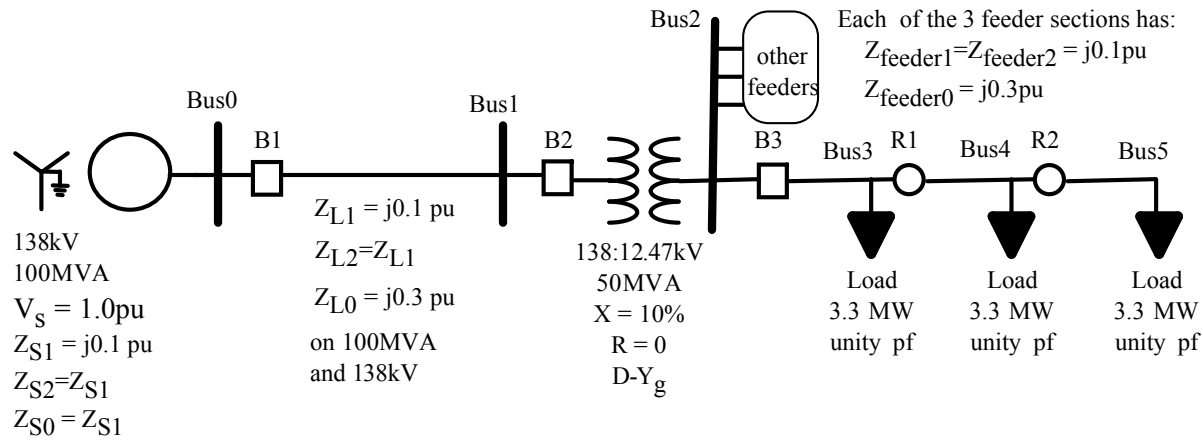


ECE 525: Homework #4

Fault Current Calculations

Calculate the fault currents for three-phase, phase-to-phase and single-phase-to-ground faults at the following locations: at the distribution station 138 kV bus, distribution station 12.47 kV bus, and the end of each of the three sections of the feeder.



- Define units and constants

$$\text{pu} := 1 \quad \text{MVA} := 1000 \text{ kW} \quad \text{MW} := \text{MVA}$$

$$a := e^{j \cdot 120 \text{ deg}}$$

$$A_{012} := \begin{pmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{pmatrix}$$

- Define system bases

$$S_B := 100\text{MVA} \quad V_{BH} := 138\text{kV} \quad V_{BL} := V_{BH} \cdot \left(\frac{12.47\text{kV}}{138\text{kV}} \right) \quad V_{BL} = 12.47\text{kV}$$

$$I_{BH} := \frac{S_B}{\sqrt{3} \cdot V_{BH}} \quad I_{BH} = 418.37\text{ A}$$

$$I_{BL} := \frac{S_B}{\sqrt{3} \cdot V_{BL}} \quad I_{BL} = 4629.91\text{ A}$$

- Per unit impedances

- Source

$$Z_{S1} := j \cdot 0.1\text{pu}$$

$$Z_{S0} := j \cdot 0.1\text{pu}$$

- Line

$$Z_{L1} := j \cdot 0.1\text{pu}$$

$$Z_{L0} := j \cdot 0.3\text{pu}$$

- Feeder sections (per section)

$$Z_{feeder1} := j \cdot 0.1\text{pu}$$

$$Z_{feeder0} := j \cdot 0.3\text{pu}$$

- Transformer

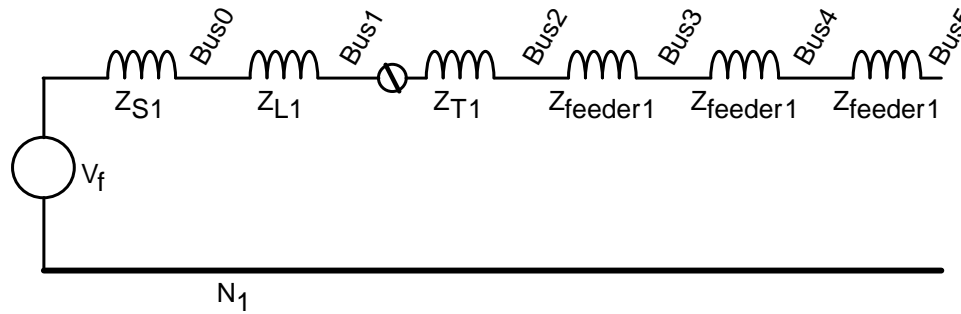
$$S_{\text{rated}} := 50\text{MVA} \quad V_{HV} := 138\text{kV} \quad V_{LV} := 12.47\text{kV} \quad Z_r := j \cdot 10\%$$

- change of base calculation

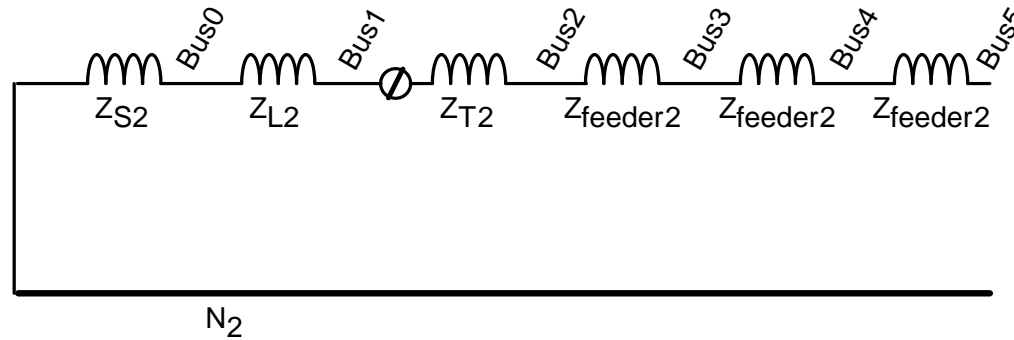
$$Z_{T1} := Z_r \cdot \left(\frac{V_{HV}}{V_{BH}} \right)^2 \cdot \left(\frac{S_B}{S_{\text{rated}}} \right) \quad Z_{T1} = 0.2i \cdot \text{pu} \quad Z_{T0} := Z_{T1}$$

Sequence Equivalent Circuits

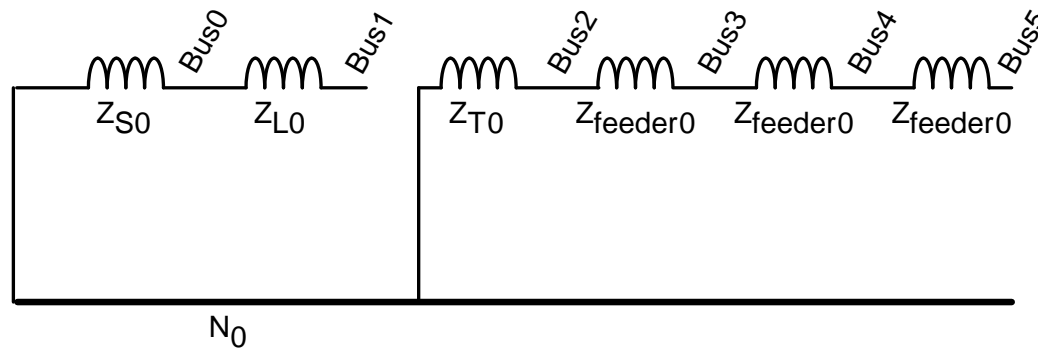
- Positive sequence equivalent circuit:



- Negative sequence equivalent circuit:



- Zero sequence equivalent circuit:



Fault current calculations

- First form Ybus and then Zbus for each sequence. First the positive sequence

$$Y_1 := \begin{pmatrix} \frac{1}{Z_{S1}} + \frac{1}{Z_{L1}} & \frac{-1}{Z_{L1}} & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L1}} & \frac{1}{Z_{L1}} + \frac{1}{Z_{T1}} & \frac{-1 \cdot e^{j \cdot 30 \text{deg}}}{Z_{T1}} & 0 & 0 & 0 \\ 0 & \frac{-1 \cdot e^{-j \cdot 30 \text{deg}}}{Z_{T1}} & \frac{1}{Z_{T1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 & 0 \\ 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 \\ 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} \end{pmatrix}$$

$$Y_1 = \begin{pmatrix} -20i & 10i & 0 & 0 & 0 & 0 \\ 10i & -15i & -2.5 + 4.33i & 0 & 0 & 0 \\ 0 & 2.5 + 4.33i & -15i & 10i & 0 & 0 \\ 0 & 0 & 10i & -20i & 10i & 0 \\ 0 & 0 & 0 & 10i & -20i & 10i \\ 0 & 0 & 0 & 0 & 10i & -10i \end{pmatrix} \cdot \text{pu}$$

$$Z_1 := Y_1^{-1}$$

$$Z_1 = \begin{pmatrix} 0.1i & 0.1i & -0.05 + 0.09i & -0.05 + 0.09i & -0.05 + 0.09i & -0.05 + 0.09i \\ 0.1i & 0.2i & -0.1 + 0.17i & -0.1 + 0.17i & -0.1 + 0.17i & -0.1 + 0.17i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.4i & 0.4i & 0.4i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.5i & 0.5i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.6i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.7i \end{pmatrix}$$

- Now the negative sequence (note that the phase shift in the Y-Δ transformer reverses)

$$Y_2 := \begin{pmatrix} \frac{1}{Z_{S1}} + \frac{1}{Z_{L1}} & \frac{-1}{Z_{L1}} & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L1}} & \frac{1}{Z_{L1}} + \frac{1}{Z_{T1}} & \frac{-1 \cdot e^{-j \cdot 30 \text{deg}}}{Z_{T1}} & 0 & 0 & 0 \\ 0 & \frac{-1 \cdot e^{j \cdot 30 \text{deg}}}{Z_{T1}} & \frac{1}{Z_{T1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 & 0 \\ 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 \\ 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} \end{pmatrix}$$

$$Y_2 = \begin{pmatrix} -20i & 10i & 0 & 0 & 0 & 0 \\ 10i & -15i & 2.5 + 4.33i & 0 & 0 & 0 \\ 0 & -2.5 + 4.33i & -15i & 10i & 0 & 0 \\ 0 & 0 & 10i & -20i & 10i & 0 \\ 0 & 0 & 0 & 10i & -20i & 10i \\ 0 & 0 & 0 & 0 & 10i & -10i \end{pmatrix} \cdot \text{pu}$$

$$Z_2 := Y_2^{-1}$$

$$Z_2 = \begin{pmatrix} 0.1i & 0.1i & 0.05 + 0.09i & 0.05 + 0.09i & 0.05 + 0.09i & 0.05 + 0.09i \\ 0.1i & 0.2i & 0.1 + 0.17i & 0.1 + 0.17i & 0.1 + 0.17i & 0.1 + 0.17i \\ -0.05 + 0.09i & -0.1 + 0.17i & 0.4i & 0.4i & 0.4i & 0.4i \\ -0.05 + 0.09i & -0.1 + 0.17i & 0.4i & 0.5i & 0.5i & 0.5i \\ -0.05 + 0.09i & -0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.6i \\ -0.05 + 0.09i & -0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.7i \end{pmatrix}$$

- Now the zero sequence (no transformer phase shift, but now open circuit)

$$Y_0 := \begin{pmatrix} \frac{1}{Z_{S0}} + \frac{1}{Z_{L0}} & \frac{-1}{Z_{L0}} & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L0}} & \frac{1}{Z_{L0}} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{Z_{T0}} + \frac{1}{Z_{feeder0}} & \frac{-1}{Z_{feeder0}} & 0 & 0 \\ 0 & 0 & \frac{-1}{Z_{feeder0}} & \frac{1}{Z_{feeder0}} + \frac{1}{Z_{feeder0}} & \frac{-1}{Z_{feeder0}} & 0 \\ 0 & 0 & 0 & \frac{-1}{Z_{feeder0}} & \frac{1}{Z_{feeder0}} + \frac{1}{Z_{feeder0}} & \frac{-1}{Z_{feeder0}} \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{feeder0}} & \frac{1}{Z_{feeder0}} \end{pmatrix}$$

$$Y_0 = \begin{pmatrix} -13.33i & 3.33i & 0 & 0 & 0 & 0 \\ 3.33i & -3.33i & 0 & 0 & 0 & 0 \\ 0 & 0 & -8.33i & 3.33i & 0 & 0 \\ 0 & 0 & 3.33i & -6.67i & 3.33i & 0 \\ 0 & 0 & 0 & 3.33i & -6.67i & 3.33i \\ 0 & 0 & 0 & 0 & 3.33i & -3.33i \end{pmatrix} \cdot \text{pu}$$

$$Z_0 := Y_0^{-1}$$

$$Z_0 = \begin{pmatrix} 0.1i & 0.1i & 0 & 0 & 0 & 0 \\ 0.1i & 0.4i & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.2i & 0.2i & 0.2i & 0.2i \\ 0 & 0 & 0.2i & 0.5i & 0.5i & 0.5i \\ 0 & 0 & 0.2i & 0.5i & 0.8i & 0.8i \\ 0 & 0 & 0.2i & 0.5i & 0.8i & 1.1i \end{pmatrix}$$

- Three phase faults:

$$V_f := 1$$

- 138 kV Bus (Bus1):

$$I_{3ph_Bus1} := \frac{V_f}{Z_{1,1,1}} \quad |I_{3ph_Bus1}| = 5 \cdot pu \quad \arg(I_{3ph_Bus1}) = -90 \cdot deg$$

$$I_{3ph_Bus1_Amps} := I_{3ph_Bus1} \cdot I_{BH} \quad |I_{3ph_Bus1_Amps}| = 2091.85 A$$

- 12.47 kV Bus (Bus2):

$$I_{3ph_Bus2} := \frac{V_f}{Z_{1,2,2}} \quad |I_{3ph_Bus2}| = 2.5 \cdot pu \quad \arg(I_{3ph_Bus2}) = -90 \cdot deg$$

$$I_{3ph_Bus2_Amps} := I_{3ph_Bus2} \cdot I_{BL} \quad |I_{3ph_Bus2_Amps}| = 11.575 \cdot kA$$

- As seen from the HV side of the transformer (B1 or B2)

$$\Delta V1 := Z_{L1} \cdot \begin{pmatrix} 0 \\ 0 \\ -I_{3\text{ph_Bus2}} \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad \Delta V1 = \begin{pmatrix} -0.22 - 0.13i \\ -0.43 - 0.25i \\ -1 \\ -1 \\ -1 \\ -1 \end{pmatrix} \cdot \text{pu}$$

$$V1 := \begin{pmatrix} 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V1 \quad V1 = \begin{pmatrix} 0.65 + 0.38i \\ 0.43 + 0.25i \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad \overrightarrow{|V1|} = \begin{pmatrix} 0.75 \\ 0.5 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

arg(V1₀) = 30·deg
arg(V1₁) = 30·deg

$$I_{B2_HV} := \frac{V1_0 - V1_1}{Z_{L1}} \quad |I_{B2_HV}| = 2.5 \cdot \text{pu} \quad \arg(I_{B2_HV}) = -60 \cdot \text{deg}$$

$$I_{B2_HV_A} := I_{B2_HV} \cdot I_{BH} \quad |I_{B2_HV_A}| = 1045.92 \cdot \text{A}$$

- We will see something similar for each of the three phase faults, with a +30 shift in the current

- At end of first feeder section (just before recloser R1)

$$I_{3\text{ph_Bus3}} := \frac{V_f}{Z_{1,3,3}} \quad |I_{3\text{ph_Bus3}}| = 2 \cdot \text{pu} \quad \arg(I_{3\text{ph_Bus3}}) = -90 \cdot \text{deg}$$

$$I_{3\text{ph_Bus3_Amps}} := I_{3\text{ph_Bus3}} \cdot I_{\text{BL}} \quad |I_{3\text{ph_Bus3_Amps}}| = 9259.83 \cdot \text{A}$$

- At end of second feeder section (just before recloser R2)

$$I_{3\text{ph_Bus4}} := \frac{V_f}{Z_{1,4,4}} \quad |I_{3\text{ph_Bus4}}| = 1.67 \cdot \text{pu} \quad \arg(I_{3\text{ph_Bus4}}) = -90 \cdot \text{deg}$$

$$I_{3\text{ph_Bus4_Amps}} := I_{3\text{ph_Bus4}} \cdot I_{\text{BL}} \quad |I_{3\text{ph_Bus4_Amps}}| = 7716.52 \cdot \text{A}$$

- At end of third (and last) feeder section

$$I_{3\text{ph_Bus5}} := \frac{V_f}{Z_{1,5,5}} \quad |I_{3\text{ph_Bus5}}| = 1.43 \cdot \text{pu} \quad \arg(I_{3\text{ph_Bus5}}) = -90 \cdot \text{deg}$$

$$I_{3\text{ph_Bus5_Amps}} := I_{3\text{ph_Bus5}} \cdot I_{\text{BL}} \quad |I_{3\text{ph_Bus5_Amps}}| = 6614.16 \cdot \text{A}$$

• **Single line to ground faults:**

- 138 kV Bus (Bus1):

$$I_{0\text{SLG_Bus1}} := \frac{V_f}{Z_{1,1,1} + Z_{2,1,1} + Z_{0,1,1}} \quad I_{1\text{SLG_Bus1}} := I_{0\text{SLG_Bus1}} \quad I_{2\text{SLG_Bus1}} := I_{0\text{SLG_Bus1}}$$

$$I_{ABC_SLG_Bus1} := A_{012} \cdot \begin{pmatrix} I_{0SLG_Bus1} \\ I_{1SLG_Bus1} \\ I_{2SLG_Bus1} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_SLG_Bus1}|} = \begin{pmatrix} 3.75 \\ 0 \\ 0 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_SLG_Bus1})} = \begin{pmatrix} -90 \\ 26.57 \\ 26.57 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_SLG_Bus1_A} := I_{ABC_SLG_Bus1} \cdot I_{BH}$$

$$\overrightarrow{|I_{ABC_SLG_Bus1_A}|} = \begin{pmatrix} 1568.89 \\ 0 \\ 0 \end{pmatrix} \text{ A}$$

- 12.47 kV Bus (Bus2):

$$I_{0SLG_Bus2} := \frac{V_f}{Z_{1,2,2} + Z_{2,2,2} + Z_{0,2,2}} \quad I_{1SLG_Bus2} := I_{0SLG_Bus2} \quad I_{2SLG_Bus2} := I_{0SLG_Bus2}$$

$$I_{ABC_SLG_Bus2} := A_{012} \cdot \begin{pmatrix} I_{0SLG_Bus2} \\ I_{1SLG_Bus2} \\ I_{2SLG_Bus2} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_SLG_Bus2}|} = \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_SLG_Bus2})} = \begin{pmatrix} -90 \\ 18.43 \\ 18.43 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_SLG_Bus2_A} := I_{ABC_SLG_Bus2} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_SLG_Bus2_A}|} = \begin{pmatrix} 13.8897 \\ 0 \\ 0 \end{pmatrix} \cdot \text{kA}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_SLG_Bus2} := 0 \text{ pu} \quad \text{no zero sequence current across the transformer}$$

$$\Delta V_{1SLGBus2} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ -I_{1SLG_Bus2} \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad \Delta V_{1SLGBus2} = \begin{pmatrix} -0.09 - 0.05i \\ -0.17 - 0.1i \\ -0.4 \\ -0.4 \\ -0.4 \\ -0.4 \end{pmatrix} \cdot \text{pu}$$

$$V_{1SLGBus2} := \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1SLGBus2} \quad \overrightarrow{|V_{1SLGBus2}|} = \begin{pmatrix} 0.9 \\ 0.8 \\ 0.6 \\ 0.6 \\ 0.6 \\ 0.6 \end{pmatrix} \quad \overrightarrow{\arg(V_{1SLGBus2})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2SLGBus2} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ -I_{2SLG_Bus2} \\ 0 \\ 0 \\ 0 \end{pmatrix} \xrightarrow{|\Delta V_{2SLGBus2}|} = \begin{pmatrix} 0.1 \\ 0.2 \\ 0.4 \\ 0.4 \\ 0.4 \\ 0.4 \end{pmatrix} \cdot \text{pu} \quad \xrightarrow{\arg(\Delta V_{2SLGBus2})} = \begin{pmatrix} 150 \\ 150 \\ 180 \\ 180 \\ 180 \\ 180 \end{pmatrix} \cdot \text{deg}$$

$$V_{2SLGBus2} := \Delta V_{2SLGBus2}$$

$$I_{1_HV_SLG_Bus2} := \frac{V_{1SLGBus2_0} - V_{1SLGBus2_1}}{Z_{L1}}$$

$$|I_{1_HV_SLG_Bus2}| = 1 \cdot \text{pu}$$

$$\arg(I_{1_HV_SLG_Bus2}) = -60 \cdot \text{deg}$$

$$I_{2_HV_SLG_Bus2} := \frac{V_{2SLGBus2_0} - V_{2SLGBus2_1}}{Z_{L1}}$$

$$|I_{2_HV_SLG_Bus2}| = 1 \cdot \text{pu} \quad \arg(I_{2_HV_SLG_Bus2}) = -120 \cdot \text{deg}$$

$$I_{ABC_HV_SLG_Bus2} := A_{012} \cdot \begin{pmatrix} I_{0_HV_SLG_Bus2} \\ I_{1_HV_SLG_Bus2} \\ I_{2_HV_SLG_Bus2} \end{pmatrix}$$

$$\vec{I_{ABC_HV_SLG_Bus2}} = \begin{pmatrix} 1.73 \\ 0 \\ 1.73 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_HV_SLG_Bus2}) = \begin{pmatrix} -90 \\ 158.2 \\ 90 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_HV_SLG_Bus2_A} := I_{ABC_HV_SLG_Bus2} \cdot I_{BH}$$

$$\vec{I_{ABC_HV_SLG_Bus2_A}} = \begin{pmatrix} 724.64 \\ 0 \\ 724.64 \end{pmatrix} \cdot \text{A}$$

- At end of first feeder section (just before recloser R1)

$$I_{0SLG_Bus3} := \frac{V_f}{Z_{1,3,3} + Z_{2,3,3} + Z_{0,3,3}} \quad I_{1SLG_Bus3} := I_{0SLG_Bus3} \quad I_{2SLG_Bus3} := I_{0SLG_Bus3}$$

$$I_{ABC_SLG_Bus3} := A_{012} \cdot \begin{pmatrix} I_{0SLG_Bus3} \\ I_{1SLG_Bus3} \\ I_{2SLG_Bus3} \end{pmatrix}$$

$$\vec{I_{ABC_SLG_Bus3}} = \begin{pmatrix} 2 \\ 0 \\ 0 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_SLG_Bus3}) = \begin{pmatrix} -90 \\ 14.04 \\ 14.04 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_SLG_Bus3_A} := I_{ABC_SLG_Bus3} \cdot I_{BL}$$

$$\vec{I_{ABC_SLG_Bus3_A}} = \begin{pmatrix} 9259.83 \\ 0 \\ 0 \end{pmatrix} \cdot \text{A}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$I_{0_HV_SLG_Bus3} := 0\text{pu}$ no zero sequence current across the transformer

$$\Delta V1_{SLGBus3} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ -I_{1SLG_Bus3} \\ 0 \\ 0 \end{pmatrix} \quad \Delta V1_{SLGBus3} = \begin{pmatrix} -0.06 - 0.03i \\ -0.12 - 0.07i \\ -0.27 \\ -0.33 \\ -0.33 \\ -0.33 \end{pmatrix} \cdot \text{pu}$$

$$V1_{SLGBus3} := \begin{pmatrix} 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V1_{SLGBus3} \quad \overrightarrow{|V1_{SLGBus3}|} = \begin{pmatrix} 0.93 \\ 0.87 \\ 0.73 \\ 0.67 \\ 0.67 \\ 0.67 \end{pmatrix} \quad \overrightarrow{\arg(V1_{SLGBus3})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V2_{SLGBus3} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ -I_{2SLG_Bus3} \\ 0 \\ 0 \end{pmatrix} \quad \overrightarrow{|\Delta V2_{SLGBus3}|} = \begin{pmatrix} 0.07 \\ 0.13 \\ 0.27 \\ 0.33 \\ 0.33 \\ 0.33 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V2_{SLGBus3})} = \begin{pmatrix} 150 \\ 150 \\ 180 \\ 180 \\ 180 \\ 180 \end{pmatrix} \cdot \text{deg}$$

$$V2_{SLG_{Bus3}} := \Delta V2_{SLG_{Bus3}}$$

$$I_{1_HV_SLG_Bus3} := \frac{V1_{SLG_{Bus3}0} - V1_{SLG_{Bus3}1}}{Z_{L1}}$$

$$|I_{1_HV_SLG_Bus3}| = 0.6667 \cdot pu$$

$$\arg(I_{1_HV_SLG_Bus3}) = -60 \cdot deg$$

$$I_{2_HV_SLG_Bus3} := \frac{V2_{SLG_{Bus3}0} - V2_{SLG_{Bus3}1}}{Z_{L1}}$$

$$|I_{2_HV_SLG_Bus3}| = 0.6667 \cdot pu$$

$$\arg(I_{2_HV_SLG_Bus3}) = -120 \cdot deg$$

$$I_{ABC_HV_SLG_Bus3} := A_{012} \cdot \begin{pmatrix} I_{0_HV_SLG_Bus3} \\ I_{1_HV_SLG_Bus3} \\ I_{2_HV_SLG_Bus3} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_HV_SLG_Bus3}|} = \begin{pmatrix} 1.15 \\ 0 \\ 1.15 \end{pmatrix} \cdot pu$$

$$\overrightarrow{\arg(I_{ABC_HV_SLG_Bus3})} = \begin{pmatrix} -90 \\ 40.6 \\ 90 \end{pmatrix} \cdot deg$$

$$I_{ABC_HV_SLG_Bus3_A} := I_{ABC_HV_SLG_Bus3} \cdot I_{BH}$$

$$\overrightarrow{|I_{ABC_HV_SLG_Bus3_A}|} = \begin{pmatrix} 483.09 \\ 0 \\ 483.09 \end{pmatrix} \cdot A$$

- At end of second feeder section (just before recloser R2)

$$I_{0SLG_Bus4} := \frac{V_f}{Z_{1_{4,4}} + Z_{2_{4,4}} + Z_{0_{4,4}}} \quad I_{1SLG_Bus4} := I_{0SLG_Bus4} \quad I_{2SLG_Bus4} := I_{0SLG_Bus4}$$

$$I_{ABC_SLG_Bus4} := A_{012} \cdot \begin{pmatrix} I_{0SLG_Bus4} \\ I_{1SLG_Bus4} \\ I_{2SLG_Bus4} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_SLG_Bus4}|} = \begin{pmatrix} 1.5 \\ 0 \\ 0 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_SLG_Bus4})} = \begin{pmatrix} -90 \\ 18.43 \\ 18.43 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_SLG_Bus4_A} := I_{ABC_SLG_Bus4} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_SLG_Bus4_A}|} = \begin{pmatrix} 6944.87 \\ 0 \\ 0 \end{pmatrix} \cdot \text{A}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_SLG_Bus4} := 0 \text{ pu} \quad \text{no zero sequence current across the transformer}$$

$$\Delta V_{1SLGBus4} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -I_{1SLG_Bus4} \\ 0 \end{pmatrix} \quad \Delta V_{1SLGBus4} = \begin{pmatrix} -0.04 - 0.03i \\ -0.09 - 0.05i \\ -0.2 \\ -0.25 \\ -0.3 \\ -0.3 \end{pmatrix} \cdot \text{pu}$$

$$V1_{SLGBus4} := \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V1_{SLGBus4} \quad \overrightarrow{|V1_{SLGBus4}|} = \begin{pmatrix} 0.95 \\ 0.9 \\ 0.8 \\ 0.75 \\ 0.7 \\ 0.7 \end{pmatrix} \quad \overrightarrow{\arg(V1_{SLGBus4})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V2_{SLGBus4} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -I2_{SLG_Bus4} \\ 0 \end{pmatrix} \quad \overrightarrow{|\Delta V2_{SLGBus4}|} = \begin{pmatrix} 0.05 \\ 0.1 \\ 0.2 \\ 0.25 \\ 0.3 \\ 0.3 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V2_{SLGBus4})} = \begin{pmatrix} 150 \\ 150 \\ 180 \\ 180 \\ 180 \\ 180 \end{pmatrix} \cdot \text{deg}$$

$$V2_{SLGBus4} := \Delta V2_{SLGBus4}$$

$$I1_{HV_SLG_Bus4} := \frac{V1_{SLGBus4_0} - V1_{SLGBus4_1}}{Z_{L1}}$$

$$|I1_{HV_SLG_Bus4}| = 0.5 \cdot \text{pu}$$

$$\arg(I1_{HV_SLG_Bus4}) = -60 \cdot \text{deg}$$

$$I2_{HV_SLG_Bus4} := \frac{V2_{SLGBus4_0} - V2_{SLGBus4_1}}{Z_{L1}}$$

$$|I_{2_HV_SLG_Bus4}| = 0.5 \cdot pu$$

$$\arg(I_{2_HV_SLG_Bus4}) = -120 \cdot deg$$

$$I_{ABC_HV_SLG_Bus4} := A_{012} \cdot \begin{pmatrix} I_{0_HV_SLG_Bus4} \\ I_{1_HV_SLG_Bus4} \\ I_{2_HV_SLG_Bus4} \end{pmatrix}$$

$$\vec{|I_{ABC_HV_SLG_Bus4}|} = \begin{pmatrix} 0.87 \\ 0 \\ 0.87 \end{pmatrix} \cdot pu$$

$$\vec{\arg(I_{ABC_HV_SLG_Bus4})} = \begin{pmatrix} -90 \\ 0 \\ 90 \end{pmatrix} \cdot deg$$

$$I_{ABC_HV_SLG_Bus4_A} := I_{ABC_HV_SLG_Bus4} \cdot I_{BH}$$

$$\vec{|I_{ABC_HV_SLG_Bus4_A}|} = \begin{pmatrix} 362.32 \\ 0 \\ 362.32 \end{pmatrix} \cdot A$$

- At end of third (and last) feeder section

$$I_{0SLG_Bus5} := \frac{V_f}{Z_{1_{5,5}} + Z_{2_{5,5}} + Z_{0_{5,5}}} \quad I_{1SLG_Bus5} := I_{0SLG_Bus5} \quad I_{2SLG_Bus5} := I_{0SLG_Bus5}$$

$$I_{ABC_SLG_Bus5} := A_{012} \cdot \begin{pmatrix} I_{0SLG_Bus5} \\ I_{1SLG_Bus5} \\ I_{2SLG_Bus5} \end{pmatrix}$$

$$\vec{|I_{ABC_SLG_Bus5}|} = \begin{pmatrix} 1.2 \\ 0 \\ 0 \end{pmatrix} \cdot pu$$

$$\vec{\arg(I_{ABC_SLG_Bus5})} = \begin{pmatrix} -90 \\ 18.43 \\ 18.43 \end{pmatrix} \cdot deg$$

$$I_{ABC_SLG_Bus5_A} := I_{ABC_SLG_Bus5} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_SLG_Bus5_A}|} = \begin{pmatrix} 5555.9 \\ 0 \\ 0 \end{pmatrix} \cdot A$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_SLG_Bus5} := 0 \text{ pu} \quad \text{no zero sequence current across the transformer}$$

$$\Delta V_{1SLGBus5} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -I_{1SLG_Bus5} \end{pmatrix} \quad \Delta V_{1SLGBus5} = \begin{pmatrix} -0.03 - 0.02i \\ -0.07 - 0.04i \\ -0.16 \\ -0.2 \\ -0.24 \\ -0.28 \end{pmatrix} \cdot \text{pu}$$

$$V_{1SLGBus5} := \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1SLGBus5} \quad \overrightarrow{|V_{1SLGBus5}|} = \begin{pmatrix} 0.96 \\ 0.92 \\ 0.84 \\ 0.8 \\ 0.76 \\ 0.72 \end{pmatrix} \quad \overrightarrow{\arg(V_{1SLGBus5})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2SLGBus5} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -I_{2SLG_Bus5} \end{pmatrix} \xrightarrow{|\Delta V_{2SLGBus5}|} \begin{pmatrix} 0.04 \\ 0.08 \\ 0.16 \\ 0.2 \\ 0.24 \\ 0.28 \end{pmatrix} \cdot \text{pu} \xrightarrow{\arg(\Delta V_{2SLGBus5})} \begin{pmatrix} 150 \\ 150 \\ 180 \\ 180 \\ 180 \\ 180 \end{pmatrix} \cdot \text{deg}$$

$$V_{2SLGBus5} := \Delta V_{2SLGBus5}$$

$$I_{1_HV_SLG_Bus5} := \frac{V_{1SLGBus5_0} - V_{1SLGBus5_1}}{Z_{L1}}$$

$$|I_{1_HV_SLG_Bus5}| = 0.4 \cdot \text{pu}$$

$$\arg(I_{1_HV_SLG_Bus5}) = -60 \cdot \text{deg}$$

$$I_{2_HV_SLG_Bus5} := \frac{V_{2SLGBus5_0} - V_{2SLGBus5_1}}{Z_{L1}}$$

$$|I_{2_HV_SLG_Bus5}| = 0.4 \cdot \text{pu}$$

$$\arg(I_{2_HV_SLG_Bus5}) = -120 \cdot \text{deg}$$

$$I_{ABC_HV_SLG_Bus5} := A_{012} \cdot \begin{pmatrix} I_{0_HV_SLG_Bus5} \\ I_{1_HV_SLG_Bus5} \\ I_{2_HV_SLG_Bus5} \end{pmatrix}$$

$$\vec{I_{ABC_HV_SLG_Bus5}} = \begin{pmatrix} 0.69 \\ 0 \\ 0.69 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_HV_SLG_Bus5}) = \begin{pmatrix} -90 \\ 133.15 \\ 90 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_HV_SLG_Bus5_A} := I_{ABC_HV_SLG_Bus5} \cdot I_{BH}$$

$$\vec{I_{ABC_HV_SLG_Bus5_A}} = \begin{pmatrix} 289.86 \\ 0 \\ 289.86 \end{pmatrix} \cdot \text{A}$$

- Line to line faults:**

- 138 kV Bus (Bus1):**

$$I_{1LL_Bus1} := \frac{V_f}{Z_{1,1} + Z_{2,1}}$$

$$I_{2LL_Bus1} := -I_{1LL_Bus1} \quad I_{0LL_Bus1} := 1.0 \cdot 10^{-15} \text{ pu}$$

$$I_{ABC_LL_Bus1} := A_{012} \cdot \begin{pmatrix} I_{0LL_Bus1} \\ I_{1LL_Bus1} \\ I_{2LL_Bus1} \end{pmatrix}$$

$$\vec{I_{ABC_LL_Bus1}} = \begin{pmatrix} 0 \\ 4.33 \\ 4.33 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_LL_Bus1}) = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_LL_Bus1_A} := I_{ABC_LL_Bus1} \cdot I_{BH}$$

$$\vec{I}_{ABC_LL_Bus1_A} = \begin{pmatrix} 0 \\ 1811.59 \\ 1811.59 \end{pmatrix} \text{ A}$$

- 12.47 kV Bus (Bus2):

$$I_{1LL_Bus2} := \frac{V_f}{Z_{12,2} + Z_{22,2}}$$

$$I_{2LL_Bus2} := -I_{1LL_Bus2} \quad I_{0LL_Bus2} := 1.0 \cdot 10^{-15} \text{ pu}$$

$$I_{ABC_LL_Bus2} := A_{012} \cdot \begin{pmatrix} I_{0LL_Bus2} \\ I_{1LL_Bus2} \\ I_{2LL_Bus2} \end{pmatrix}$$

$$\vec{I}_{ABC_LL_Bus2} = \begin{pmatrix} 0 \\ 2.17 \\ 2.17 \end{pmatrix} \cdot \text{pu}$$

$$\arg(I_{ABC_LL_Bus2}) = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_LL_Bus2_A} := I_{ABC_LL_Bus2} \cdot I_{BL}$$

$$\vec{I}_{ABC_LL_Bus2_A} = \begin{pmatrix} 0 \\ 10.0241 \\ 10.0241 \end{pmatrix} \cdot \text{kA}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$I_{0_HV_LL_Bus2} := 0\text{pu}$ no zero sequence current for this fault type

$$\Delta V_{1LLBus2} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ -I_{1LL_Bus2} \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad \Delta V_{1LLBus2} = \begin{pmatrix} -0.11 - 0.06i \\ -0.22 - 0.13i \\ -0.5 \\ -0.5 \\ -0.5 \\ -0.5 \end{pmatrix} \cdot \text{pu}$$

$$V_{1LLBus2} := \begin{pmatrix} 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1LLBus2} \quad \overrightarrow{|V_{1LLBus2}|} = \begin{pmatrix} 0.88 \\ 0.75 \\ 0.5 \\ 0.5 \\ 0.5 \\ 0.5 \end{pmatrix} \quad \overrightarrow{\arg(V_{1LLBus2})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2LLBus2} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ -I_{2LL_Bus2} \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad \overrightarrow{|\Delta V_{2LLBus2}|} = \begin{pmatrix} 0.13 \\ 0.25 \\ 0.5 \\ 0.5 \\ 0.5 \\ 0.5 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V_{2LLBus2})} = \begin{pmatrix} -30 \\ -30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$V_{2LLBus2} := \Delta V_{2LLBus2}$$

$$I_{1_HV_LL_Bus2} := \frac{V_{1LLBus2_0} - V_{1LLBus2_1}}{Z_{L1}}$$

$$|I_{1_HV_LL_Bus2}| = 1.25 \cdot pu$$

$$\arg(I_{1_HV_LL_Bus2}) = -60 \cdot deg$$

$$I_{2_HV_LL_Bus2} := \frac{V_{2LLBus2_0} - V_{2LLBus2_1}}{Z_{L1}}$$

$$|I_{2_HV_LL_Bus2}| = 1.25 \cdot pu$$

$$\arg(I_{2_HV_LL_Bus2}) = 60 \cdot deg$$

$$I_{ABC_HV_LL_Bus2} := A_{012} \cdot \begin{pmatrix} I_{0_HV_LL_Bus2} \\ I_{1_HV_LL_Bus2} \\ I_{2_HV_LL_Bus2} \end{pmatrix}$$

$$\vec{|I_{ABC_HV_LL_Bus2}|} = \begin{pmatrix} 1.25 \\ 2.5 \\ 1.25 \end{pmatrix} \cdot pu$$

$$\vec{\arg(I_{ABC_HV_LL_Bus2})} = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot deg$$

$$I_{ABC_HV_LL_Bus2_A} := I_{ABC_HV_LL_Bus2} \cdot I_{BH}$$

$$\vec{|I_{ABC_HV_LL_Bus2_A}|} = \begin{pmatrix} 522.96 \\ 1045.92 \\ 522.96 \end{pmatrix} \cdot A$$

- At end of first feeder section (just before recloser R1)

$$I_{1LL_Bus3} := \frac{V_f}{Z_{13,3} + Z_{23,3}} \quad I_{2LL_Bus3} := -I_{1LL_Bus3} \quad I_{0LL_Bus3} := 1.0 \cdot 10^{-15} \text{ pu}$$

$$I_{ABC_LL_Bus3} := A_{012} \cdot \begin{pmatrix} I_{0LL_Bus3} \\ I_{1LL_Bus3} \\ I_{2LL_Bus3} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_LL_Bus3}|} = \begin{pmatrix} 0 \\ 1.73 \\ 1.73 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_LL_Bus3})} = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_LL_Bus3_A} := I_{ABC_LL_Bus3} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_LL_Bus3_A}|} = \begin{pmatrix} 0 \\ 8019.25 \\ 8019.25 \end{pmatrix} \cdot \text{A}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_LL_Bus3} := 0 \text{ pu} \quad \text{no zero sequence current for this fault type}$$

$$\Delta V_{1LLBus3} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ -I_{1LL_Bus3} \\ 0 \\ 0 \end{pmatrix} \quad \Delta V_{1LLBus3} = \begin{pmatrix} -0.09 - 0.05i \\ -0.17 - 0.1i \\ -0.4 \\ -0.5 \\ -0.5 \\ -0.5 \end{pmatrix} \cdot \text{pu}$$

$$V_{1LLBus3} := \begin{pmatrix} 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \cdot e^{j \cdot 30\text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1LLBus3} \quad \overrightarrow{|V_{1LLBus3}|} = \begin{pmatrix} 0.9 \\ 0.8 \\ 0.6 \\ 0.5 \\ 0.5 \\ 0.5 \end{pmatrix} \quad \overrightarrow{\arg(V_{1LLBus3})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2LLBus3} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ -I_{2LL_Bus3} \\ 0 \\ 0 \end{pmatrix} \quad \overrightarrow{|\Delta V_{2LLBus3}|} = \begin{pmatrix} 0.1 \\ 0.2 \\ 0.4 \\ 0.5 \\ 0.5 \\ 0.5 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V_{2LLBus3})} = \begin{pmatrix} -30 \\ -30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$V_{2LLBus3} := \Delta V_{2LLBus3}$$

$$I_{1_HV_LL_Bus3} := \frac{V_{1LLBus3_0} - V_{1LLBus3_1}}{Z_{L1}}$$

$$|I_{1_HV_LL_Bus3}| = 1 \cdot \text{pu}$$

$$\arg(I_{1_HV_LL_Bus3}) = -60 \cdot \text{deg}$$

$$I_{2_HV_LL_Bus3} := \frac{V_{2LLBus3_0} - V_{2LLBus3_1}}{Z_{L1}}$$

$$|I_{2_HV_LL_Bus3}| = 1 \cdot \text{pu}$$

$$\arg(I_{2_HV_LL_Bus3}) = 60 \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus3} := A_{012} \cdot \begin{pmatrix} I_{0_HV_LL_Bus3} \\ I_{1_HV_LL_Bus3} \\ I_{2_HV_LL_Bus3} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus3}|} = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_HV_LL_Bus3})} = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus3_A} := I_{ABC_HV_LL_Bus3} \cdot I_{BH}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus3_A}|} = \begin{pmatrix} 418.37 \\ 836.74 \\ 418.37 \end{pmatrix} \cdot \text{A}$$

- At end of second feeder section (just before recloser R2)

$$I_{1LL_Bus4} := \frac{V_f}{Z_{1,4} + Z_{2,4}} \quad I_{2LL_Bus4} := -I_{1LL_Bus4} \quad I_{0LL_Bus4} := 1.0 \cdot 10^{-15} \text{ pu}$$

$$I_{ABC_LL_Bus4} := A_{012} \cdot \begin{pmatrix} I_{0LL_Bus4} \\ I_{1LL_Bus4} \\ I_{2LL_Bus4} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_LL_Bus4}|} = \begin{pmatrix} 0 \\ 1.44 \cdot \text{pu} \\ 1.44 \end{pmatrix}$$

$$\overrightarrow{\arg(I_{ABC_LL_Bus4})} = \begin{pmatrix} 0 \\ 180 \cdot \text{deg} \\ 0 \end{pmatrix}$$

$$I_{ABC_LL_Bus4_A} := I_{ABC_LL_Bus4} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_LL_Bus4_A}|} = \begin{pmatrix} 0 \\ 6682.71 \cdot \text{A} \\ 6682.71 \end{pmatrix}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_LL_Bus4} := 0 \text{ pu} \quad \text{no zero sequence current for this fault type}$$

$$\Delta V_{1LLBus4} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -I_{1LL_Bus4} \\ 0 \end{pmatrix}$$

$$\Delta V_{1LLBus4} = \begin{pmatrix} -0.07 - 0.04i \\ -0.14 - 0.08i \\ -0.33 \\ -0.42 \\ -0.5 \\ -0.5 \end{pmatrix} \cdot \text{pu}$$

$$V_{1LLBus4} := \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1LLBus4} \quad \overrightarrow{|V_{1LLBus4}|} = \begin{pmatrix} 0.92 \\ 0.83 \\ 0.67 \\ 0.58 \\ 0.5 \\ 0.5 \end{pmatrix} \quad \overrightarrow{\arg(V_{1LLBus4})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2LLBus4} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -I_{2LL_Bus4} \\ 0 \end{pmatrix} \quad \overrightarrow{|\Delta V_{2LLBus4}|} = \begin{pmatrix} 0.08 \\ 0.17 \\ 0.33 \\ 0.42 \\ 0.5 \\ 0.5 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V_{2LLBus4})} = \begin{pmatrix} -30 \\ -30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$V_{2LLBus4} := \Delta V_{2LLBus4}$$

$$I_{1_HV_LL_Bus4} := \frac{V_{1LLBus4_0} - V_{1LLBus4_1}}{Z_{L1}}$$

$$\boxed{|I_{1_HV_LL_Bus4}| = 0.8333 \cdot \text{pu}}$$

$$\boxed{\arg(I_{1_HV_LL_Bus4}) = -60 \cdot \text{deg}}$$

$$I_{2_HV_LL_Bus4} := \frac{V_{2LLBus4_0} - V_{2LLBus4_1}}{Z_{L1}}$$

$$|I_{2_HV_LL_Bus4}| = 0.8333 \cdot \text{pu}$$

$$\arg(I_{2_HV_LL_Bus4}) = 60 \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus4} := A_{012} \cdot \begin{pmatrix} I_{0_HV_LL_Bus4} \\ I_{1_HV_LL_Bus4} \\ I_{2_HV_LL_Bus4} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus4}|} = \begin{pmatrix} 0.83 \\ 1.67 \\ 0.83 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_HV_LL_Bus4})} = \begin{pmatrix} 0 \\ 180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus4_A} := I_{ABC_HV_LL_Bus4} \cdot I_{BH}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus4_A}|} = \begin{pmatrix} 348.64 \\ 697.28 \\ 348.64 \end{pmatrix} \cdot \text{A}$$

- At end of third feeder section (end of feeder)

$$I_{1LL_Bus5} := \frac{V_f}{Z_{15,5} + Z_{25,5}}$$

$$I_{2LL_Bus5} := -I_{1LL_Bus5}$$

$$I_{0LL_Bus5} := 1.0 \cdot 10^{-15} \text{ pu}$$

$$I_{ABC_LL_Bus5} := A_{012} \cdot \begin{pmatrix} I_{0LL_Bus5} \\ I_{1LL_Bus5} \\ I_{2LL_Bus5} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_LL_Bus5}|} = \begin{pmatrix} 0 \\ 1.24 \cdot pu \\ 1.24 \end{pmatrix}$$

$$\overrightarrow{\arg(I_{ABC_LL_Bus5})} = \begin{pmatrix} 0 \\ 180 \cdot deg \\ 0 \end{pmatrix}$$

$$I_{ABC_LL_Bus5_A} := I_{ABC_LL_Bus5} \cdot I_{BL}$$

$$\overrightarrow{|I_{ABC_LL_Bus5_A}|} = \begin{pmatrix} 0 \\ 5728.03 \cdot A \\ 5728.03 \end{pmatrix}$$

- Fault current as seen on HV side of transformer by B2 (or B1)

$$I_{0_HV_LL_Bus5} := 0pu \quad \text{no zero sequence current for this fault type}$$

$$\Delta V_{1LLBus5} := Z_1 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -I_{1LL_Bus5} \end{pmatrix} \quad \Delta V_{1LLBus5} = \begin{pmatrix} -0.06 - 0.04i \\ -0.12 - 0.07i \\ -0.29 \\ -0.36 \\ -0.43 \\ -0.5 \end{pmatrix} \cdot pu$$

$$V_{1LLBus5} := \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta V_{1LLBus5} \quad \overrightarrow{|V_{1LLBus5}|} = \begin{pmatrix} 0.93 \\ 0.86 \\ 0.71 \\ 0.64 \\ 0.57 \\ 0.5 \end{pmatrix} \quad \overrightarrow{\arg(V_{1LLBus5})} = \begin{pmatrix} 30 \\ 30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$\Delta V_{2LLBus5} := Z_2 \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -I_{2LL_Bus5} \end{pmatrix} \quad \overrightarrow{|\Delta V_{2LLBus5}|} = \begin{pmatrix} 0.07 \\ 0.14 \\ 0.29 \\ 0.36 \\ 0.43 \\ 0.5 \end{pmatrix} \cdot \text{pu} \quad \overrightarrow{\arg(\Delta V_{2LLBus5})} = \begin{pmatrix} -30 \\ -30 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$V_{2LLBus5} := \Delta V_{2LLBus5}$$

$$I_{1_HV_LL_Bus5} := \frac{V_{1LLBus5_0} - V_{1LLBus5_1}}{Z_{L1}}$$

$$\boxed{|I_{1_HV_LL_Bus5}| = 0.7143 \cdot \text{pu}}$$

$$\boxed{\arg(I_{1_HV_LL_Bus5}) = -60 \cdot \text{deg}}$$

$$I_{2_HV_LL_Bus5} := \frac{V_{2LLBus5_0} - V_{2LLBus5_1}}{Z_{L1}}$$

$$|I_{2_HV_LL_Bus5}| = 0.7143 \cdot \text{pu}$$

$$\arg(I_{2_HV_LL_Bus5}) = 60 \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus5} := A_{012} \cdot \begin{pmatrix} I_{0_HV_LL_Bus5} \\ I_{1_HV_LL_Bus5} \\ I_{2_HV_LL_Bus5} \end{pmatrix}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus5}|} = \begin{pmatrix} 0.71 \\ 1.43 \\ 0.71 \end{pmatrix} \cdot \text{pu}$$

$$\overrightarrow{\arg(I_{ABC_HV_LL_Bus5})} = \begin{pmatrix} 0 \\ -180 \\ 0 \end{pmatrix} \cdot \text{deg}$$

$$I_{ABC_HV_LL_Bus5_A} := I_{ABC_HV_LL_Bus5} \cdot I_{BH}$$

$$\overrightarrow{|I_{ABC_HV_LL_Bus5_A}|} = \begin{pmatrix} 298.84 \\ 597.67 \\ 298.84 \end{pmatrix} \cdot \text{A}$$

Mid-line Fault Between B3 and R1

- First form Ybus and then Zbus for each sequence. First the positive sequence

$$Y_1(m) := \begin{bmatrix} \frac{1}{Z_{S1}} + \frac{1}{Z_{L1}} & \frac{-1}{Z_{L1}} & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L1}} & \frac{1}{Z_{L1}} + \frac{1}{Z_{T1}} & \frac{-1 \cdot e^{j \cdot 30 \text{deg}}}{Z_{T1}} & 0 & 0 & 0 & 0 \\ 0 & \frac{-1 \cdot e^{-j \cdot 30 \text{deg}}}{Z_{T1}} & \frac{1}{Z_{T1}} + \frac{1}{m \cdot Z_{\text{feeder1}}} & 0 & 0 & 0 & \frac{-1}{m \cdot Z_{\text{feeder1}}} \\ 0 & 0 & 0 & \frac{1}{(1-m) \cdot Z_{\text{feeder1}}} + \frac{1}{Z_{\text{feeder1}}} & \frac{-1}{Z_{\text{feeder1}}} & 0 & \frac{-1}{(1-m) \cdot Z_{\text{feeder1}}} \\ 0 & 0 & 0 & \frac{-1}{Z_{\text{feeder1}}} & \frac{1}{Z_{\text{feeder1}}} + \frac{1}{Z_{\text{feeder1}}} & \frac{-1}{Z_{\text{feeder1}}} & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{\text{feeder1}}} & \frac{1}{Z_{\text{feeder1}}} & 0 \\ 0 & 0 & \frac{-1}{m \cdot Z_{\text{feeder1}}} & \frac{-1}{(1-m) \cdot Z_{\text{feeder1}}} & 0 & 0 & \frac{1}{m \cdot Z_{\text{feeder1}}} + \frac{1}{(1-m) \cdot Z_{\text{feeder1}}} \end{bmatrix}$$

$$Y_1(0.7) = \begin{pmatrix} -20i & 10i & 0 & 0 & 0 & 0 & 0 \\ 10i & -15i & -2.5 + 4.33i & 0 & 0 & 0 & 0 \\ 0 & 2.5 + 4.33i & -19.29i & 0 & 0 & 0 & 14.29i \\ 0 & 0 & 0 & -43.33i & 10i & 0 & 33.33i \\ 0 & 0 & 0 & 10i & -20i & 10i & 0 \\ 0 & 0 & 0 & 0 & 10i & -10i & 0 \\ 0 & 0 & 14.29i & 33.33i & 0 & 0 & -47.62i \end{pmatrix} \cdot \text{pu}$$

$$Z_1(m) := Y_1(m)^{-1}$$

$$Z_1(0.7) = \begin{pmatrix} 0.1i & 0.1i & -0.05 + 0.09i & -0.05 + 0.09i & -0.05 + 0.09i & -0.05 + 0.09i & -0.05 + 0.09i \\ 0.1i & 0.2i & -0.1 + 0.17i & -0.1 + 0.17i & -0.1 + 0.17i & -0.1 + 0.17i & -0.1 + 0.17i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.4i & 0.4i & 0.4i & 0.4i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.5i & 0.5i & 0.47i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.6i & 0.47i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.5i & 0.6i & 0.7i & 0.47i \\ 0.05 + 0.09i & 0.1 + 0.17i & 0.4i & 0.47i & 0.47i & 0.47i & 0.47i \end{pmatrix}$$

- Now the negative sequence (note that the phase shift in the Y-Δ transformer reverses)

- Assume ANSI phase shift (so HV leads LV by 30 degrees)

- Neglect load

$$Y_2(m) := \begin{bmatrix} \frac{1}{Z_{S1}} + \frac{1}{Z_{L1}} & \frac{-1}{Z_{L1}} & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L1}} & \frac{1}{Z_{L1}} + \frac{1}{Z_{T1}} & \frac{-1 \cdot e^{-j \cdot 30 \text{deg}}}{Z_{T1}} & 0 & 0 & 0 & 0 \\ 0 & \frac{-1 \cdot e^{j \cdot 30 \text{deg}}}{Z_{T1}} & \frac{1}{Z_{T1}} + \frac{1}{m \cdot Z_{feeder1}} & 0 & 0 & 0 & \frac{-1}{m \cdot Z_{feeder1}} \\ 0 & 0 & 0 & \frac{1}{(1-m) \cdot Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 & \frac{-1}{(1-m) \cdot Z_{feeder1}} \\ 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} + \frac{1}{Z_{feeder1}} & \frac{-1}{Z_{feeder1}} & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{feeder1}} & \frac{1}{Z_{feeder1}} & 0 \\ 0 & 0 & \frac{-1}{m \cdot Z_{feeder1}} & \frac{-1}{(1-m) \cdot Z_{feeder1}} & 0 & 0 & \frac{1}{m \cdot Z_{feeder1}} + \frac{1}{(1-m) \cdot Z_{feeder1}} \end{bmatrix}$$

$$Z_2(m) := Y_2(m)^{-1}$$

- Now the zero sequence (no transformer phase shift, but now open circuit)

$$Y_0(m) := \begin{bmatrix} \frac{1}{Z_{S0}} + \frac{1}{Z_{L0}} & \frac{-1}{Z_{L0}} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{-1}{Z_{L0}} & \frac{1}{Z_{L0}} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{Z_{T0}} + \frac{1}{m \cdot Z_{feeder0}} & 0 & 0 & 0 & 0 & \frac{-1}{m \cdot Z_{feeder0}} \\ 0 & 0 & 0 & \frac{1}{(1-m) \cdot Z_{feeder0}} + \frac{1}{Z_{feeder0}} & \frac{-1}{Z_{feeder0}} & 0 & 0 & \frac{-1}{(1-m) \cdot Z_{feeder0}} \\ 0 & 0 & 0 & \frac{-1}{Z_{feeder0}} & \frac{1}{Z_{feeder0}} + \frac{1}{Z_{feeder0}} & \frac{-1}{Z_{feeder0}} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{-1}{Z_{feeder0}} & \frac{1}{Z_{feeder0}} & 0 & 0 \\ 0 & 0 & \frac{-1}{m \cdot Z_{feeder0}} & \frac{-1}{(1-m) \cdot Z_{feeder0}} & 0 & 0 & \frac{1}{m \cdot Z_{feeder0}} + \frac{1}{(1-m) \cdot Z_{feeder0}} \end{bmatrix}$$

$$Z_0(m) := Y_0(m)^{-1}$$

- Three phase faults at 70% of the feeder

$$V_f := 1$$

- 138 kV Bus (Bus1):

$$I_{3\text{ph_BusM}}(m) := \frac{V_f}{Z_1(m)_{6,6}} \quad |I_{3\text{ph_BusM}}(0.7)| = 2.13 \cdot \text{pu} \quad \arg(I_{3\text{ph_BusM}}(0.7)) = -90 \cdot \text{deg}$$

$$I_{3\text{ph_BusM_Amps}} := I_{3\text{ph_BusM}}(0.7) \cdot I_{BL} \quad |I_{3\text{ph_BusM_Amps}}| = 9.85 \cdot \text{kA}$$

- As seen from the HV side of the transformer (B1 or B2)

$$\Delta V1(m) := Z_1(m) \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -I_{3\text{ph_BusM}}(m) \end{pmatrix} \quad \Delta V1(0.7) = \begin{pmatrix} -0.18 - 0.11i \\ -0.37 - 0.21i \\ -0.85 \\ -1 \\ -1 \\ -1 \\ -1 \end{pmatrix} \cdot \text{pu}$$

$$\begin{aligned}
 \mathbf{V1(m)} &:= \begin{pmatrix} 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \cdot e^{j \cdot 30 \text{deg}} \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \Delta \mathbf{V1(m)} \quad \mathbf{V1(0.7)} = \begin{pmatrix} 0.68 + 0.39i \\ 0.5 + 0.29i \\ 0.15 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \xrightarrow{|\mathbf{V1(0.7)}|} \begin{pmatrix} 0.79 \\ 0.57 \\ 0.15 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \\
 & \qquad \qquad \qquad \arg(\mathbf{V1(0.7)}_0) = 30 \cdot \text{deg} \\
 & \qquad \qquad \qquad \arg(\mathbf{V1(0.7)}_1) = 30 \cdot \text{deg} \\
 & \qquad \qquad \qquad \arg(\mathbf{V1(0.7)}_2) = 0 \cdot \text{deg}
 \end{aligned}$$

$$\mathbf{I_{BM_HV}(m)} := \frac{\mathbf{V1(m)}_0 - \mathbf{V1(m)}_1}{Z_{L1}} \quad \boxed{|\mathbf{I_{BM_HV}(0.7)}| = 2.1277 \cdot \text{pu}} \quad \boxed{\arg(\mathbf{I_{BM_HV}(0.7)}) = -60 \cdot \text{deg}}$$

$$\mathbf{I_{BM_HV_A}(m)} := \mathbf{I_{BM_HV}(m)} \cdot \mathbf{I_{BH}} \quad \boxed{|\mathbf{I_{BM_HV_A}(0.7)}| = 890.15 \cdot \text{A}}$$

- We will see something similar for each of the three phase faults, with a +30 shift in the current

Similar procedure for the SLG, LL and DLG faults

Load current calculations

- Positive sequence current for each load:

$$P_{\text{load}} := 3.3\text{MW} \quad I_{\text{load}} := \frac{P_{\text{load}}}{\sqrt{3} \cdot V_{\text{BL}}} \quad I_{\text{load}} = 152.79 \text{ A} \quad \text{unity power factor}$$

- Worst case zero sequence current: assume a worst case of a 20% imbalance

$$I_{0_load_max} := 0.20 \cdot I_{\text{load}} \quad I_{0_load_max} = 30.56 \text{ A} \quad \text{Note this is } 3I_0$$

- This is also the load current seen by recloser R2

$$I_{\text{Load_R2_1}} := I_{\text{load}}$$

$$I_{\text{Load_R2_0max}} := I_{0_load_max}$$

- Load at recloser R1

$$I_{\text{load_R1_1}} := 2 \cdot I_{\text{load}} \quad I_{\text{load_R1_1}} = 305.57 \text{ A}$$

$$I_{\text{Load_R1_0max}} := 2I_{0_load_max} \quad I_{\text{Load_R1_0max}} = 61.11 \text{ A}$$

- Load current at 12.47kV breaker (B3)

$$I_{\text{load_B3_1}} := 3 \cdot I_{\text{load}} \quad I_{\text{load_B3_1}} = 458.36 \text{ A} \quad \sqrt{3} \cdot 12.47\text{kV} \cdot 458.36\text{A} = 9.9 \times 10^6 \text{ W}$$

$$I_{\text{Load_B3_0max}} := 3I_{0_load_max} \quad I_{\text{Load_B3_0max}} = 91.67 \text{ A}$$

- Load current on 138kV system (B1 and B2): two approaches:

A. Assume that the only feeder supplied by the transformer is the one we're modeling:

$$I_{\text{load_B2_a}} := I_{\text{load_B3_1}} \cdot \left(\frac{V_{\text{BL}}}{V_{\text{BH}}} \right) \quad I_{\text{load_B2_a}} = 41.42 \text{ A}$$

B. Assume that there are other feeders too and the transformer is loaded to 80% of its MVA rating (so 40 MVA):

$$I_{\text{load_B2_b}} := 0.8 \cdot \left(\frac{50 \text{ MVA}}{\sqrt{3} \cdot V_{\text{BH}}} \right) \quad I_{\text{load_B2_b}} = 167.35 \text{ A}$$

Note: There won't be any zero sequence imbalance current on the HV side due to transformer connection.