

## ECE 320: Lecture 24

### Example

#### *Rotating Machine Case:*

Now put a loop of wire in a magnetic field. The loop is free to rotate.

Example:  $R := 0.3\text{ohm}$

$$V_{dc} := 120\text{V}$$

$$r := 0.5\text{m}$$

$$l := 1\text{m}$$

$$B := 0.25\text{T}$$

Initial Starting Current and Torque (no load)

$$I_{\text{start}} := \frac{V_{dc}}{R} \quad I_{\text{start}} = 400\text{ A}$$

$$\tau_{\text{init}} = \frac{2}{\pi} \cdot \phi \cdot I_{\text{start}} = 2 \cdot r \cdot l \cdot B \cdot I_{\text{start}} \quad \tau_{\text{init}} := 2 \cdot r \cdot l \cdot B \cdot I_{\text{start}} \quad \tau_{\text{init}} = 100\text{ N}\cdot\text{m}$$

- Steady-state rotational velocity at no-load

$$E_a := V_{dc}$$

$$\omega := \frac{E_a}{2 \cdot r \cdot l \cdot B} \quad \omega = 480 \frac{\text{rad}}{\text{sec}}$$

- No load with flux dropping to 0.2 T

$$B_2 := 0.2\text{T}$$

$$\omega := \frac{E_a}{2 \cdot r \cdot l \cdot B_2} \quad \omega = 600 \frac{\text{rad}}{\text{sec}}$$

Note that if B goes to 0, infinite speed.

B goes to zero if remove the field

Add 10 N-m load

$$\tau_{\text{load}} := 10 \text{ N}\cdot\text{m} \quad \text{opposing rotation}$$

$$I_{\text{load}} := \frac{\tau_{\text{load}}}{2 \cdot r \cdot l \cdot B} \quad I_{\text{load}} = 40 \text{ A}$$

$$E_{a\_load} := V_{dc} - I_{\text{load}} \cdot R \quad E_{a\_load} = 108 \text{ V}$$

$$\omega_{\text{motor}} := \frac{E_{a\_load}}{2 \cdot r \cdot l \cdot B} \quad \omega_{\text{motor}} = 432 \frac{\text{rad}}{\text{sec}}$$

$$P_{\text{in}} := V_{dc} \cdot I_{\text{load}} \quad P_{\text{in}} = 4800 \text{ W}$$

$$P_{\text{elec}} := P_{\text{in}} - R \cdot I_{\text{load}}^2 \quad P_{\text{elec}} = 4320 \text{ W}$$

Also for a rotating machine:

$$P_{\text{mech}} := \tau_{\text{load}} \cdot \omega_{\text{motor}} \quad P_{\text{mech}} = 4320 \text{ W} \quad \text{same as } P_{\text{elec}} \text{ is no friction/windage losses}$$

Generator

$$\tau_{\text{gen}} := 7.5 \text{ N}\cdot\text{m} \quad \text{in direction of rotation}$$

$$I_{\text{gen}} := \frac{-\tau_{\text{gen}}}{2 \cdot r \cdot l \cdot B} \quad I_{\text{gen}} = -30 \text{ A} \quad \text{reverse polarity of current in circuit...}$$

$$E_{a\text{gen}} := V_{dc} - I_{\text{gen}} \cdot R \quad E_{a\text{gen}} = 129 \text{ V} \quad \text{larger than } V_{dc}$$

$$\omega_{\text{gen}} := \frac{E_{a\text{gen}}}{2 \cdot r \cdot l \cdot B} \quad \omega_{\text{gen}} = 516 \frac{\text{rad}}{\text{sec}}$$

$$P_{\text{out}} := V_{dc} \cdot (-I_{\text{gen}}) \quad P_{\text{out}} = 3600 \text{ W}$$

$$P_{\text{elec}} := P_{\text{out}} + R \cdot I_{\text{gen}}^2 \quad P_{\text{elec}} = 3870 \text{ W}$$

Also for a rotating machine:

$$P_{\text{mech}} := \tau_{\text{gen}} \cdot \omega_{\text{gen}} \quad P_{\text{mech}} = 3870 \text{ W}$$