim 1000A$
- Current sensing used for relaying and can do direction sensing
- Limit over voltages nearly as well as effective ground
- Sometimes use zig-zag transformer with resistor on neutral (if no R, then magnetizing branch is ground path)



**U**  
**I** Solid Effective Grounding ECE525  
Lecture 19

- Most popular in North America
- $X_0/X_1 \leq 3$  and  $R_0/X_1 \leq 1$  and are positive
- Uni-grounded (Europe) versus multi-grounded (U.S.)
- Best for detecting faults, sensing direction, and fault locating



## Grounding Examples

$$a := 1 \cdot e^{j \cdot 120 \text{deg}} \quad A_{012} := \begin{pmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{pmatrix} \quad \text{MVA} := 1000 \text{kW} \quad \text{pu} := 1$$

A 4160 V feeder is supplied by the WYE connected side of a 75 MVA transformer. The system  $\text{MVA}_{sc}$  supplying the delta side of the transformer is 650 MVA. The transformer has a leakage reactance of 10%. A ground impedance will be connected in the neutral of 4.16kV side of the transformer to limit fault currents.

A Sketch the per unit diagram for the system

$$\text{MVA}_{base} := 100 \text{MVA}$$

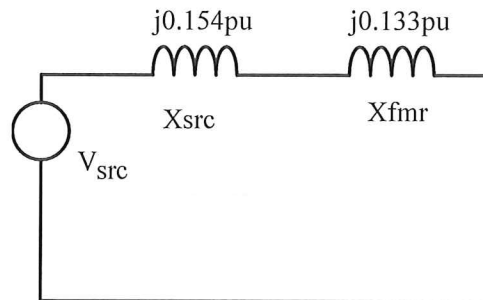
$$\text{S}_{rated} := 75 \text{MVA} \quad V_{LL} := 4.16 \text{kV} \quad V_{ln} := \frac{V_{LL}}{\sqrt{3}} \quad V_{ln} = 2.402 \cdot \text{kV}$$

$$\text{MVA}_{sc} := 650 \text{MVA}$$

$$X_{src\_pu} := \frac{1.0^2}{\left(\frac{\text{MVA}_{sc}}{\text{MVA}_{base}}\right)} \quad X_{src\_pu} = 0.154 \cdot \text{pu}$$

$$X_{xfmr} := 0.1 \cdot \left(\frac{4160 \text{V}}{4160 \text{V}}\right)^2 \cdot \left(\frac{\text{MVA}_{base}}{\text{S}_{rated}}\right)$$

$$X_{xfmr} = 0.133 \cdot \text{pu}$$



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$$X_{gndpu} := \text{Im}(Z_{gnd})$$

$$X_{gndpu} = 2.077 \text{ per unit}$$

$$X_{gnd} := X_{gndpu} \cdot Z_{base}$$

$$X_{gnd} = 0.359 \Omega$$

$$L_{gnd} := \frac{X_{gnd}}{2 \cdot \pi \cdot 60\text{Hz}}$$

$$L_{gnd} = 0.954 \cdot \text{mH at } 60\text{Hz}$$

D If the feeder is largely underground, the capacitance cannot be neglected. If the total per phase capacitance to ground is  $1.5 \mu\text{F}$ , determine the grounding resistance needed to limit the single line to ground fault current to 20 A.

$$C_{parasitic} := 1.5 \mu\text{F}$$

$$X_c := \frac{1}{2 \cdot \pi \cdot 60\text{Hz} \cdot C_{parasitic}}$$

$$X_c = 1.768 \cdot \text{k}\Omega$$

$$X_{c\_pu} := \frac{X_c}{Z_{base}}$$

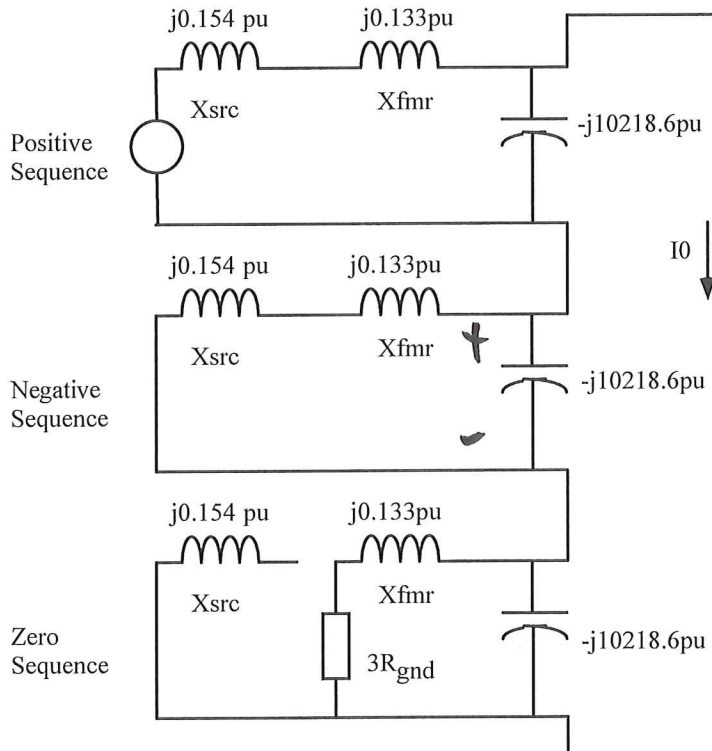
$$X_{c\_pu} = 10218.6 \cdot \text{pu}$$

$$I_{slg\_max} := 20\text{A}$$

$$I_{slgpu} := \frac{I_{slg\_max}}{I_{base}}$$

$$I_{slgpu} = 1.441 \times 10^{-3} \cdot \text{pu}$$

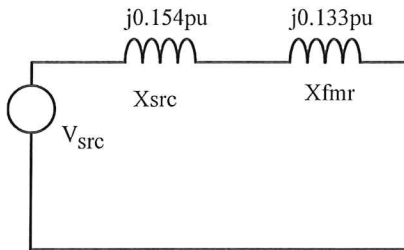
The sequence networks will now change with the addition of the capacitance as shown.



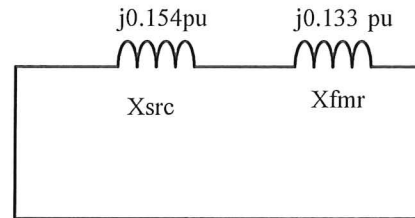
Alternate selection  
for  $R_{gnd}$   
 $\rightarrow$  IF Capacitance  
is known  
 $3R_{gr} = X_{c0}$   
 $\rightarrow$  limits SLG  
current to  
 $\sim$  charging current

**B** Determine sequence networks for the system

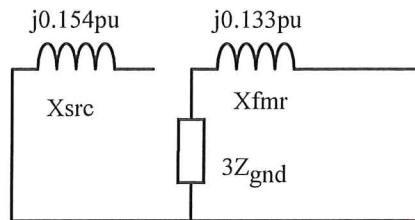
Positive Sequence:



Negative Sequence:



Zero Sequence:



Note that this is a  $\Delta$ -Y grounded transformer. Also, assuming that zero sequence leakage impedance equal to positive and negative sequence values.

**C** Assume that the feeder is all overhead lines with negligible capacitance. Determine the ground *reactance* needed to limit the single line to ground fault current to 6000A.

$$I_{f\_slgmax} := 6000A$$

$$I_{base} := \frac{MVA\_base}{\sqrt{3} \cdot V\_LL}$$

$$I_{base} = 13.88 \cdot kA$$

$$Z_{base} := \frac{V\_LL^2}{MVA\_base}$$

$$I_{fpu} := \frac{I_{f\_slgmax}}{I_{base}}$$

$$I_{fpu} = 0.432 \cdot pu$$

For a SLG fault we have (connect positive, negative and zero sequence circuits in series):

$$I_0 = \frac{V_{fault}}{Z_1 + Z_2 + Z_0 + 3 \cdot jX_{gnd}}$$

where  $V_{fault} := 1.0 \cdot e^{j \cdot 90deg}$

$$Z_1 := jX_{src\_pu} + jX_{xfmr} \quad Z_2 := Z_1$$

$$Z_0 := jX_{xfmr}$$

and we know for a SLG fault:  $I_0 := \frac{I_{fpu}}{3}$

Solve for  $Z_{gnd}$

$$Z_{gnd} := \frac{1}{3} \left[ \frac{V_{fault}}{I_0} - (Z_1 + Z_2 + Z_0) \right]$$

$$Z_{gnd} = 2.0772i \quad \text{per unit}$$

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E Calculate the line to ground voltages on the unfaulted phases in parts C and D and calculate the zero sequence voltages and currents.

**Part C:**

$$I0\_partC := \frac{V_{fault}}{Z0 + 3 \cdot jX_{gndpu} + Z1 + Z2}$$

$$I0\_partC = 0.144$$

$$I1\_partC := I0\_partC$$

$$I2\_partC := I0\_partC$$

as a check:  $Ia\_partC := 3 \cdot I0\_partC$

$$|Ia\_partC| = 0.432 \text{ pu}$$

$$|Ia\_partC| \cdot I_{base} = 6 \text{ kA}$$

$$V1\_partC := V_{fault} - I1\_partC \cdot Z1$$

$$V1\_partC = 0.959i$$

$$V2\_partC := -I2\_partC \cdot Z2$$

$$V2\_partC = -0.041i$$

$$V0\_partC := -I0\_partC \cdot (Z0 + 3 \cdot jX_{gndpu})$$

$$V0\_partC = -0.917i$$

$$Vabc\_partC := A_{012} \cdot \begin{pmatrix} V0\_partC \\ V1\_partC \\ V2\_partC \end{pmatrix}$$

$$Vabc\_partC = \begin{pmatrix} 0 \\ 0.866 - 1.376i \\ -0.866 - 1.376i \end{pmatrix}$$

at fault point

$$|Vabc\_partC| = \begin{pmatrix} 0 \\ 1.626 \\ 1.626 \end{pmatrix}$$

$$\arg(Vabc\_partC) = \begin{pmatrix} 90 \\ -57.812 \\ -122.188 \end{pmatrix} \cdot \text{deg}$$

$$V_{ln} \cdot |Vabc\_partC| = \begin{pmatrix} 0 \\ 3.905 \\ 3.905 \end{pmatrix} \cdot \text{kV}$$

overvoltage on unfaulted phase

**Part D:**

$$Z_{gndD} := \frac{(3 \cdot R_{gnd\_pu} + Z0) \cdot (-j \cdot Xc\_pu)}{(3 \cdot R_{gnd\_pu} + Z0) - j \cdot Xc\_pu}$$

$$I0\_partD := \frac{V_{fault}}{Z_{gndD} + Z1 + Z2}$$

$$I0\_partD = -9.771 \times 10^{-5} + 4.703i \times 10^{-4}$$

$$I1\_partD := I0\_partD$$

$$I2\_partD := I0\_partD$$

$$|I0\_partD| = 4.804 \times 10^{-4}$$



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as a check:  $I_{a\_partD} := 3 \cdot I_{0\_partD}$       $|I_{a\_partD}| = 1.441 \times 10^{-3}$  pu  
 $|I_{a\_partD}| \cdot I_{base} = 20.001 \cdot A$

$V_{1\_partD} := V_{fault} - I_{1\_partD} \cdot Z_1$

$|V_{1\_partD}| = 1$

$V_{2\_partD} := -I_{2\_partD} \cdot Z_2$

$|V_{2\_partD}| = 1.38 \times 10^{-4}$

$V_{0\_partD} := -I_{0\_partD} \cdot (Z_{gndD})$

$|V_{0\_partD}| = 1$

$V_1 = 1$   
 $V_1 + V_2 + V_0 = 0$   
 $V_0 = -1$

$V_{abc\_partD} := A_{012} \begin{pmatrix} V_{0\_partD} \\ V_{1\_partD} \\ V_{2\_partD} \end{pmatrix}$

$V_{abc\_partD} = \begin{pmatrix} 0 \\ 0.866 - 1.5i \\ -0.866 - 1.5i \end{pmatrix}$

$|V_{abc\_partD}| = \begin{pmatrix} 0 \\ 1.732 \\ 1.732 \end{pmatrix}$

$\arg(V_{abc\_partD}) = \begin{pmatrix} 107.593 \\ -60.013 \\ -120.01 \end{pmatrix} \cdot \text{deg}$

at fault point

$V_{ln} \cdot |V_{abc\_partD}| = \begin{pmatrix} 0 \\ 4.16 \\ 4.161 \end{pmatrix} \cdot \text{kV}$

F Compute the single line to ground fault current and the voltage on the unfaulted phases if the transformer is solidly grounded. Calculate the zero sequence voltages and currents.

$I_{0\_gnd} := \frac{V_{fault}}{Z_0 + Z_1 + Z_2}$

$I_{0\_gnd} = 1.413$

$I_{1\_gnd} := I_{0\_gnd}$

$I_{2\_gnd} := I_{0\_gnd}$

$I_{a\_gnd} := 3 \cdot I_{0\_gnd}$

$I_{a\_gnd} = 4.239$  per unit

$I_{a\_gnd} \cdot I_{base} = 58.833 \cdot \text{kA}$

$V_{1\_gnd} := V_{fault} - I_{1\_gnd} \cdot Z_1$

$V_{1\_gnd} = 0.594i$

$V_{2\_gnd} := -I_{2\_gnd} \cdot Z_2$

$V_{2\_gnd} = -0.406i$

$V_{0\_gnd} := -I_{0\_gnd} \cdot Z_0$

$V_{0\_gnd} = -0.18841i$



Fault Detection & Direction Determination  
as impacted by Grounding

(1) Solidly grounded:

Detection: overcurrent protection

→ phase elements

→ ground elements

- negative sequence elements

⇒  $I_{\text{fault}}$  typically much larger than  
load current (can use phase  
elements)

# Direction Sensing:

→ voltage + current

→ Torque elements

- phase quantities
- negative sequence
- positive sequence

## ② Low impedance grounded

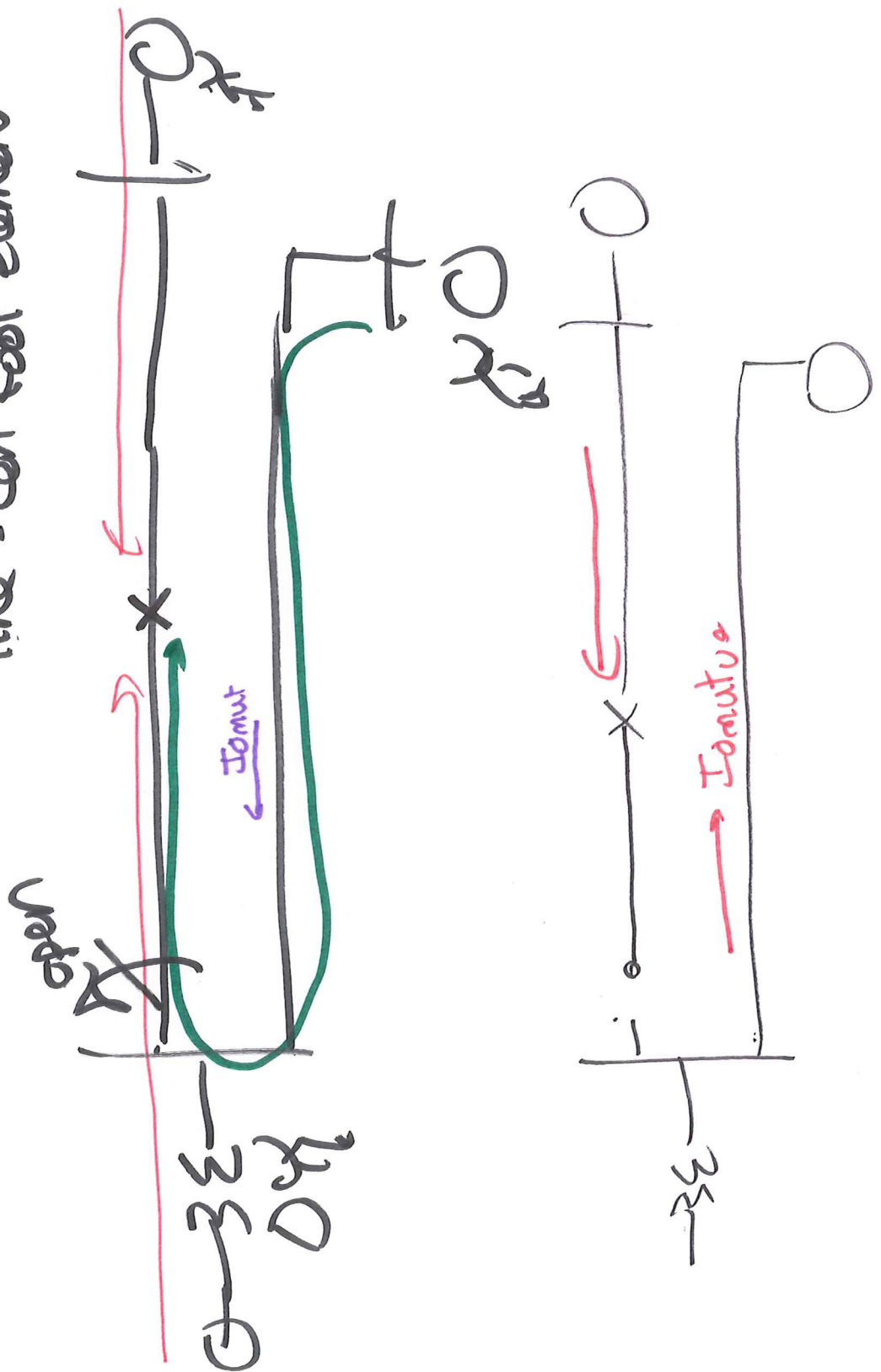
Detection:

— SLG : Limits  $I_0$  - can still use overcurrent elements  
 → ground overcurrent

— DLG, 3φ, LL : overcurrent  
 as above

Direction - largely same as above, zero seq directional

- Cauter with zero sep direction  
 → mutual coupling to parallel  
 line - can fool element



# High Resistance Grounded

## Fault Detection

SLG:  $V_{ng} = 3V_0$  → also for ungrounded

LL, DLG, 3 $\phi$ : overcurrent

—same as earlier

Direction determination — same as earlier