

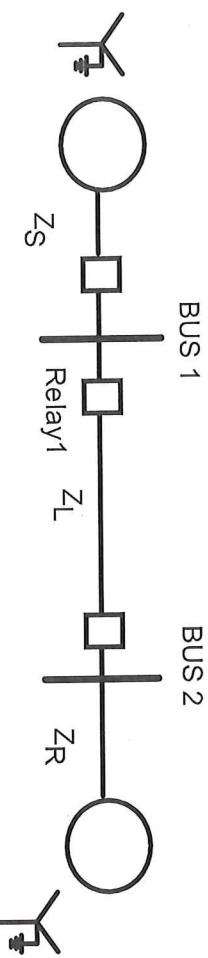
ECE 526

PROTECTION OF
POWER SYSTEMS II

SESSION no. 22

Variation on problem from lecture 20

1. The impedances for the system below are given in secondary ohms.



$$V_S := 100V \cdot e^{j \cdot 0\text{deg}} \quad \text{at } 60\text{Hz}$$

$V_R := 100V \cdot e^{-j \cdot 20\text{deg}}$ at ~~59~~ Hz, so angle is just initial condition

$$Z_{L1} := 10\text{ohm} \cdot e^{j \cdot 75\text{deg}} \quad Z_{S1} := 4\text{ohm} \cdot e^{j \cdot 85\text{deg}} \quad Z_{R1} := 5\text{ohm} \cdot e^{j \cdot 85\text{deg}}$$

For a period of approximately 2-3 seconds do the following:

~~versus~~

1. Plot the instantaneous voltage and current seen at relay 1 ~~versus~~ time
2. Plot the apparent impedance seen by Relay1 versus time (need to have phasors to really do this right--see example posted)
3. Plot the apparent impedance in the impedance plane

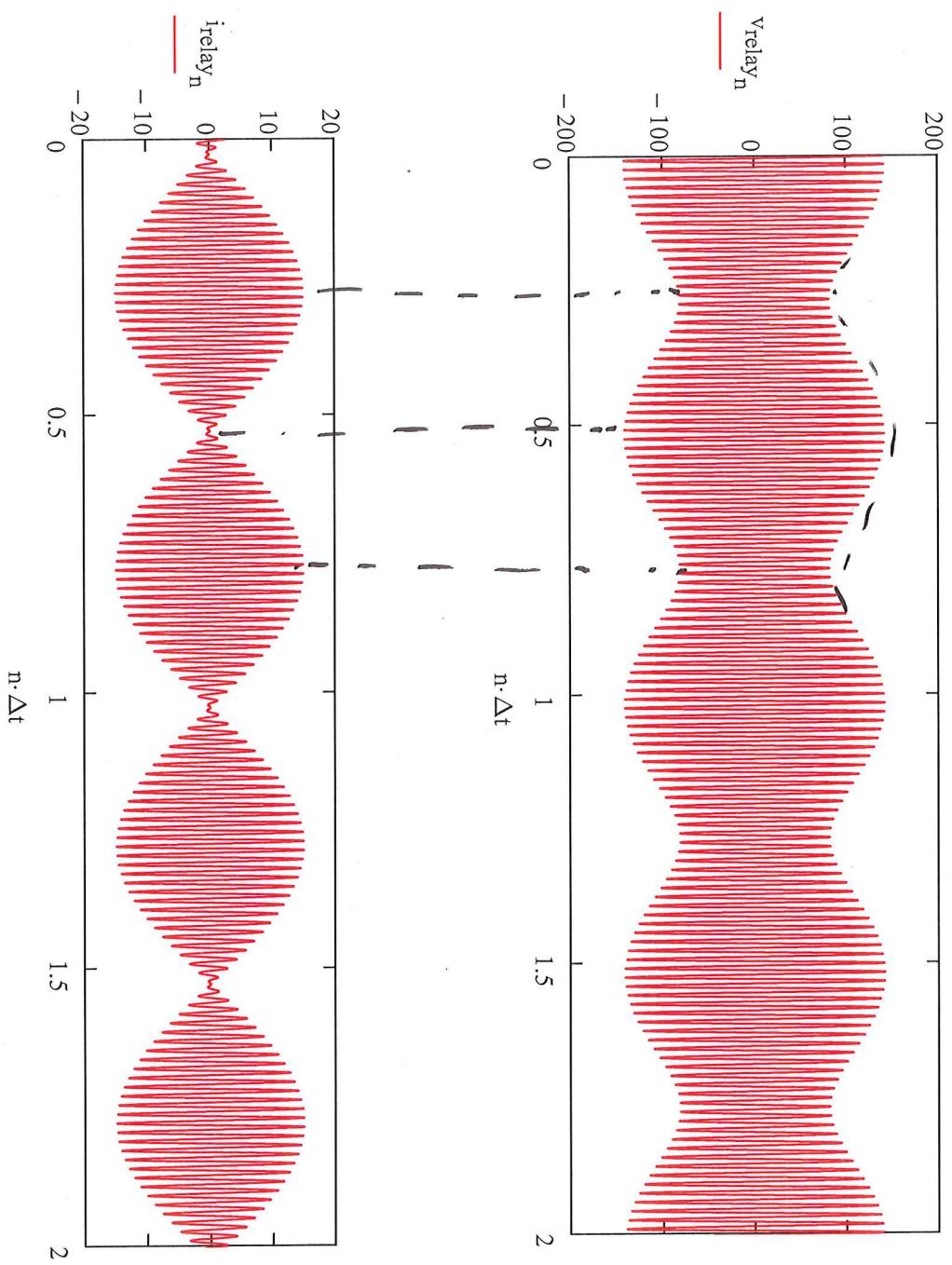
$$Z_{\text{equiv}} := Z_{S1} + Z_{L1} + Z_{R1}$$

$$f_1 := 60\text{Hz} \quad f_2 := 58\text{Hz}$$

$$\omega_{s1} := 2 \cdot \pi \cdot f_1 \quad \omega_{s2} := 2 \cdot \pi \cdot f_2$$

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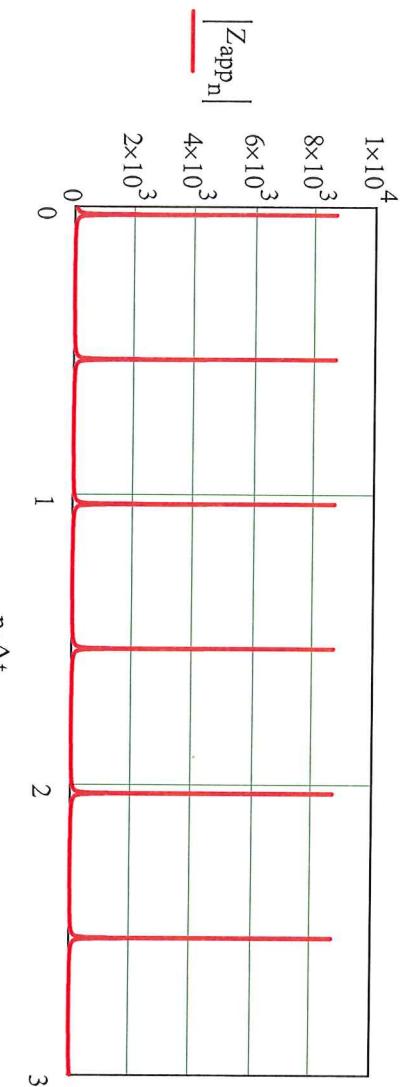
Instantaneous voltage and current versus time



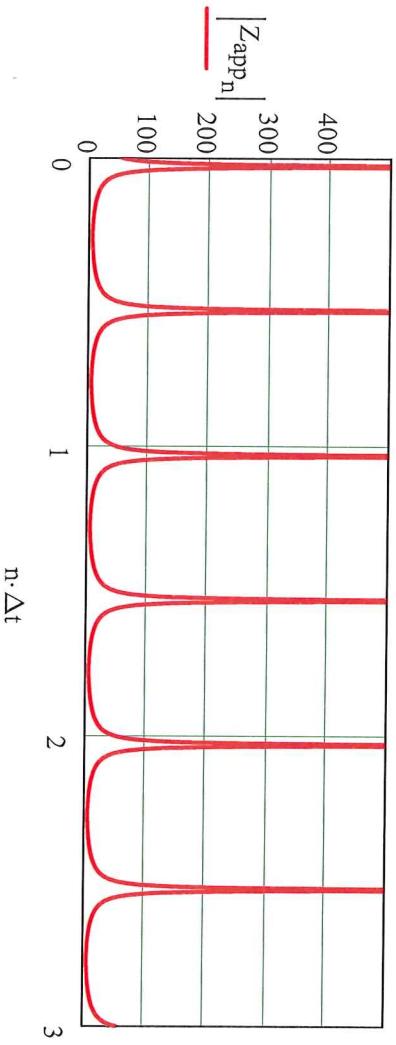
- Calculate apparent impedance seen by the relay using phasor voltage and current:

$$Z_{app_n} := \frac{V_{relay_n}}{I_{relay_n}}$$

-phasor

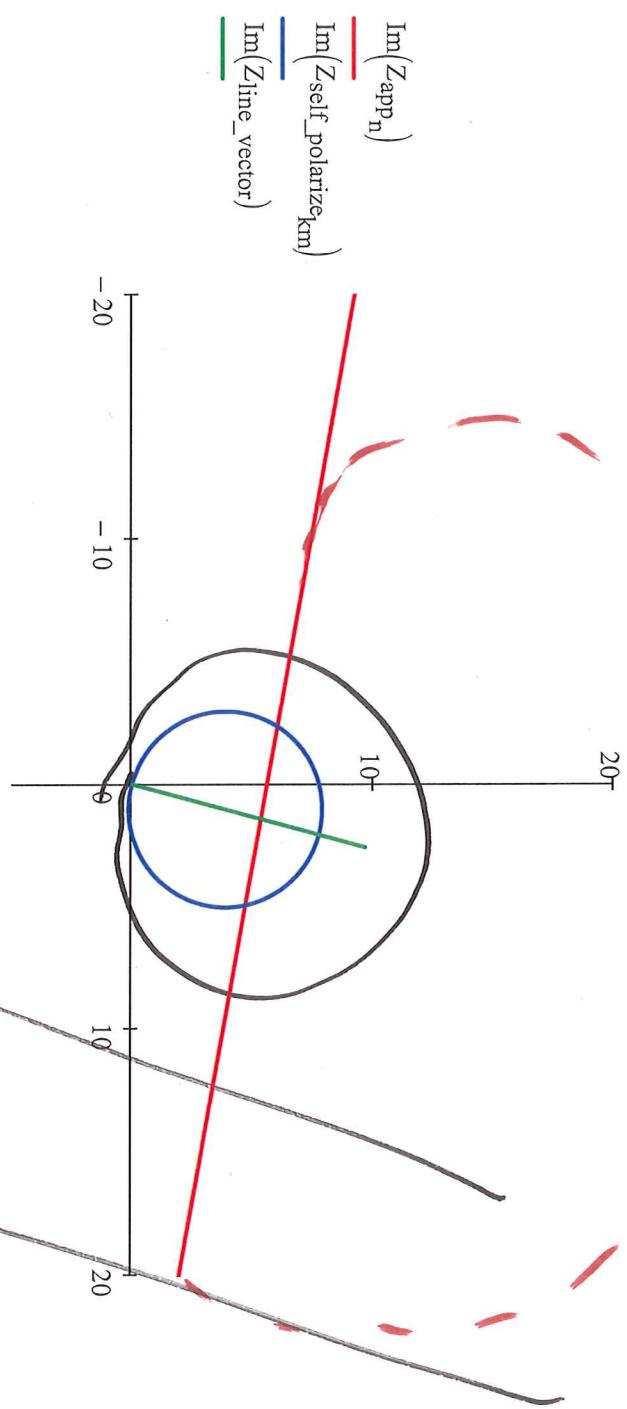


Plot with zoomed in vertical scale:

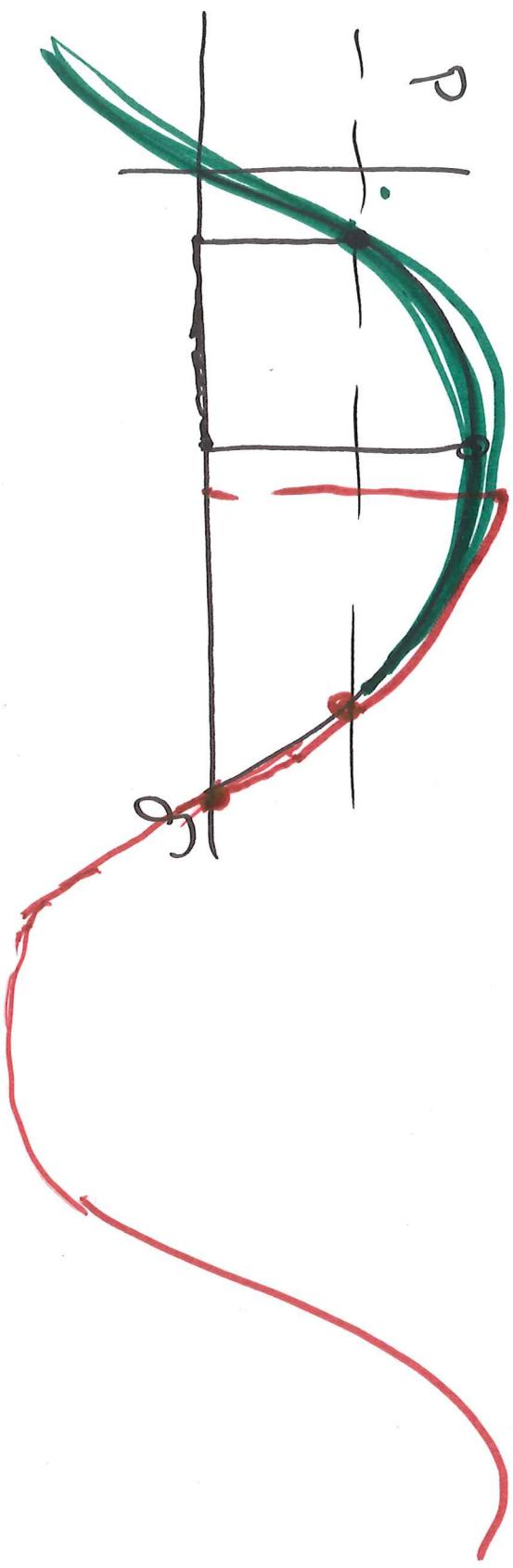


ψ_2 ψ_1

- Scale to show the mho circle and line impedance:



$\text{Re}(Z_{\text{app}_n}), \text{Re}(Z_{\text{self_polarize_km}}), \text{Re}(Z_{\text{line_vector}})$



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Approach 2: Apply a very simple 60 Hz cosine filter

$\text{spc} := 128 \quad \text{ncyc} := 120$

$i := 0 .. \text{spc} \cdot \text{ncyc} \quad k := \text{spc} - 1 .. \text{ncyc} \cdot \text{spc}$

$$t_{l_i} := \frac{i}{\text{spc} \cdot f_1}$$

Source Voltages in time domain

$$V_{1i} := 100V \cdot \sqrt{2} \cdot \sin(2 \cdot \pi \cdot f_1 \cdot t_{l_i}) \quad V_{2i} := 100V \cdot \sqrt{2} \cdot \sin(2 \cdot \pi \cdot f_2 \cdot t_{l_i} - 20\text{deg})$$

Phasors for Sources from a simple filter approximation

$$V_{1\text{cpxk}} := V_{1k} + j \cdot V_{1} \underbrace{\text{cpxk}}_{k - \frac{\text{spc}}{4}} \quad V_{2\text{cpxk}} := V_{2k} + j \cdot V_{2} \underbrace{\text{cpxk}}_{k - \frac{\text{spc}}{4}}$$

Voltage difference $V_{\text{Difcpxk}} := V_{1\text{cpxk}} - V_{2\text{cpxk}}$

$$\text{Line Current} \quad I_{\text{cpxk}} := \frac{V_{\text{Difcpxk}}}{Z_{S1} + Z_{L1} + Z_{R1}}$$

$$\text{Relay voltage} \quad V_{\text{Relayk}} := V_{1\text{cpxk}} - I_{\text{cpxk}} \cdot Z_{S1}$$

$$v_{a_n} := \sqrt{2} \cdot |100V| \cdot \cos(\omega_{s1} \cdot T \cdot i \cdot n + 0)$$

$$v_{b_n} := \sqrt{2} \cdot |100V| \cdot \cos(\omega_{s2} \cdot T \cdot i \cdot n + \delta_0)$$

$$\text{Relay Sampling Rate } K := 32 \quad k_s := 0, 1..31$$

$$\text{Number of cycles } N := 64 \quad o := 0, 1..N \cdot K - 1$$

$$M \leftarrow \text{submatrix}(v_a, x \cdot 2, x \cdot 2 + 31, 0, 0)$$

$$\text{val}_x \leftarrow \frac{2}{K \cdot \sqrt{2}} \sum_{k_s} \left(M_{k_s} \cdot e^{-i \cdot 2 \cdot \pi \cdot \frac{k_s}{K}} \right)$$

val

$$VB := \begin{cases} \text{for } x \in 0, 1..(N) \cdot K - 1 \\ M \leftarrow \text{submatrix}(v_b, x \cdot 2, x \cdot 2 + 31, 0, 0) \\ \text{val}_x \leftarrow \frac{2}{K \cdot \sqrt{2}} \sum_{k_s} \left(M_{k_s} \cdot e^{-i \cdot 2 \cdot \pi \cdot \frac{k_s}{K}} \right) \\ \text{val} \end{cases}$$

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OUT OF STEP CALCULATIONS AND SIMULATIONS

$$f := 60\text{Hz} \quad \omega := 2 \cdot \pi \cdot f$$

- Transmission Line Impedance:

$$Z_{1L} := 8\text{ohm} \cdot e^{j \cdot 87.6\text{deg}} \quad Z_{1L} = (0.335 + 7.993i)\Omega$$

$$R_1 := \text{Re}(Z_{1L}) \quad R_1 = 0.335\Omega$$

$$X_1 := \text{Im}(Z_{1L}) \quad X_1 = 7.993\Omega$$

- Thevenin Equivalent Sources:

$$E_S := 61.44V \cdot e^{j \cdot 50\text{deg}}$$

$$Z_{1S} := 1.776\text{ohm} \cdot e^{j \cdot 88\text{deg}}$$

$$E_R := 0.8 \cdot |E_S| \cdot e^{j \cdot 0\text{deg}} \quad E_R = 49.152V$$

$$Z_{1R} := 3.3\text{ohm} \cdot e^{j \cdot 88\text{deg}}$$

- Total Impedance:

$$Z_T := Z_{1S} + Z_{1L} + Z_{1R} \quad |Z_T| = 13.076\Omega \quad \arg(Z_T) = 87.755\cdot\text{deg}$$

- Load Current

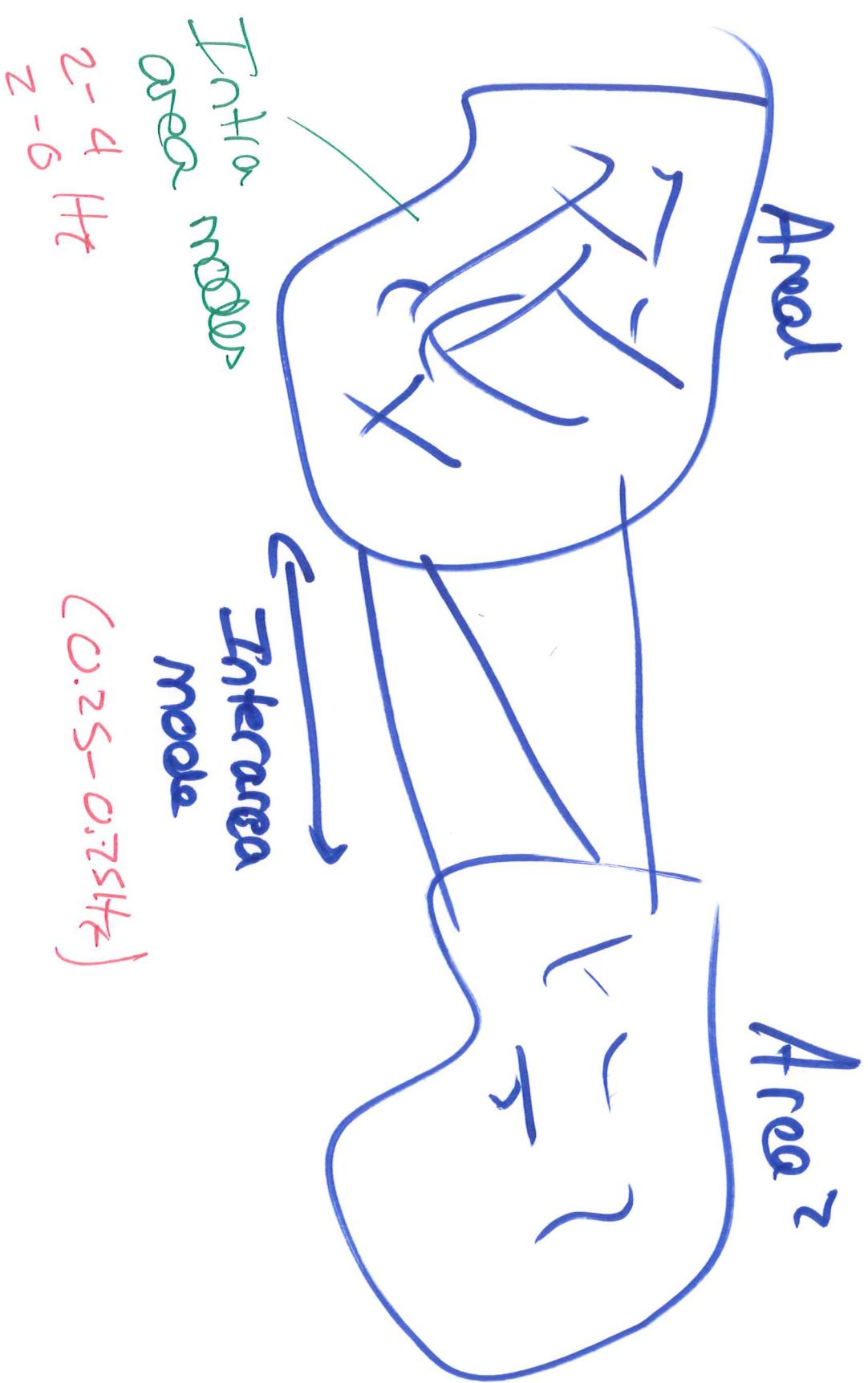
$$I_{\text{Load}} := \frac{E_S - E_R}{Z_T} \quad |I_{\text{Load}}| = 3.674A \quad \arg(I_{\text{Load}}) = 13.842\cdot\text{deg}$$

- Relay voltage during normal load conditions:

$$V_{R\text{Load}} := E_S - I_{\text{Load}} \cdot Z_{1S} \quad |V_{R\text{Load}}| = 57.637V \quad \arg(V_{R\text{Load}}) = 44.892\cdot\text{deg}$$

- Effective Load Flow Impedance

$$Z_{\text{Load}} := \frac{V_{R\text{Load}}}{I_{\text{Load}}} \quad |Z_{\text{Load}}| = 15.686\Omega \quad \arg(Z_{\text{Load}}) = 31.05\cdot\text{deg}$$



Determining the Right Resistive Blinders

Zone 5 Starting Load Angle:

$$\delta_5 := 90\text{deg}$$

$$\text{ANGIR} := \delta_5$$

Zone 6 Starting Load Angle:

$$\delta_6 := 60\text{deg}$$

$$\text{ANGOR} := \delta_6$$

Right Zone 5 Resistive Binder:

$$R1R5 := \frac{|ZT|}{2 \cdot \tan\left(\frac{\delta_5}{2}\right)}$$

$$R1R5 = 6.538 \Omega$$

Right Zone 6 Resistive Binder:

$$R1R6 := \frac{|ZT|}{2 \cdot \tan\left(\frac{\delta_6}{2}\right)}$$

$$R1R6 = 11.324 \Omega$$

Determining the Out-of-Step Blocking Delay (OSBD)

Slip frequency: $\text{slip} := 3\text{Hz}$

Load angle increment between Zone 6 and Zone 5:

$$\Delta\delta_{65} := \delta_5 - \delta_6$$

$$\Delta\delta_{65} = 30 \cdot \text{deg}$$

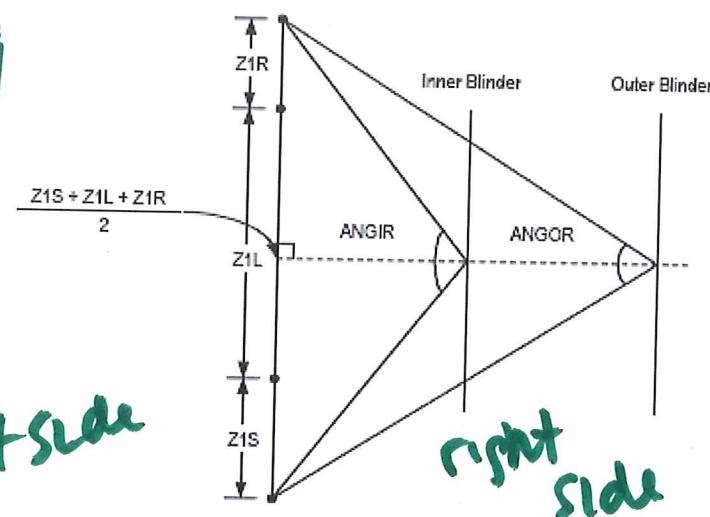
Time increment between Zone 6 and Zone 5:

$$\text{cycles} := 1$$

$$\text{OSBD} := \frac{\Delta\delta_{65} \cdot f}{\text{slip} \cdot 360\text{deg}}$$

$$\text{OSBD} = 1.667 \cdot \text{cycles}$$

Hz deg cycle



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Simulation Set up

Desired slip frequency: $ss := \text{slip}$

Desired angle between steps: $\Delta\delta := 0.1\text{deg}$

Number of steps: $N := 10000$

Initial step angle: $\delta_1 := 30\text{deg}$

Load angle steps:

$$k := 0..N-1 \quad n := 1..N-1 \quad k1 := 1..N-1$$

$$\delta_0 := \delta_1 \quad \delta_n := \delta_0 + n \cdot \Delta\delta$$

Time between steps:

$$\Delta t := \frac{\Delta\delta \cdot f}{ss \cdot 360\text{deg}} \quad \Delta t = 5.556 \times 10^{-3} \text{ s} \quad \Delta T := \Delta t$$

Create Time Vector:

$$t_0 := 0 \quad t_n := \frac{n \cdot \Delta t}{f} \quad \text{in cycles}$$

Source Voltages (allow angle for ES to vary relative to ER):

values $ES_k := ES \cdot e^{j \cdot \delta_k}$ $ER = 49.152 \text{ V}$ *LO*

Relay current for each step:

$$I_k := \frac{ES_k - ER}{ZT} \quad \text{Amps (rms)} \quad \beta a_k := \arg(I_k) \quad IM_k := |I_k|$$

Relay Voltage for each step:

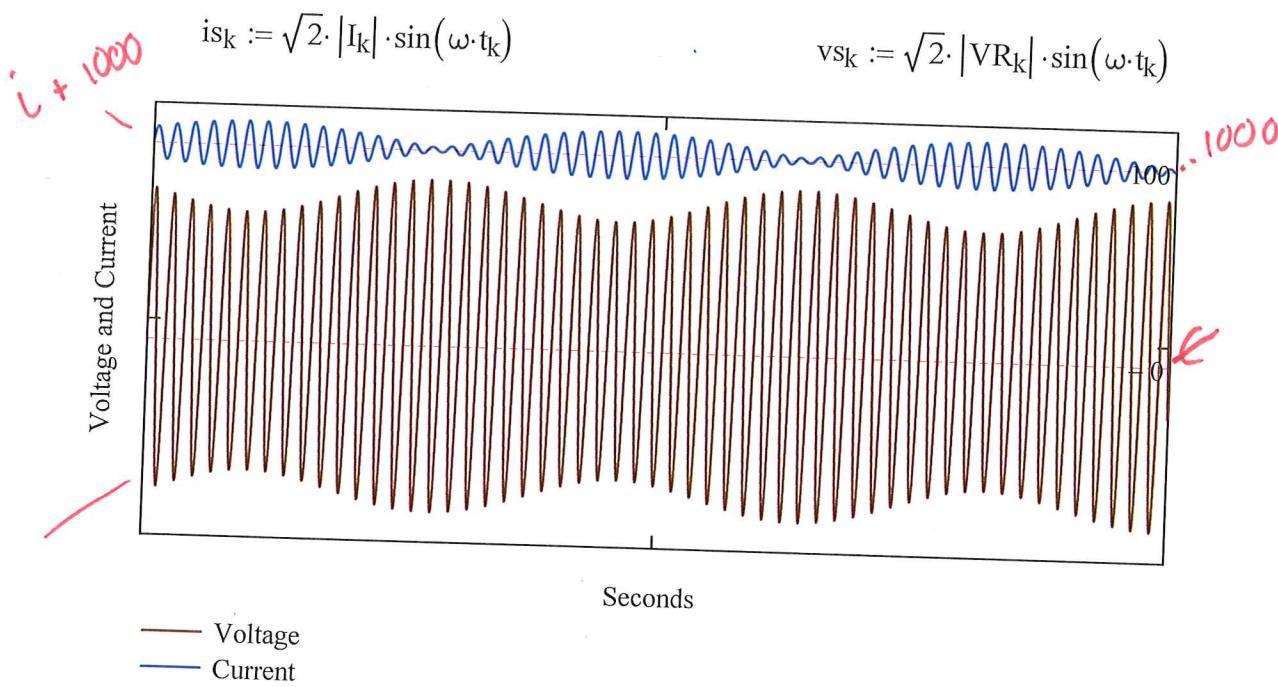
$$VR_k := ES_k - I_k \cdot Z_{1S} \quad \phi a_k := \arg(VR_k) \quad VM_k := |VR_k|$$

Apparent Relay Impedance:

$$Z\lambda_k := \frac{VR_k}{I_k}$$

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Instantaneous Current and Voltage at the Relay Location:



Now Plot Against a Mho characteristic:

Zone 2 Reach in pu of Z1L: $ZR := 120\%$

$$Z1 := ZR \cdot Z1L \quad |Z1| = 9.6 \Omega \quad m := 0, 1.. \frac{|Z1L|}{\text{ohm}}$$

$$Z_{\text{line}}_m := e^{j \cdot \arg(Z1L)} \cdot m$$

Define angle variation

$$\ell := 0, 1..360 \quad \varepsilon_\ell := 1 \cdot \text{deg}$$

$$Z1_\ell := \frac{Z1}{2} + \frac{Z1}{2} \cdot e^{j \cdot \varepsilon_\ell}$$

Vectors for Right side blenders:

$$y := -75, -74..75$$

$$R5_{y+75} := \frac{R1}{X1} \cdot y + \frac{\frac{|R1R5|}{\text{ohm}}}{\sin(\arg(Z1L))}$$

$$R6_{y+75} := \frac{R1}{X1} \cdot y + \frac{\frac{|R1R6|}{\text{ohm}}}{\sin(\arg(Z1L))}$$

$$ES := 61.44V \cdot e^{j \cdot 50\text{deg}}$$

$$|Z1L| = 8\Omega$$

$$|ER| = 49.152\text{ V}$$

$$|Z1S| = 1.776\Omega$$

$$\arg(Z1L) = 87.6 \cdot \text{deg}$$

$$|Z1R| = 3.3\Omega$$

$$\arg(Z1S) = 88 \cdot \text{deg}$$

$$\arg(Z1R) = 88 \cdot \text{deg}$$

Settings for OSB

Zone 2 Reach in pu of Z1L:

$$ZR = 120\%$$

$$Z2P := |ZR \cdot Z1L|$$

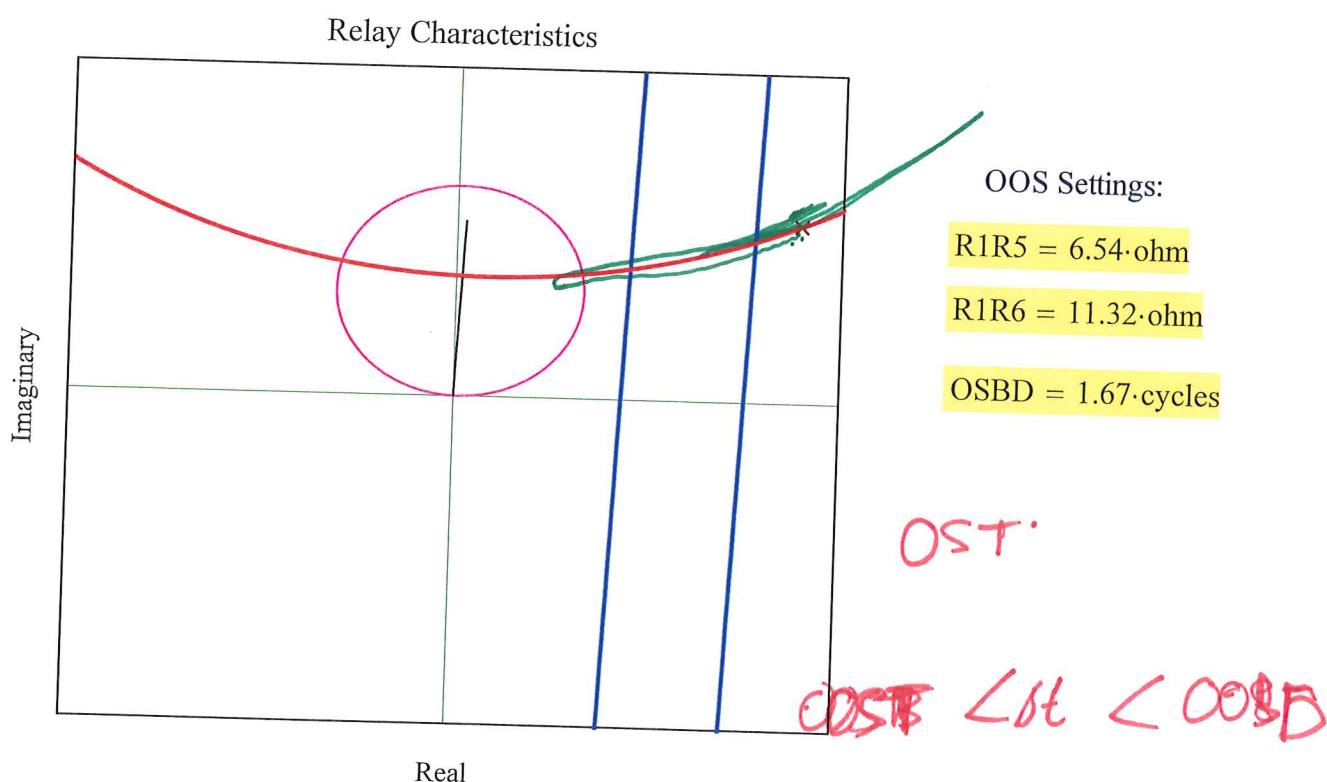
$$Z2P = 9.6\Omega$$

Maximum Slip frequency: slip = 3 · Hz

Zone 5 Entry Load Angle: $\delta_5 = 90 \cdot \text{deg}$

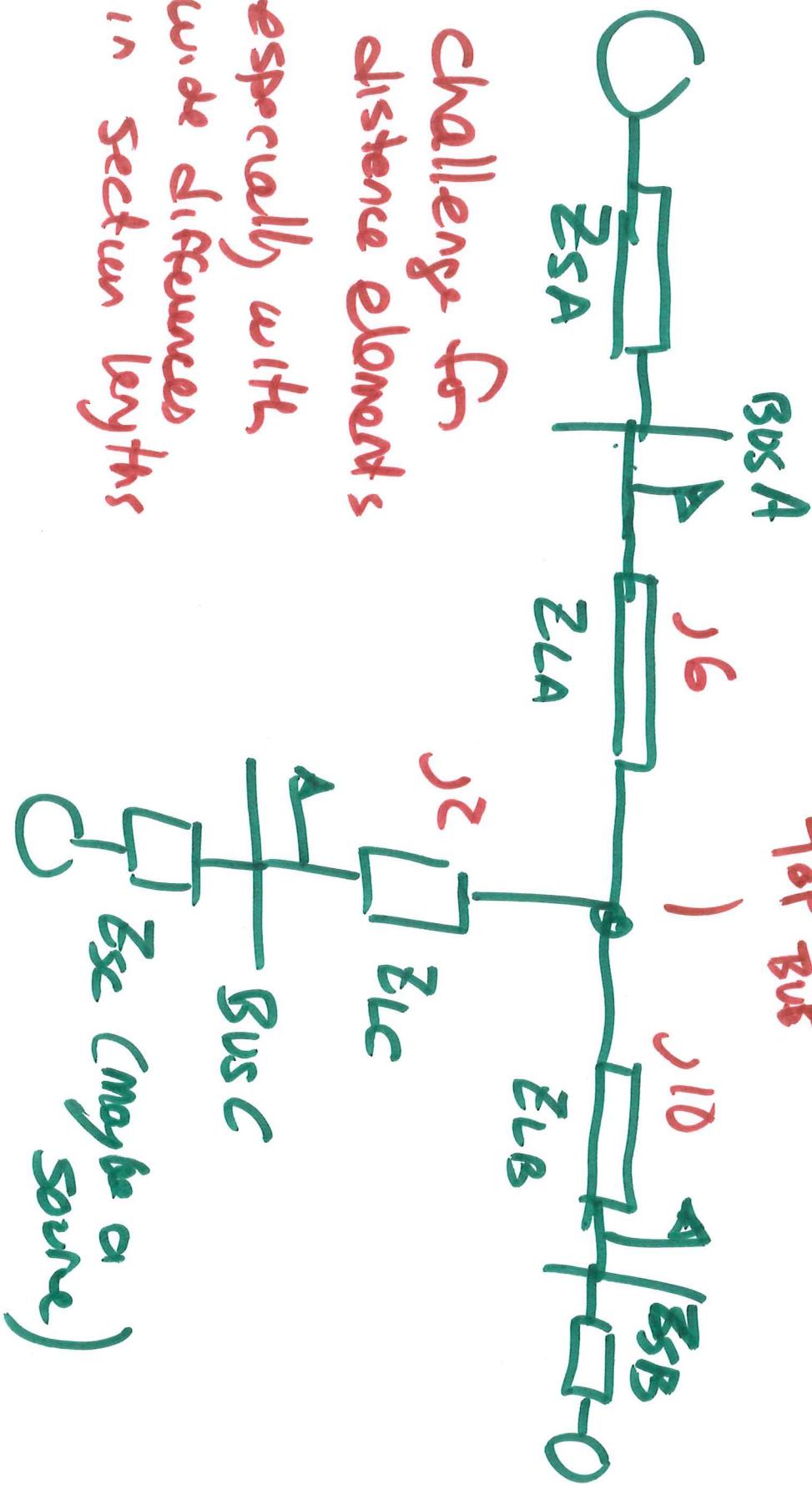
Zone 6 Entry Load Angle: $\delta_6 = 60 \cdot \text{deg}$

System Nominal Frequency: f = 60 · Hz



multi-terminal lines (Tapped lines)

Top (connection) bus
(no substations)



- challenge for distance elements
- especially with wide differences in section lengths

Challenges

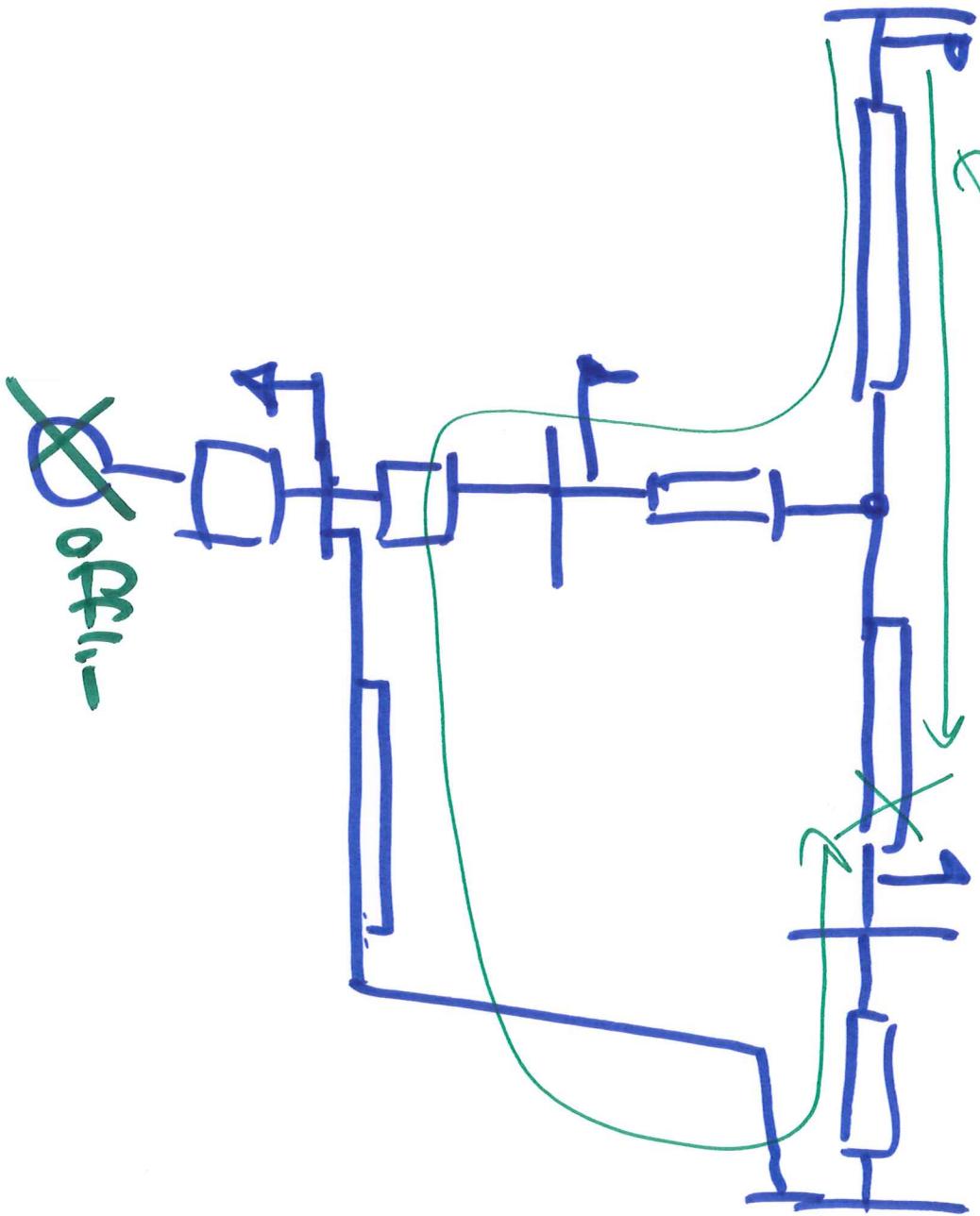
1. Setting Zone 1 coverage for uneven length sections (guarantee underreach)
- w/ infill

2. Setting Zone 2 coverage
- guarantee over reach
(w/ infill)

'n lead - underreach
causes -

3. Cross feed effects

- potential to overreach
cause



Setting distance

Zone 1 - several option

(relay A)

① Set Zone 1 at 80-~~85%~~ of

Z_{LA1}

Distance to the top point

needs
comm
coord for
a code for
high speed
trip
trip

- No high speed trip for faults
anywhere on all 3 breakers

② Zone 1: 80-90% of Z_{LA1} + min (Z_{LB1}, Z_{LC1})

90% (J6 + J2)

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$$\textcircled{3} \min d_{SO-90\%} \text{ of } \left(Z_{UA} + Z_{LB} \right) \text{ with infed}$$
$$\left. \begin{array}{l} Z_{UA} + Z_{LB} \\ -\text{Study} \\ \text{cross feed} \end{array} \right\}$$

requires more studies

Zone 2: overreach beyond for bus
for all terminals

$$Z_{SA} := 4\text{ohm}\cdot e^{j\cdot 82\text{deg}} \quad Z_{SB} := 5\text{ohm}\cdot e^{j\cdot 82\text{deg}} \quad Z_{SC} := 3\text{ohm}\cdot e^{j\cdot 82\text{deg}}$$

- Line impedances:

$$Z_{LA} := 2\text{ohm}\cdot e^{j\cdot 82\text{deg}} \quad Z_{LB} := 5\text{ohm}\cdot e^{j\cdot 82\text{deg}} \quad Z_{LC} := 3\text{ohm}\cdot e^{j\cdot 82\text{deg}}$$

Two options for setting zone 1:

Option 1: Set the Zone 1 to 85% of the line impedance to the tap point, Z_{LA} .

$$\rightarrow \boxed{Z_{Zone1_reach} := 0.80 Z_{LA}} \quad \boxed{|Z_{Zone1_reach}| = 1.6\Omega} \quad \arg(Z_{Zone1_reach}) = 82\text{-deg}$$

Option 2: Set the Zone 1 to 85% of the line impedance to the tap point, Z_{LA} plus the smaller of Z_{LB} and Z_{LA} without the infeed considered.

$$Z_{AplusB} := 0.85(Z_{LA} + Z_{LB}) \quad |Z_{AplusB}| = 5.95\Omega \quad \arg(Z_{AplusB}) = 82\text{-deg}$$

$$Z_{AplusC} := 0.85(Z_{LA} + Z_{LC}) \quad |Z_{AplusC}| = 4.25\Omega \quad \arg(Z_{AplusC}) = 82\text{-deg}$$

The smaller impedance is the case with Z_{LC} , so:

$$Z_{Zone1_reach_alt} := 0.85(Z_{LA} + Z_{LC}) \quad \boxed{|Z_{Zone1_reach_alt}| = 4.25\Omega} \quad \arg(Z_{Zone1_reach_alt}) = 82\text{-deg}$$

Set the Zone 2 reach to 120% of Z_{LA} plus the maximum apparent impedance to Bus B or Bus C with infeed included.

Apparent impedance from tap point to Bus B as seen from Bus A:

- The fault current will include a contribution from the source behind C
- Here is much more complete derivation if you're interested.

The first term can be rearranged by cancelling the V_f in the numerator and denominator, plus the $(Z_A + Z_C)$:

$$Z_{\text{appA_B}} = \frac{1}{\left[\overline{Z_A \cdot Z_C + Z_{LB} \cdot (Z_A + Z_C)} \right]} \cdot (Z_C) - Z_{SA} = \frac{\left[Z_A \cdot Z_C + Z_{LB} \cdot (Z_A + Z_C) \right]}{Z_C} - Z_{SA}$$

$$Z_{\text{appA_B}} = Z_A + Z_{LB} \cdot \frac{Z_A + Z_C}{Z_C} - Z_{SA}$$

- Now substitute for Z_A and Z_C .

$$Z_{\text{appA_B}} = Z_{SA} + Z_{LA} + Z_{LB} \cdot \frac{(Z_{SA} + Z_{LA}) + (Z_{SC} + Z_{LC})}{Z_{SC} + Z_{LC}} - Z_{SA}$$

So finally:

$$Z_{\text{appA_B}} := Z_{LA} + Z_{LB} \cdot \frac{(Z_{SA} + Z_{LA}) + (Z_{SC} + Z_{LC})}{Z_{SC} + Z_{LC}} \quad |Z_{\text{appA_B}}| = 12 \Omega \quad \arg(Z_{\text{appA_B}}) = 82.\text{deg}$$

- Similarly, the apparent impedance to a fault at Bus C as seen from Bus A:

$$Z_{\text{appA_C}} := Z_{LA} + Z_{LC} \cdot \frac{(Z_{SA} + Z_{LA}) + (Z_{SB} + Z_{LB})}{Z_{SB} + Z_{LB}} \quad |Z_{\text{appA_C}}| = 6.8 \Omega \quad \arg(Z_{\text{appA_C}}) = 82.\text{deg}$$

- Set Zone 2 reach using 120% of the the *larger* apparent impedance, which in this case is the one to Bus B.

$$\text{Zone2_reach} := 120\% \cdot \left[Z_{LA} + Z_{LB} \cdot \frac{(Z_{SA} + Z_{LA}) + (Z_{SC} + Z_{LC})}{Z_{SC} + Z_{LC}} \right]$$

$$|\text{Zone2_reach}| = 14.4 \Omega$$

- Notice that this overreaches the remote source impedances for either line. $\arg(\text{Zone2_reach}) = 82.\text{deg}$

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