

ECE 525

POWER SYSTEM PROTECTION  
AND RELAYING

SESSION no. 8

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Simple Digital Filter Calculation

RS := 16

$$LPW := \text{floor}\left(\frac{2}{60 \cdot \Delta t \cdot RS}\right)$$

$$LP(a) := \left(1 + \frac{1}{RS}\right) \cdot \sum_{k=0}^{LPW-1} \frac{I_{a-LPW+k}}{LPW}$$

ii := LPW .. ceil  $\left(\frac{CY}{f \cdot \Delta t}\right)$

I<sub>ii</sub> := LP(ii)

# cycles

S<sub>max</sub> := CY · RS

S<sub>min</sub> := 2 .. S

I<sub>a\_s</sub> := linterp  $\left(t, I, \frac{s}{RS \cdot 60}\right)$

if := (RS - 1) .. S

$$IF_{if} := \frac{2}{RS} \cdot \sum_{k=0}^{RS-1} \left[ \cos\left(k \cdot \frac{2 \cdot \pi}{RS}\right) \cdot I_{a_{[if-(RS-1)]+k}} \right]$$

iv := (RS + 1) .. S

I<sub>cp<sub>x</sub></sub> := IF<sub>iv</sub> + j · IF<sub>iv</sub> ·  $\frac{RS}{4}$

cosine output by 90°

Enter the number of samples per cycle of the relay

Calculate the number of samples to create an averaging LP filter with at cutoff frequency at 1/2 the sampling frequency.

Averaging Filter

Calculate filtered current

Calculate the number of relay samples available in the data and create an index "s" as a row pointer

Create a vector "Ia" representing the relay's sampled values

Create a filter index, "if" and apply a full cycle cosine filter, "IF" to vector "Ia"

digital cosine filter  
Cosine Filter

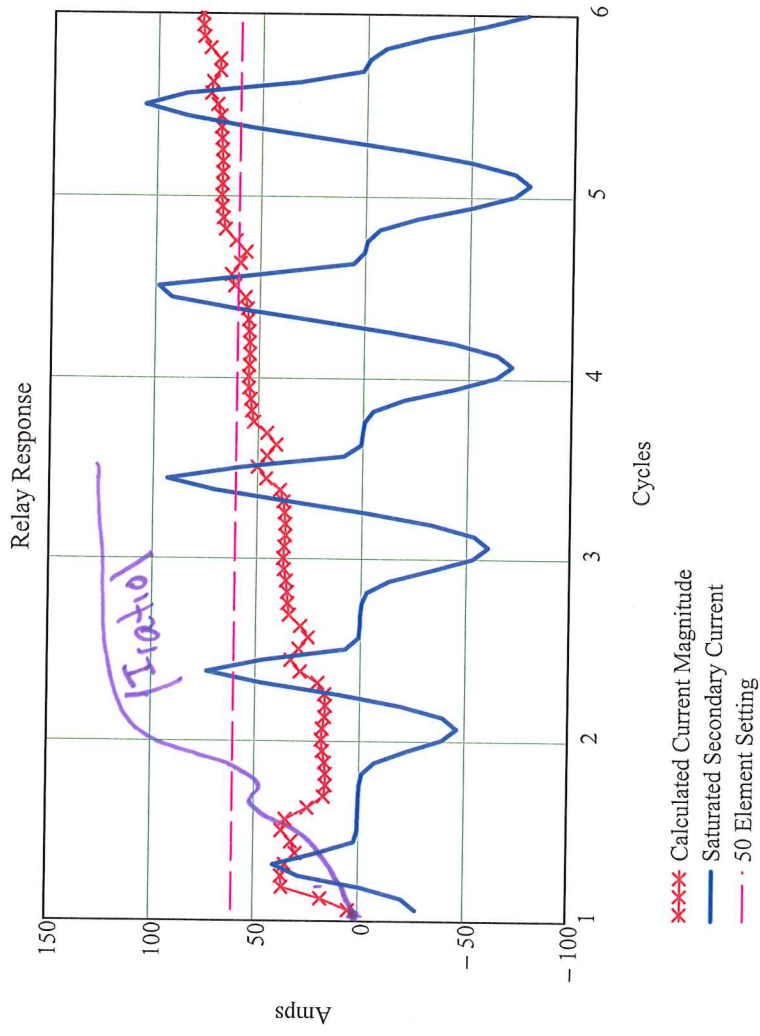


Create a vector index, "iv" and form a complex vector, "Icp<sub>x</sub>" from filtered quantities at 90 degree intervals

I<sub>phasor</sub> = COSINE + j SINE

output of cosine filter

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### ECE 525: Lecture 6

ORIGIN := 1

CT Data: C600 class, 1200/5

Full ratio:  $N_{full} := \frac{1200}{5}$

$N_{full} = 240$

CT Excitation Curve

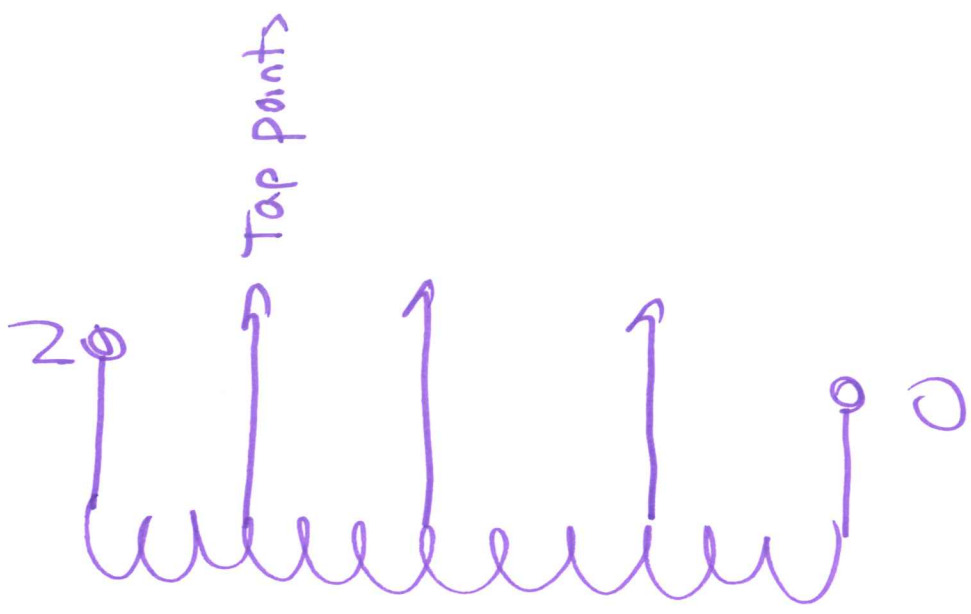
$I_m$	0.001	0.09
	.04	90
	.1	428
	.12	520
	.14	600
	.2	700
	.3	780
	.4	800
	40	927

excitation :=

TAPS

240
200
180
160
120
100
80
60
40
20

t :=



$$v_t(N2) := \left( \frac{N2}{t_1} \right) \cdot \text{excitation}^{(2)}$$

$t_1$  ~ 1st point in vector t

$$Im_t(N2) := \left( \frac{t_1}{N2} \right) \cdot \text{excitation}^{(1)}$$

turn := 1

$$R_{turn} := 0.0024 \frac{\text{ohm}}{\text{turn}}$$

Full winding:  $R_{secondary} := R_{turn} \cdot 240 \text{turn}$

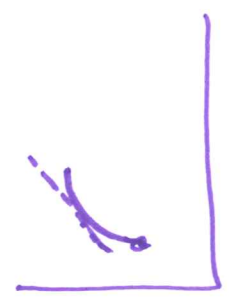
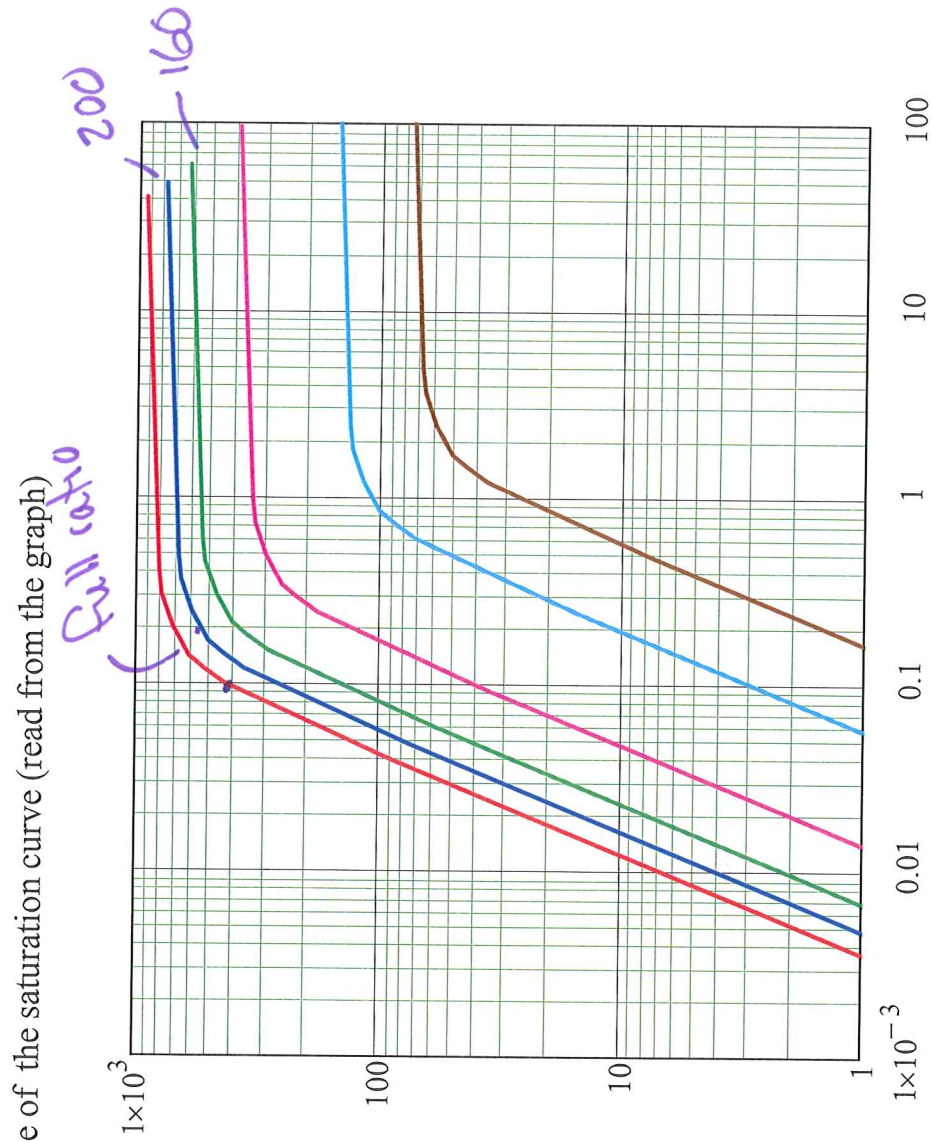
$R_{secondary} = 0.58 \Omega$

$V_{1200} := 428 \text{V}$  at the bottom of the knee of the saturation curve (read from the graph)

$$V_{per\_turn} := \frac{V_{1200}}{240 \text{turn}}$$

$$V_{per\_turn} = 1.783 \text{V}$$

- Notice that the knee is at 600V for full tap



$Im_t(t_1), Im_t(t_2), Im_t(t_4), Im_t(t_6), Im_t(t_9), Im_t(t_{10})$   
magnetizing currents

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## ECE 525: Lecture 8

- For C-class current transformers, the CT is rated such that the error in the secondary current
  - will be less than 10% if the 20 times rated current flows through a standard burden.
- This should be adjusted to account for the effect of the decaying offset.
- So the equation to never saturate is:

$$R_{\text{totalburden\_pu}} \cdot I_{f\_pu} \cdot \left( 1 + \frac{X_{\text{system}}}{R_{\text{system}}} \right) < 20$$

Assuming that the inductance in the CT secondary windings, lead wire and relay can be neglected, the voltage across the CT equivalent circuit magnetizing branch is:

$$v_m(t) = i_{\text{secondary}}(t) \cdot (R_{ct} + R_b) \quad \text{where:} \quad R_b = R_{\text{lead}} + R_{\text{relay}}$$

We want to get a measure of how long it takes the CT to saturate if it not sized to meet the above equation.

Equation for current with the DC offset:

$$i_{\text{secondary}}(t) = I_{f_{\text{max\_sec}}} \cdot \left( e^{\frac{-t}{T_p}} - \cos(\omega \cdot t) \right)$$

- Assumes fault timing for worst DC offset.

The paper: Juergen Holbach, "Modern Solutions to Stabilize Numerical Differential Relays for Current Transformer Saturation during External Faults", *2006 Power Systems Conference: Advanced Metering, Protection, Control, Communication, and Distributed Resources*, gives the following three equations for estimating the time to saturation for a CT:

The notes included several equations that could be used to describe what the author called " $V_{\text{knee}}$ ".

$$v_{\text{sat1}}(t_s) = I_{f_{\text{max\_sec}}} \cdot R_b \cdot \left[ (-X_{\text{overR}}) \cdot \left( e^{\frac{-t_s}{T_p}} - 1 \right) + 1 \right]$$

*not per unit*

Saturation free > 12 ms

$$\rightarrow v_{\text{sat2}}(t_s) = I_{f_{\text{max\_sec}}} \cdot R_b \cdot \left[ (-X_{\text{overR}}) \cdot \left( e^{\frac{-t_s}{T_p}} - 1 \right) - \sin(\omega \cdot t_s) \right]$$

Saturation free 7-12 ms

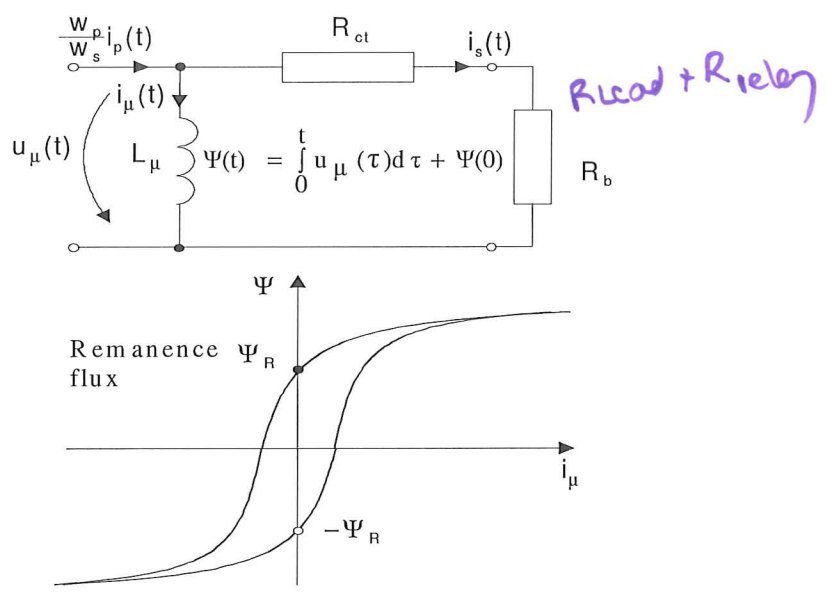
$$v_{\text{sat3}}(t_s) = I_{f_{\text{max\_sec}}} \cdot R_b \cdot (1 - \cos(\omega \cdot t_s))$$

Saturation free < 7ms

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# Current transformer equivalent circuit and magnetising characteristic

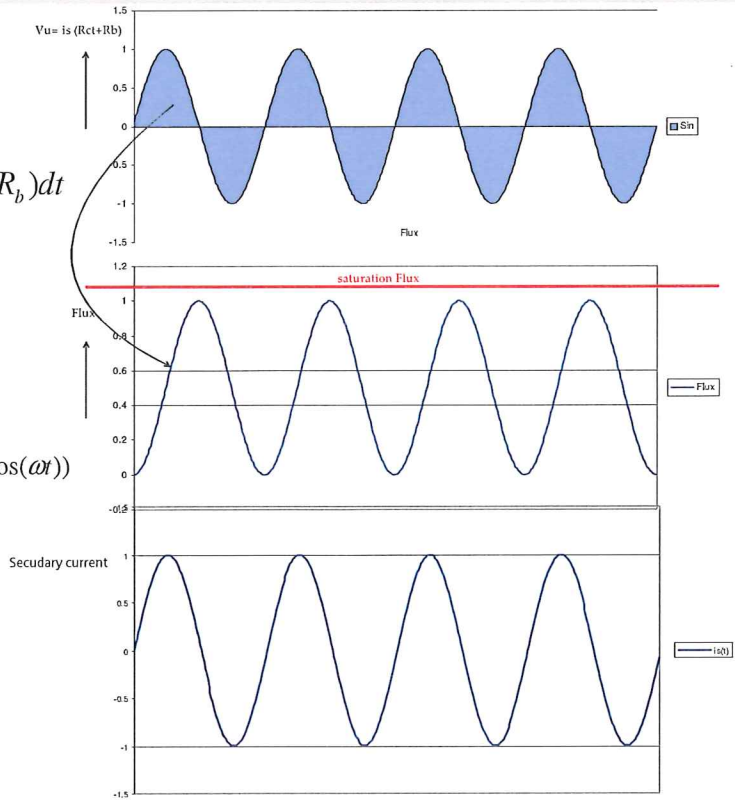


# Voltage and flux under unsaturated condition

$$\begin{aligned} Flux &= \int v_\mu(t) dt \\ &= \int i_s(t) \cdot (R_{CT} + R_b) dt \end{aligned}$$

for  $i_s(t) = I \sin(\omega t)$

$$Flux = \frac{I \cdot (R_{CT} + R_b)}{\omega} (1 - \cos(\omega t))$$



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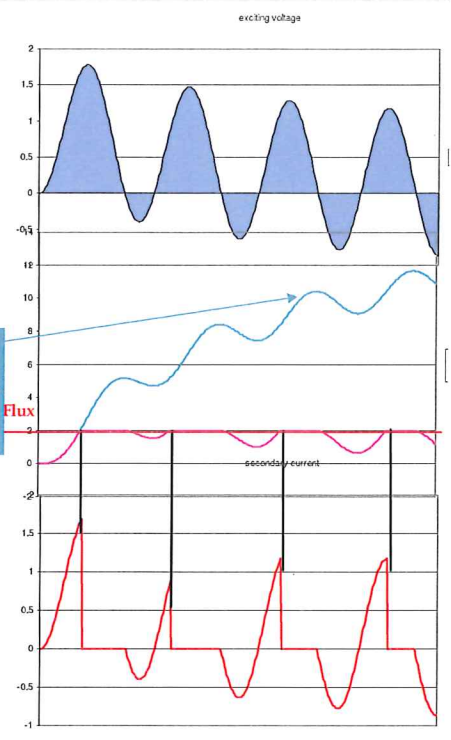
## DC-Offset

$$\begin{aligned} Flux &= \int v_{\mu}(t) dt \\ &= \int i_s(t) \cdot (R_{CT} + R_b) dt \\ i_s(t) &= I \left( e^{\frac{t}{T_p}} - \cos(\omega t) \right) \end{aligned}$$

$$V_{knee} = I(R_{CT} + R_b) \left\{ -\omega T_p \left[ e^{\frac{t}{T_p}} - 1 \right] - \sin(\omega t) \right\}$$

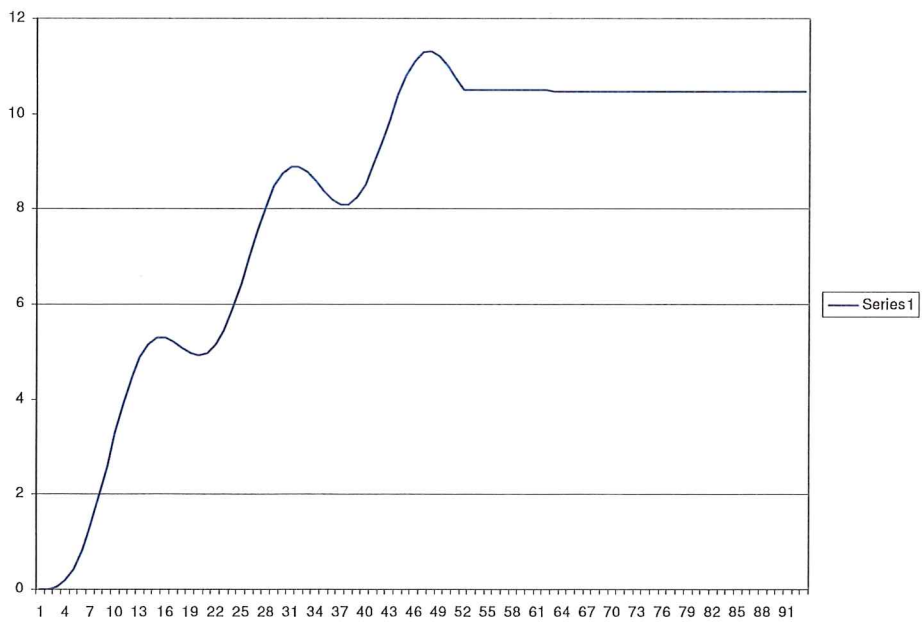
For no saturation at all : Set t=infinite and -sin(wt)=1

$$\begin{aligned} V_{knee} &= I(R_{CT} + R_b) \left[ 1 + \omega T_p \right] \text{ or} \\ V_{knee} &= I(R_{CT} + R_b) \left[ 1 + \frac{X}{R} \right] \end{aligned}$$



## Remanence

The flux inside the CT will not go to zero after the fault current is interrupted!





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## Considering remanence flux

$$K_{\text{Remanece}} = \frac{100}{100 - \text{Prozent of Remanence Percent}}$$

Example: Worst case of remanence (iron closed CT's) = 80%

$$K_{\text{Remanece}} = \frac{100}{100 - 80} = 5$$



## CT dimensioning for no saturation under all worst case condition

Example:  $I_{sc}=20000A$ , CT ratio = 1000/5,  $R_{CT}=0.5 \text{ Ohm}$ ,  $R_b=0.5 \text{ Ohm}$   
 $T_p=60ms$ , iron closed CT

1. considering DC offset

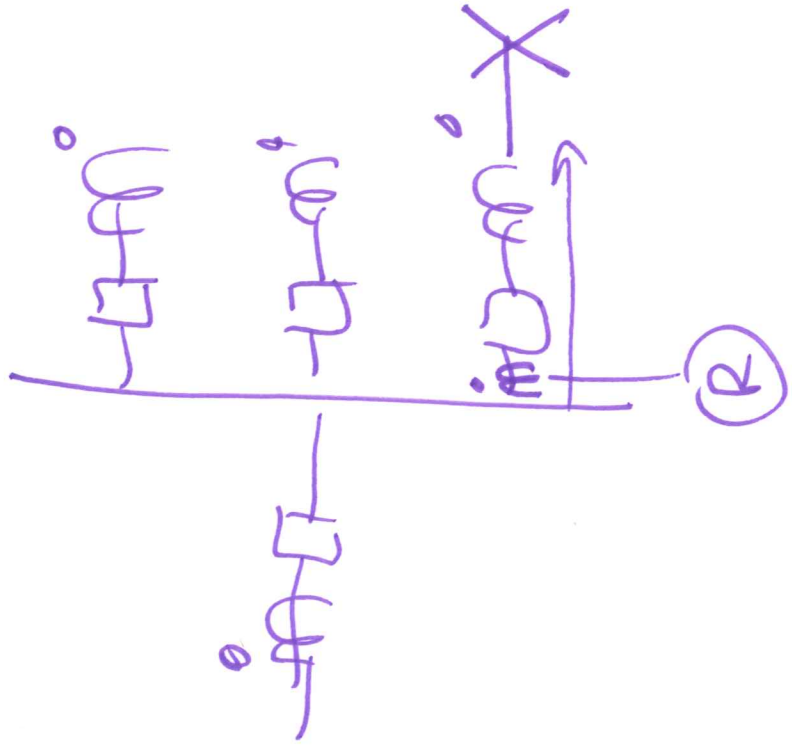
$$V_{knee} = I(R_{CT} + R_b) [1 + \omega T_p]$$

$$V_{knee} = 100A \cdot 10hm(1 + 22.6) = 2260V$$

2. considering 80% remanence

$$K_{\text{Remanece}} = \frac{100}{100 - 80} = 5 \quad \Rightarrow \quad V_{knee} = 5 \cdot 2260V = 11300V$$

The dimension of a CT that will not saturate for the maximum short circuit current that has a full DC offset with a long time constant and is at 80% in remanence, will lead to uneconomical and oversized CT's.



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## With consideration of saturation free time tsat

The requirement that no saturation is allowed will lead to uneconomical and oversized CT's

$$V_{knee} = I(R_{CT} + R_b) \left[ 1 + \frac{X}{R} \right]$$

Modern numerical relays only require a certain saturation free time tsat. The following formula takes this into consideration:

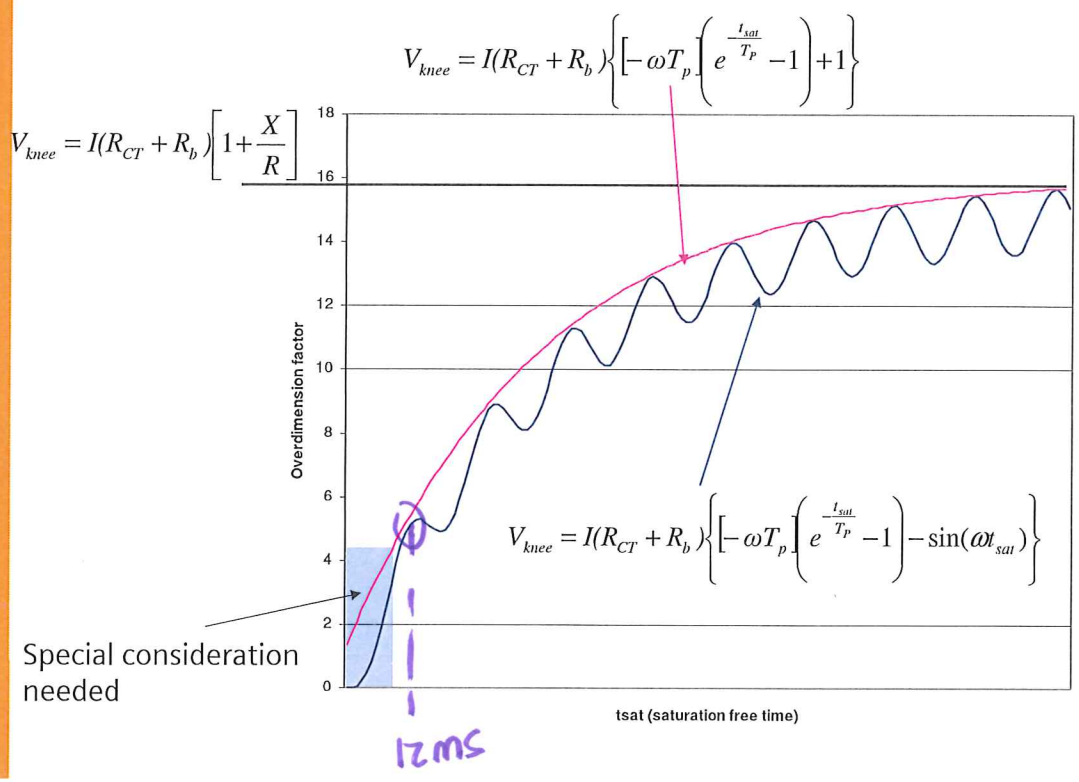
$$V_{knee} = I(R_{CT} + R_b) \left\{ \left[ -\omega T_p \left( e^{\frac{t_{sat}}{T_p}} - 1 \right) - \sin(\omega t_{sat}) \right] \right\}$$

Many times a simplified version where  $-\sin(\omega t)$  is replaced by 1 is used

$$V_{knee} = I(R_{CT} + R_b) \left\{ \left[ -\omega T_p \left( e^{\frac{t_{sat}}{T_p}} - 1 \right) + 1 \right] \right\}$$



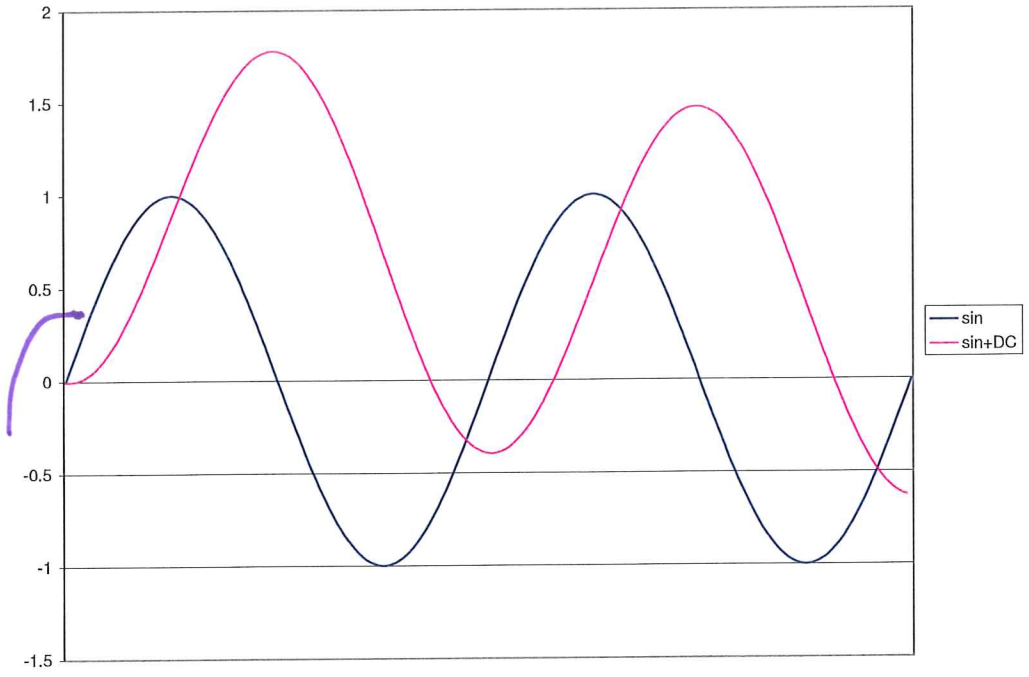
## What does the different formulas describe?



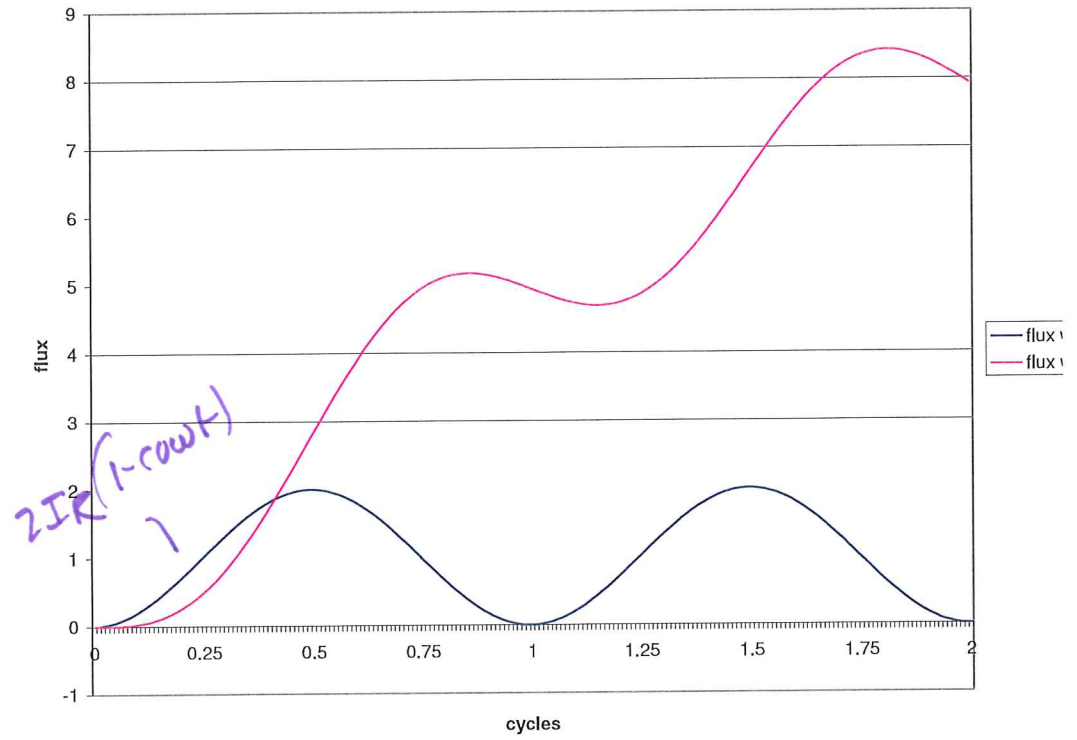
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### Saturation free times < 7ms



### Flux for saturation free time < 7 ms



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## Which formula should be applied

No saturation  $V_{knee} = I(R_{CT} + R_b) \left[ 1 + \frac{X}{R} \right]$

Saturation free time > 12ms  $V_{knee} = I(R_{CT} + R_b) \left\{ [-\omega T_p] \left( e^{\frac{t_{sat}}{T_p}} - 1 \right) + 1 \right\}$

Saturation free time between 7-12 ms  $V_{knee} = I(R_{CT} + R_b) \left\{ [-\omega T_p] \left( e^{\frac{t_{sat}}{T_p}} - 1 \right) - \sin(\omega t_{sat}) \right\}$

Saturation free time < 7ms  $V_{knee} = I(R_{CT} + R_b) [1 - \cos(\omega t_{sat})]$



## Influence of CT saturation on protection

- Distance protection
  - Close in faults
    - Direction has to be correct
    - High speed tripping decision before saturation
  - Zone end fault
    - Accuracy and timing will be effected
  
- Overcurrent protection
  - based on RMS or fundamental
  - 50 element not influenced if remaining current is above pickup
  - 51 element experienced an additional time delay
  
- Differential protection
  - Critical for the security of the protection!

- They are not exactly a voltage. This is better described as the Volt-Time Area
- If you are working from measured data:

$$VTA(x) = \sum_{j=0}^x (V_{sec,j} \cdot \Delta t) \quad \Delta t \text{ is the sampling rate}$$

- A more general equation is

$$B_s \cdot N \cdot \text{Area} \cdot \omega = \omega \cdot I_{fmax\_sec} \cdot R_b \cdot \left( e^{\frac{-t}{T_p}} - \cos(\omega \cdot t) \right)$$

- So this works out to be the flux as a function of time, multiplied times the frequency
- Adding the frequency covers the summation of time slices

**Example**

*total burden*

$$R_b := 5\text{ohm} \quad CTR := \frac{1200}{5} \quad CTR = 240$$

*RMS*

$$I_{fmax\_sec} := 18.5\text{A} \quad I_{fmax\_sec} = 90\text{A}$$

$$I_{fp} := CTR \cdot I_{fmax\_sec} \quad I_{fp} = 21.6\text{kA} \quad \bullet \text{ Fault current referred to primary}$$

$$I_{fmax\_sec} \cdot (R_b) = 450\text{V} \quad \bullet \text{ If no DC offset needs to be included}$$

$$XoverR := 12 \quad \omega := 2 \cdot \pi \cdot 60\text{Hz}$$

$$T_p := \frac{XoverR}{\omega} \quad T_p = 31.83\text{ms}$$

$$I_{fmax\_sec} \cdot (R_b) \cdot (1 + XoverR) = 5850\text{V} \quad \bullet \text{ Expensive custom order}$$

- pu equation:  $\frac{I_{fmax\_sec}}{5\text{A}} \cdot \left( \frac{R_b}{8\text{ohm}} \right) \cdot (1 + XoverR) = 146.25$

*800*

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87  
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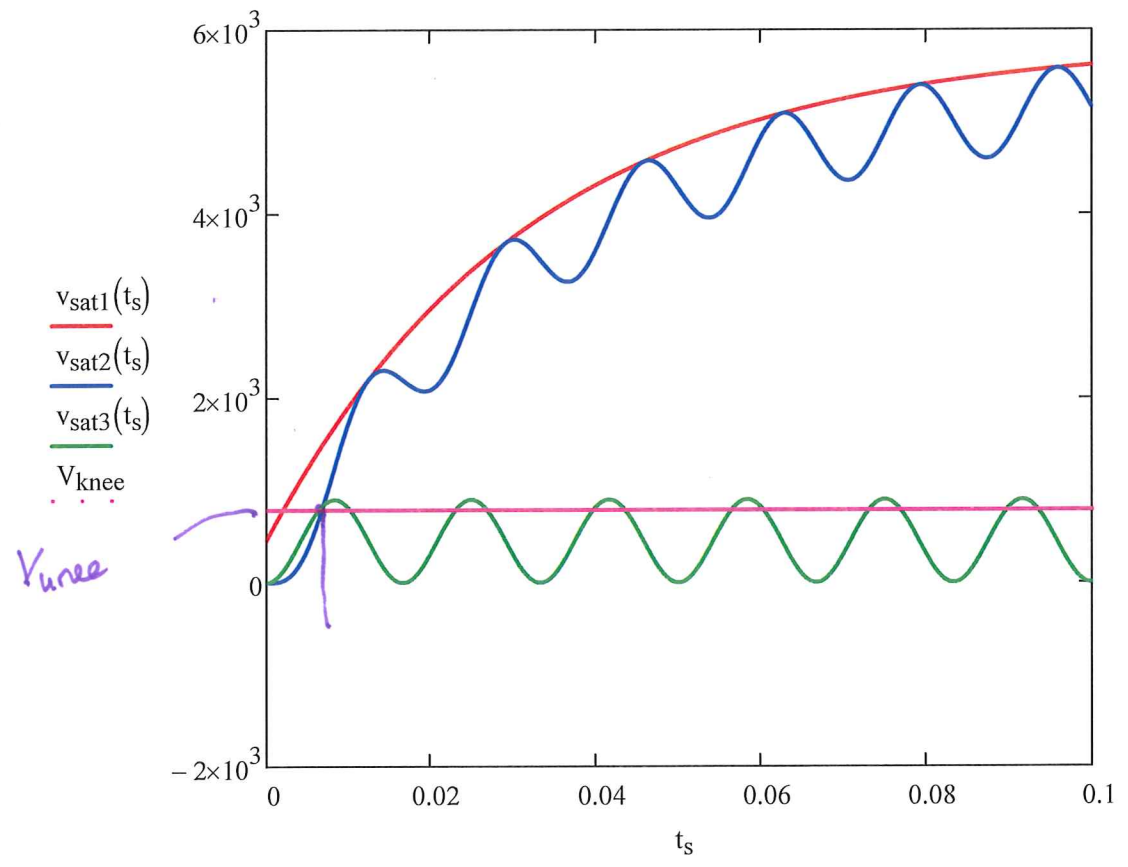
Now lets say we want  $V_{knee} := 800V$

$$v_{sat1}(t_s) := I_{fmax\_sec} \cdot R_b \cdot \left[ (-X_{overR}) \cdot \left( e^{\frac{-t_s}{T_p}} - 1 \right) + 1 \right]$$

$$v_{sat2}(t_s) := \left[ I_{fmax\_sec} \cdot R_b \cdot \left[ (-X_{overR}) \cdot \left( e^{\frac{-t_s}{T_p}} - 1 \right) - \sin(\omega \cdot t_s) \right] \right]$$

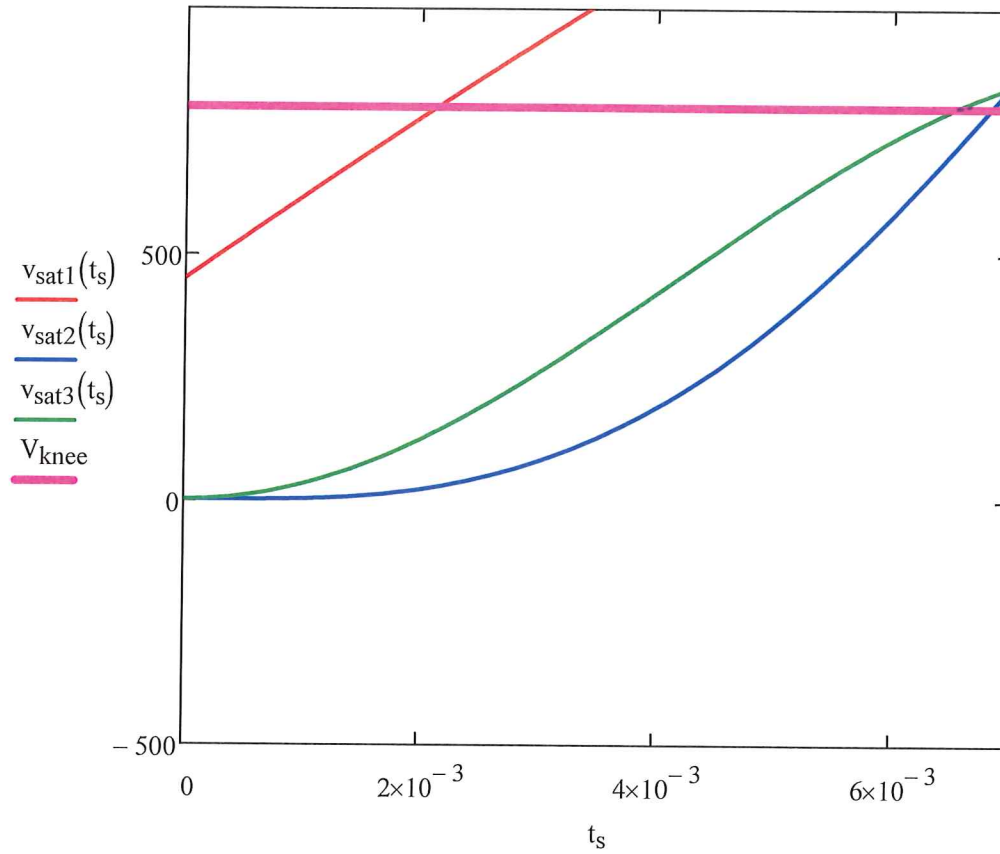
$$v_{sat3}(t_s) := I_{fmax\_sec} \cdot R_b \cdot (1 - \cos(\omega \cdot t_s))$$

$t_s := 0ms, 0.1ms.. 100ms$



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Zoom in to the beginning:

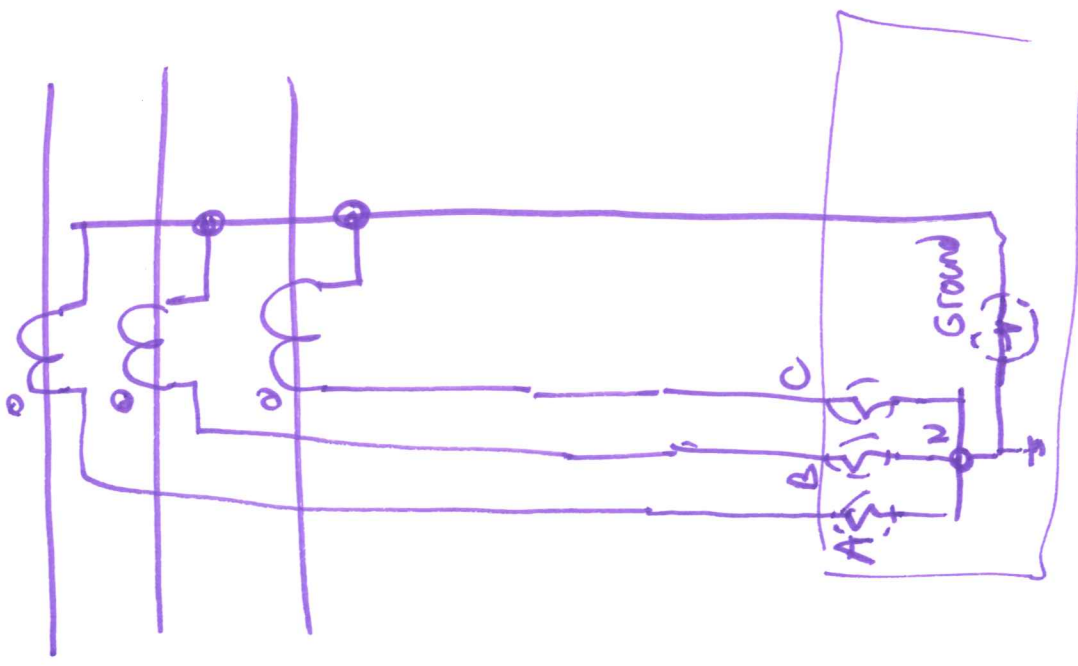
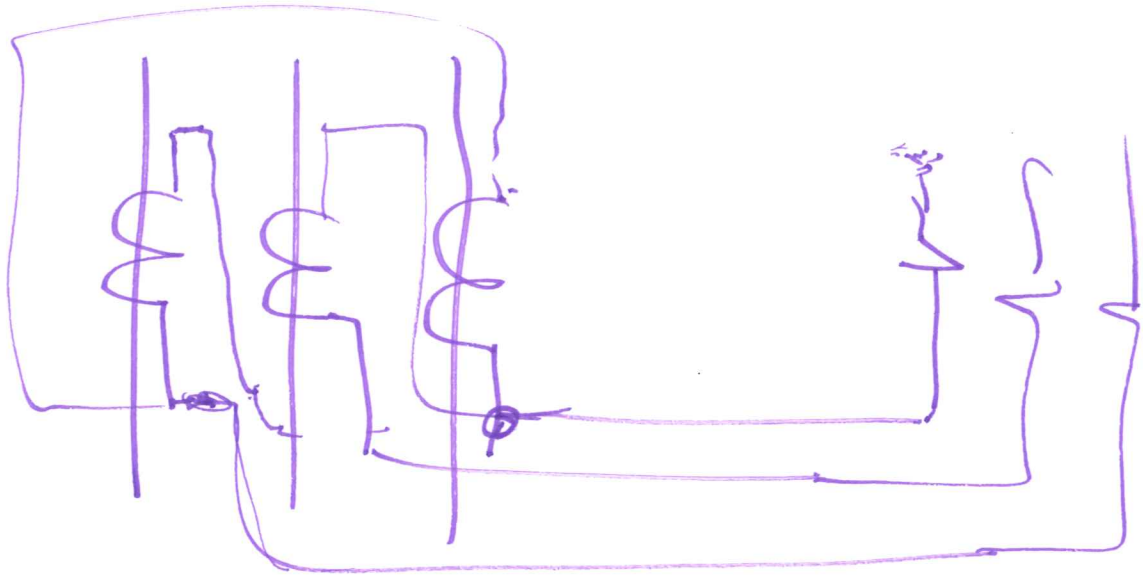


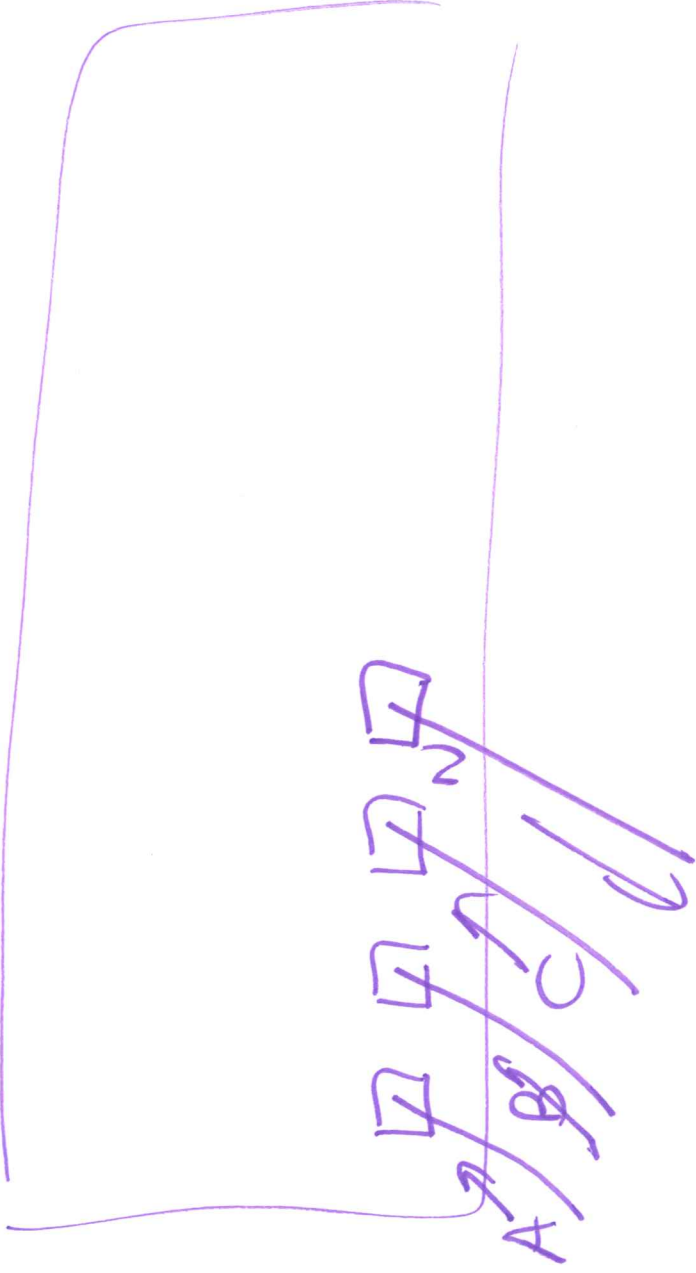
Saturation in 6.6 ms





# CT connections





Ungrounded system (as high R grounded)

core flux summary CT

